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# Interstitially stabilized phases in the zirconium-nickel system

Mackay, Richard Alan, Ph.D.

Iowa State University, 1993



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Interstitially stabilized phases in the

zirconium - nickel system

by

# Richard Alan Mackay

# A Dissertation Submitted to the

# Graduate Faculty in Partial Fulfillment of the

Requirements for the Degree of

### DOCTOR OF PHILOSOPHY

Department: Major:

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1993

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#### **1. INTRODUCTION**

The investigation of metal rich sulfides of the early transition metals has led to the discovery of several new compounds and has necessitated new explanations in the theory of bonding in extended solids. To illustrate this point, a report published in 1964 stated the compound Ti<sub>2</sub>S would be thermodynamically unstable with respect to disproportionation to the elements or to TiS and Ti, and hence would not form [1]. The thermodynamic calculations were based on the Kapustinskii equation [3] for an ionic model of bonding. Shortly afterwards, the crystal structure of Ti<sub>2</sub>S was The structure of Ti<sub>2</sub>S is very different from an ionic compound where Coulombic solved [2]. interactions between the metal and nonmetal provide the significant stabilizing force. The high coordination of titanium and the short titanium-titanium distances are evidence of the strong metalmetal interactions involved in this metal-rich sulfide and these interactions are not accounted for by considering only Coulombic interactions. The ability to calculate properties and predict the chemistry in this class of metal rich compounds depends on the ability to determine the effect of the presence of extensive metal-metal bonding, a factor not included in the ionic model. While the ability to predict new compounds and structures still lies in the future, the discovery of so many new materials with extensive regions of metal-metal bonding has motivated chemists to explain the electronic and structural features in these compounds. Before proceeding further, the term metal-rich should be defined more clearly. For any compound  $M_x X_y$ , where M is a metal atom and X is a nonmetal atom, one can quickly determine if x > y, however, this criterion tells nothing about the extent of metal-metal bonding or coordination environment of the metal. As it is the strength of this metal-metal bonding that is essential for the formation of these phases, a better criterion is the condition  $\sum n(M-M) / \sum n(M-X) > 1$ , where n is the Pauling bond order [4], as determined by the equation  $d(n) = d(1) - 0.6 \log n$ . Because of the empirical nature of this equation the individual bond orders calculated mean little by themselves, but the bond orders scale as indications of bond

strengths, and the comparison of the sum of all the metal-metal interactions with the sum of all the metal-nonmetal interactions does yield a meaningful definition of metal-rich compounds. With this in mind, the new oxygen stabilized phases found in this research are viewed as oxidized intermetallics rather than reduced metal oxides.

A number of metal-rich compounds have been discovered in this lab alone. Considering just the binary sulfides of the Group 4 and Group 5 elements, they include  $Ti_2S$  [2],  $Ti_8S_3$  [5],  $Zr_2S$  [6],  $Zr_{21}S_8$  [6],  $Zr_9S_2$  [7],  $Hf_2S$  [8],  $Nb_{21}S_8$  [9],  $Nb_{14}S_5$  [10],  $Ta_2S$  [11],  $\alpha$ - $Ta_6S$  [12],  $\beta$ - $Ta_6S$  [13]. Other groups in other laboratories have contributed to this work, synthesizing additional new compounds, such as a low temperature binary phase, Ta3S2 [14], and carrying out theoretical band energy calculations [15]. The results are immensely interesting and surprising. For example, for a given stoichiometry, M<sub>2</sub>S, the phases Ti<sub>2</sub>S, Zr<sub>2</sub>S, Hf<sub>2</sub>S, Ta<sub>2</sub>S exist. Within Group 4, the titanium and zirconium phases have the same structure, roughly based on bcc units in the metal framework. Dihafnium sulfide has a unique hexagonal structure, with close packed layers in the order ABACBC for Hf-S-Hf-Hf-S-Hf layers. In Group 5, the structure of the tantalum phase is different from either of those in Group 4, being built of chains of interpenetrating icosahedra. No phases of this stoichiometry form at all for vanadium or niobium. All of the phases are characterized by high sulfur coordination, often with capped trigonal prismatic coordination, and with sulfur occuring as a substituent on metal sites in bcc fragments. The tantalum sulfides have distinctive icosahedral chains. The zirconium and niobium phases are built up of bcc units. The compounds formed by the elements grouped together within a column of the Periodic Table are distinguished as much by their differences as by their similarities, if not more so. Naturally, it is these differences that are of interest to the chemist.

Exploiting the differences between the tantalum sulfides and the niobium sulfides, X.Yao discovered several new ternary metal rich compounds in the Ta/Nb/S system [16-19]. These

compounds form only in the ternary system and form structures stabilized entropically by a mixing of tantalum and niobium on the metal sites. The results of band calculations on two of these phases indicate also the importance of the relative strength of the metal-metal and the metal-nonmetal bonds in determining the ordering of niobium and tantalum on the mixed metal sites [19]. This result has been generalized to include several mixed-metal phosphides and sulfides [20]. Similarly, an investigation of mixed-metal sulfides of mixed Group 4 and Group 5 metals has yielded exciting results. A new structure  $Hf_{10}Ta_3S_3$  is related to the gamma brass structure, with sulfur filling large channels. Other phases, such as  $Zr_9Ta_4S_{4-x}$ , are new examples of kappa phases, with metal frameworks made up of early transition metals [21]. In a like manner, there are investigations on the mixing of sulfur and selenium in metal rich systems. That is to say,  $Ta_2S$  and  $Ta_2Se$  have different structures, so the ternary Ta/S/Se system is not necessarily expected to contain large solid solubility regions, and the ternary system may include interesting new phases [22].

The formation of these metal-rich compounds has always involved the early transition metals. The specific examples cited so far have been from Groups 4 and 5. Binary metal-rich compounds are not known to form for the later transition metals [23]. The ability of the early transition metals to fill vacant d-orbitals in forming metal-nonmetal bonds through interactions with the nonmetal, and maintain significant metal-metal bonding seems a necessary condition for the formation of these compounds. As the late transition metals have few vacant orbitals they do not meet this condition and binary metal rich sulfides of late transition metals do not form.

The question arises of what might happen in ternary compounds with mixed early transition metal-late transition metal frameworks. Although initially begun as an effort to place iron group metals in the sulfur - lined channels of the Ta<sub>2</sub>S structure, the discovery of  $M_2Ta_9S_6$  (where M = Fe, Co, Ni) suggested new possibilities in structures and properties of metal rich compounds [24,25]. Significantly, the structure contains only M-Ta, Ta-Ta, and Ta-S interactions, but no M-S

interactions. The structure consists of a hexagonal metal network, with large channels lined by sulfur atoms, a feature similar to  $Ta_2S$ . A theoretical band structure calculation suggests that filling the sulfur-lined channels of  $M_2Ta_9S_6$  with metal atoms might be energetically favorable [26]. This suggestion neglects the inference that these channels are not void regions at all; they contain nonbonding, lone pair orbitals of sulfur. The sulfur atoms are separated by van der Waals' contacts within the channels. Presumably that is why the addition of the metal M atoms to  $Ta_2S$  caused a rearrangement of the structure, rather than a filling of the channels. Additional new ternary phases include Nb<sub>9</sub>Ni<sub>2-x</sub>S<sub>3+x</sub>[27] and M<sub>2</sub>Ta<sub>11</sub>Se<sub>8</sub> (where M = Fe, Co, Ni) [28]. These results in the ternary systems of mixed early and late transition metals again confirm the differences that exist in chemical behaviour between niobium and tantalum, as was found in the binary sulfides.

The research project described in this dissertation began as an investigation of the ternary system of mixed early-late transition metal compounds involving zirconium rather than niobium or tantalum as the early transition metal. Based on the known binary phases of metal-rich sulfides, and the observed differences between the Group 4 and Group 5 compounds, as well as the novel features in the ternary phases, there was no way of predicting what phases might form, but it was highly probable new phases would form.

This research has in fact led to the discovery of several new phases. The results, however, have taken a somewhat different path than the work previously described. Several new phases have been discovered, but rather than new sulfides, these phases are all new oxides. The presence of oxygen, adventitious or not, is a well documented problem in the synthesis of solid state compounds. Modem instrumentation has increased the solid-state scientists' capability of detecting the presence of small impurity atoms in samples. For example, the intensity of X-ray diffraction depends on the amount of electron density within the unit cell of the crystal, and the geometrical distribution of the electron density. Light elements such as oxygen have less electron density than transition elements

and are less easily observed by single crystal X-ray diffraction techniques. The increased intensity in X-ray beams available with a rotating anode as the X-ray source enables sufficient collection of even the weak data points to satisfactorily refine the light atom positions in the structure. This has been an important factor in the success of this research. Neutron diffraction, although not a common procedure, is now a standard procedure, and is in a number of cases inherently better for locating light atoms since it does not depend on electron density. In addition, elemental analysis of bulk samples, such as by Energy Dispersive X-ray Spectroscopy or EDS, can help identify the presence of impurity atoms.

Techniques have also been improved so as to eliminate, or reduce, the likelihood of oxygen contamination in solid state reactions. Whether the oxygen comes from surface oxides on the starting material, or from residual gaseous oxygen in the reaction chamber, or from reaction with the container, the end result is the same - an oxide phase forms. Each source of oxygen must be eliminated to form oxygen free samples. The presence of surface oxides can be reduced by using foils, with less surface than powders, which are etched or cleaned before using. This use has the disadvantage of providing less surface area for reaction with the desired reactants. This is of no consequence in arc-melting, but is important for diffusion-limited reactions. Alternately, bulk metals can be converted to the hydride, and subsequently dehydrided. Sample containers can also be a source of oxygen. Samples heated in fused silica ampoules, SiO<sub>2</sub>, are susceptible to reaction directly with the container, which contains oxygen, as well as with oxygen in the form of water, absorbed within the walls of the glass, which degasses at temperatures above 1000°C. Of course, if the sample melts it may react with the container whether the container is silica, alumina, zirconia or any other refractory material. A common technique now in use is to carry out reactions in inert metal containers. These containers can be sealed under an inert gas, and subsequently sealed in an evacuated silica tube. Another technique, used exclusively in this research, is the use of tungsten

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crucibles and heating of the samples under a dynamic vacuum in an induction furnace. The Knudsen cell design of the tungsten crucibles actually creates a condition within the cell that is more reducing than the residual atmosphere that can be achieved by pumping [30]. Tungsten oxides are volatile and pumped out. As noted by previous workers in the zirconium sulfide system, reaction with the crucible can result in the formation of  $W_2Zr$  [29].

The effectiveness of these techniques for the careful exclusion of oxygen is evident in the number of new compounds which have been discovered, and which would not form in the presence of oxygen. The early transition metals have a high affinity towards oxygen, and the formation of oxides is often thermodynamically favorable to the formation of oxygen - free compounds. Thus, although the metal - rich sulfides are often quite stable with respect to oxidation under ambient conditions, they do not form in the presence of oxygen. The exclusion of oxygen has been so effective it has perhaps led chemists to believe the interesting phases do not contain oxygen. The results of this research certainly show the interesting aspects of oxygen - stabilized phases, that is, phases which form only in the presence of small amounts of oxygen. Subtleties in the structural chemistry of these oxygen - stabilized phases are more clearly understood with the single crystal X-ray diffraction studies carried out and the improved ability to detect the light elements by X-ray crystallography.

At first glance, there is not an obvious connection between the sulfides described earlier, and the oxides studied in this research. Indeed, the differences between the sulfides and the oxides in the metal rich compounds are readily apparent. First, sulfur is larger than oxygen. That is to say, sulfur occupies larger crystallographic sites, and can be more highly coordinated. Second, oxygen is more electronegative than sulfur; the energy levels of oxygen 2p orbitals lie at lower energies than do those of sulfur 3p. The bonding overlaps will be different in oxides than in sulfides, and the nature of the bonding will be different. The sulfur in binary metal - rich sulfides has been described

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as having directional, delocalized bonds [31]. Oxygen orbital overlaps are more localized. The results of these differences are twofold. First, because of the size difference, oxygen can often occupy small vacant so-called interstitial sites within a metal framework, without significant structural distortion of the framework. Hence, many oxygen stabilized compounds are called after a parent structure type, i.e.  $Zr_3NiO$  has the filled  $Re_3B$  type structure, and  $Zr_4Ni_2O$  has the filled Ti<sub>2</sub>Ni type structure. Sulfur, on the other hand, is larger, and occupies larger interstitial sites, or can occupy smaller vacant sites only by making the site larger, with a corresponding expansion in the metal framework, as observed for the new sulfur-containing kappa phases and stuffed gamma brasses [21]. The second effect is seen in the ability of sulfur to, in essence, become part of the metal framework, i.e. substitute on a metal atom position in the bcc units in the niobium sulfides, or the layered compounds of mixed niobium/tantalum sulfides, with an accompanying distortion in the framework. The metallic character of sulfur becomes apparent in these phases - that is, the ability of the sulfur orbitals to be involved in delocalized bonding in the conduction band. The corollary to this, then, is the substitution of a metal atom on a sulfur site, as in  $Nb_9Ni_{2-x}S_{3+x}$  [27], and in the kappa phase  $Zr_9W_4(S,Ni)O_3$  [80]. One might object to describing the sulfur in these metal-rich sulfides as interstitial atoms. The metal-rich sulfides are novel structures, and the metal frameworks within these structures are also novel. To avoid overextending the use of the term "interstitial", rather than characterizing the sulfur as interstitial sulfur, the mixed tantalum/niobium sulfides and mixed early-late transition metal sulfides are here referred to as sulfur-stabilized intermetallics. The presence of small amounts of sulfur (up to 6 metal atoms for each sulfur atom) enables the formation of new phases which do not exist in the binary intermetallic phases. In a similar way, by calling the new phases oxygen stabilized, it is recognized that the phases do not form in the binary zirconium-nickel intermetallic system. By calling them interstitially stabilized one notes the oxygen atoms occupy small sites which are known to be vacant in some intermetallic compounds

with the same local structural arrangement. Whether considering sulfides or oxides, the structural chemistry is dominated by the fact that the presence of either of these nonmetal atoms effects the metal-metal bonding in intermetallics. The resulting balance of metal-metal and metal-nonmetal interactions results in new phases, and gives clues about the nature of the bonding.

Specifically, to note the change in the bonding that results from interstitial oxygen, consider the binary zirconium - nickel system. There are eight known phases in this system:  $Zr_2Ni$ , ZrNi,  $Zr_9Ni_{11}$ ,  $Zr_7Ni_{10}$ ,  $Zr_8Ni_{21}$ ,  $ZrNi_3$ ,  $Zr_2Ni_7$ ,  $ZrNi_5$  [32]. The phase diagram is complex, and the variation in structure and stoichiometry is striking. Classical chemical concepts, such as oxidation numbers, are not useful in intermetallic systems. Oxidation numbers, such as  $Zr^{+1}$  and Ni<sup>-1</sup> for ZrNi, that would have any meaning throughout the series of phases, or even for that particular phase cannot be simply assigned. Intermetallic compounds characteristically fill space efficiently, and the atoms have correspondingly high coordination numbers. The bonding cannot be interpreted as containing two-centered - two-electron bonds. Rather, the bonding within these compounds involves extensive delocalization of electrons.

Today, band calculations can give quantitative analysis of bonding in many known solids. Earlier interpretations of intermetallic compounds were more qualitative. One prevalent concept was the radius ratio rule. This was based on a model of packing of hard spheres. Crystal structures of intermetallics could be generalized, as Laves did, as arrangements of spheres which pack to exhibit high symmetry, fill space most efficiently, and have the greatest number of connections between the atoms [33]. In a general sense this was useful because certain structure types appear over and over in intermetallic systems. There are two weaknesses of this model, however. The idea of hard sphere packing gives no chemical understanding to the structures. Atoms are not hard spheres. A completely nondirectional nature of bonding results. It also led to a proliferation of tables of radii to be used which would satisfy the radius ratio rules for the new structures constantly being discovered. Tables for radii take into account all possible factors influencing interatomic distances, including atomic charge and coordination number [34-38]. One result of the use of this model was the rationalization of the reported nonoccurrence of the  $Ti_2Ni$  type structure in the Zr/Ni/O system [39], a phase this study shows does indeed exist. A recent study has successfully classified the structures that form for all binary, ternary and quaternary compounds [110]. This method also depends on the size differences of the constituent atoms, but uses this parameter along with the electronegativity differences of the atoms, and the sum of the valence electrons. The consideration of these three parameters together, rather than individually, increases the success and usefulness of the classification.

While the radius-ratio rules and structural classification are based on purely structural considerations, and no chemical considerations, the concept of Lewis acid - base behavior as it relates to the interactions among the transition metals does not explain structures of intermetallics. Late transition metals have paired electrons in d orbitals unavailable for bonding. Early transition metals have empty d orbitals. The sharing of electrons between late transition metals, acting as Lewis bases, and early transition metals, acting as Lewis acids, increases the total number of electrons available for bonding, and increases bond strength. This concept explains why compounds such as HfPt<sub>3</sub> have such favorable enthalpies of formation [40-41]. In the binary zirconium/nickel system one would expect strong zirconium - nickel bonds according to the their Lewis acid - base properties. From the crystal structures of the phases that form in this system, one can indeed see the high coordination of zirconium by nickel, and of nickel by zirconium, as well as zirconium - zirconium and nickel - nickel contacts.

The Brewer-Engel theory relies heavily on the concept of Lewis acid-base interactions and gives a structural component to the concept. The qualitative aspects have been highly successful in predicting the structure and properties of new compounds [42-43]. The structure, or long range

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electronic ordering is determined by the number of s and p electrons. The electrons in the d orbitals are involved in short range interactions. To count the electrons in the s and p orbitals correctly one must consider the electronic configuration of the atom as it is in the compound, not in the electronic ground state of the gaseous atom. For those phases that form, according to the theory, the energy necessary for promotion of electrons from the ground state is more than offset by the bonding energy gained.

One deficiency of this method is the treatment of interstitial elements. They are considered in this model, if at all, only as electron acceptors or electron donors. They are not considered to have an influence on bonding within the network. They are hard spheres which fill space. The effect of adding interstitial atoms is only to possibly change the number of electrons in the s and p orbitals, which may then favor a structure different than that adopted by the interstitial-free compound. A more chemically sound explanation in terms of bonding comes from band theory. In the rigid band approach the addition of oxygen to an intermetallic system provides energetically low-lying core levels, which are filled by electrons from the conduction band, thus the number of electrons in the conduction band changes, and a corresponding change in structure may be energetically favorable. Furthermore, the addition of oxygen, and the donation of electrons from the conduction band implies the formation of metal-oxygen bonds, and as these bonds form, there is a simultaneous change in the metal-metal bonding within the metal framework, which may favor formation of a new phase.

The idea of electron counts is an important one. Hume-Rothery suggested certain electron concentrations as being important for formation of certain phases. Several systems have been studied in which structural changes corresponding to modification of electron counts by substitution of more or less electron rich elements, or by addition of interstitials, have been observed. This conceptual understanding of electron count and the role of interstitials in intermetallics is being

supported by recent band energy calculations [44,45].

Typically, when an interstitial element reacts with a binary early-late transition metal compound to form a ternary compound, the compound crystallizes in a common structure type. In fact, only a limited number of structure types are known for interstitially - stabilized phases of mixed early and late transition metals [46]. These phases are: 1) the filled Ti<sub>2</sub>Ni type, 2) the kappa phase type, 3) the filled Re<sub>3</sub>B type, 4) the filled  $Mn_5Si_3$  type (known for Nb-M-O where M = Ir, Pt), and 5) the cubic Laves phase observed in the Zr-Ni-O system [47,48]. The first three of these types are found in the zirconium - nickel system with the addition of interstitial atoms, and make up the body of this research. In order of appearance in this dissertation, a single crystal study of the previously reported Zr<sub>3</sub>NiO phase, of the filled Re<sub>3</sub>B type structure, is presented first. Following this is a discussion of a series of compounds of the filled Ti<sub>2</sub>Ni type, involving the early transition metals zirconium and niobium, and mixed zirconium/titanium and niobium/tantalum. A discussion of the results of band calculations for this phase is included. New zirconium kappa phases have been found and are reported next. Finally, a new structure type has been found for an interstitially stabilized phase made up of a ternary metal framework of zirconium - titanium - nickel. The ternary metal system, Zr-Ti-Ni, contains phases which do not occur in either of the binary systems Zr-Ni or Ti-Ni (i.e. the hexagonal Laves phase ZrTiNi [9,10], and the BaPb<sub>3</sub> type structure ZrTi<sub>2</sub>Ni<sub>9</sub> [11,12]). It is natural to expect that interstitials in this ternary system may stabilize new compounds, with respect to the ternary intermetallics and interstitially stabilized binary compounds.

#### 2. EXPERIMENTAL TECHNIQUES

#### Synthesis

This section contains information on experimental techniques common to all the experiments performed in this work. Specific details will be included in the individual sections. The experiments were designed to take advantage of the equipment available in the lab. Specifically, the synthetic procedure of metal rich compounds generally consists of arc melting of the initial reactants, followed by annealing the samples.

Arc melting was performed with a CENTORR Model 5SA Single Arc Furnace, powered by a Hanovia Model 28151 Compact Arc Lamp Power System. Samples of between 0.5 and 1.5 grams were placed on a water cooled copper hearth, and melted under argon by an arc formed between the sample and a thoriated non-consumable tungsten electrode. Depending on the sample, current output was between 50-100 Amps D.C. There has been no indication of contamination by copper in arc melted samples in any of the previous work done in this lab. Likewise, there has been no evidence of copper contamination in any of the samples in this work, either by the formation of copper containing phases, or as detected by elemental analysis. A more significant source of contamination is atmospheric oxygen. The chamber is pumped by a mechanical pump, and backfilled with argon. This pump/purge cycle is repeated 3-5 times, and the chamber is left with a positive pressure of argon (~ 3 atm). A safety valve releases pressure at 6 atm. To remove residual oxygen in the chamber prior to melting the sample, a zirconium metal piece is melted first for 30-60 seconds as an oxygen getter. The calculated collision frequency is sufficiently high that the high reactivity of zirconium towards oxygen is expected to be effective in reducing the amount of oxygen present which may contaminate the sample. This has been true for work done on sulfides, and holds true for this work with oxides. After the initial discovery of the oxides as minor phases, it was desirable

to find a way of controlling the amount of oxygen present in the sample and thus synthesize bulk samples of the desired phases. This was accomplished by preparing samples, by arc melting, using a stoichiometric amount of a metal oxide. Other sources of oxygen were reduced to a minimum. Surface oxides on the metals were reduced by using metal foils rather than powders. The surface oxides were removed by cleaning with acid solutions immediately prior to use. This was most important for compounds containing titanium and zirconium, both of which are very reactive towards oxygen. The reactivity of these metals to oxygen indicates the high stability of the oxides with respect to the elements. The fact that these metal oxides can be used as reactants in these reactions indicates the high stability of the products with respect to the oxides and the competing intermetallic phases. A problem can arise in the reaction of oxides in that it is difficult to arc melt insulating materials. They often splatter, or fly apart when the arc comes in contact with them. A generally successful technique was to place the oxide powder between layers of metal foils. The arc was brought in contact with the edge of the foil and slowly moved toward the center. In this way the small amount of oxide present dissolved and reacted with the molten metal and the sample maintained its conductive, metallic properties. Typically a sample was arc melted three times, for approximately one minute each time, the sample being turned over each time to increase homogeneity.

Despite this procedure, the arc melted samples are generally not homogeneous due to the large difference in cooling rate between the part of the sample in contact with the water cooled copper hearth and the top of the sample. All of the samples prepared were between 0.5 and 1.5 grams, and within this range sample size had no apparent affect on homogeneity. The arc melting procedure was often very clean, with little mass loss due to vaporization. The most volatile species was nickel, and if samples were arc melted for longer times the loss of nickel was detected by mass loss as well as by formation of  $ZrO_2$  from the excess zirconium.

The samples show no evidence of decomposition or reactivity with air or moisture, and all subsequent handling was done in air. The homogeneity of the samples could be improved by annealing samples after arc melting. Two types of furnaces were available for annealing. The Marshall/Thermcraft and Astro furnaces are tube furnaces with capabilities of reaching 1200°C. Samples were placed in fused silica tubes, 10 mm I.D., 12 mm O.D., and evacuated to 10<sup>-5</sup>-10<sup>-6</sup> torr using an oil diffusion pump backed by a mechanical rough pump. Sometimes the samples were annealed as a button resulting from the arc melt. However, greater homogeneity resulted from first crushing the arc-melted button to a powder in a diamond mortar and cold pressing the powder to form a pellet for annealing. When samples were placed in the silica tube, the tubes were heated while they were being evacuated to try to eliminate as much moisture from the walls of the silica as possible, and finally sealed under vacuum. Sealed tubes were typically 120-150 mm in length. To ensure the vacuum was not lost in the sealing step each tube was gently heated. If the walls slowly collapsed, this was taken as evidence that the tube was still under vacuum. A single sample was placed in each tube, but several tubes could be placed in the furnace at once. Samples were annealed at varying temperatures, as low as 800°C, but generally not above 1000°C where reaction with oxygen from moisture degassed from the walls of the silica container is more likely.

Annealing at higher temperatures was performed in a Lepel High Frequency Induction Heating Unit. This unit contained a Lepel High Frequency Generator T-20 with Thyratron Regulator T-660. A quarter inch copper tube carried the high frequency field, and surrounded the water cooled quartz jacket which in turn surrounded the sample. The sample chamber was under a dynamic vacuum maintained by an oil diffusion pump backed by a mechanical pump. The sample was not heated until the pressure within the chamber, measured by an ion gauge, was  $10^{-6}$  torr. The pressure within the chamber could become as low as  $10^{-8}$  torr. The samples were placed in tungsten crucibles. Tungsten is a suitable container for annealing several intermetallics and oxides, as long

as the sample does not melt. Samples containing zirconium that melted in the crucible often form  $W_2Zr$ . Surprisingly, the new kappa phase  $Zr_9W_4(S,Ni)O_3$  was formed because of reaction between the sample and container. Melting the sample is to be avoided exactly for this reason. It is much easier to include tungsten in the starting material than to use the container as a reactant. The presence of a low melting phase, melting below 1000°C, presumably the cubic Laves phase in the Zr-Ni-O system [47,48], often resulted in reaction of the sample with the container. To avoid melting samples some were heated in the crucible without a lid. Thus, it could be visually determined whether or not the sample had melted during the annealing procedure. However, this procedure is not without consequence. The temperature of the sample in the induction furnace is determined by optical pyrometry. Each tungsten crucible is made with a hole in the bottom from which nearly black body radiation is emitted. The sample temperature within a closed crucible is higher than the sample temperature within an open crucible, without a lid, when the temperatures read by the pyrometer in the two cases are equal. For this reason, temperatures as measured were used for comparison between samples, and are not to be taken as actual temperatures. No attempt was made to calibrate these measurements. No corrections are applied to pyrometer readings for loss of intensity from passing through the quartz windows or reflectance from the mirror. Actual temperatures within a closed crucible are believed to be at least 50°C higher than the temperature read at this temperature range.

Except for the foils, all chemicals were used as received. Foils were placed in acid cleaning solutions just prior to use in order to remove surface oxides. They were immediately rinsed with distilled water and subsequently with alcohol (methanol or ethanol) and air dried. The acid cleaning solution for zirconium was made from the volume percents of the following - 10% HF, 45% HNO<sub>3</sub>, 45% H<sub>2</sub>O. The titanium cleaning solution was made from 60% by volume of H<sub>2</sub>O<sub>2</sub> (30%). 10% HF, 30% H<sub>2</sub>O; for niobium the solution contained 50 volume % HF, and 50% HNO<sub>3</sub>. Nickel was

Chemical	Source	Purity	Comments
Zr	Alfa	99.9%	0.25 mm foil
Zr	Alfa	99+%	powder
Zr	Johnson Matthey	99.9%	-20+60 mesh <sup>a</sup>
ZrO <sub>2</sub>	Johnson Matthey Puratronic	99.9975%	
Ti	Ames Laboratory		foil
Ti <sub>2</sub> O <sub>3</sub>	Johnson Matthey	99+%	
Ni	Inco	99.99%	foil <sup>b</sup>
Ni	Fisher Scientific	purified	powder
NiO	Johnson Matthey Puratronic	99.998%	
Nb	Alfa	99.8%	-325 mesh
Та	Johnson Matthey	99.98%	-60 mesh
Мо	Alfa	99.9+%	-200 mesh
W	Alfa	99.98%	-100 mesh
Cu	J.T. Baker Chemical Co.	99.98%	ribbons
Со	Alfa	99.5%	pieces
Si	Johnson Matthey	99.999%	zone refined
S	Fisher Scientific		lab grade

 Table 2.1 Chemicals used in synthesis of new materials

<sup>a</sup> This powder contained 10 atomic % Ti, according to quantitative analysis by XPS.
 <sup>b</sup> Nickel received from Inco was arc-melted under argon and rolled into a foil. Elemental analysis was performed after this treatment.

cleaned in concentrated HNO<sub>3</sub>. The materials used are listed in the following table, Table 2.1.

#### Characterization

Sample characterization and phase identification was routinely performed by X-ray diffraction techniques. X-ray powder diffraction was used to identify phases present in a sample. Powder patterns were recorded photographically using vacuum Guinier cameras, Enraf-Nonius, Delft Model FR552. The cameras are equipped with quartz monochromators and adjusted to select diffraction from CuK $\alpha$ 1 radiation ( $\lambda$ =1.54056 Å). With the X-ray generator power set at 20 mA and 45 kV, exposure time was typically two hours for powder samples. Samples were mounted on clear adhesive tape and placed on a rotating holder to eliminate effects of preferred orientation. The films were interpreted by measurement of line positions relative to an internal silicon standard (NIST, a=5.43088 Å). These measurements were done automatically on a KEJ Instruments Line Scanner LS-20.

Single crystals were examined by oscillation and Weissenberg photographs on a Charles Supper Company Weissenberg Camera 9000ST. A nickel filter reduced CuK $\beta$  radiation. Photographic techniques are useful for determining lattice parameters and possible space groups.

A Rigaku AFC6R diffractometer, with a rotating anode, was used to collect single crystal diffraction data. This diffractometer was set up to run with MoK $\alpha$  radiation ( $\lambda$ = 0.71069 Å) at 50 kV and 140 mA. The high intensity of the X-ray beam obtained with this diffractometer made it possible to collect enough weak intensity peaks to solve the structures from very small crystals.

Qualitative elemental analysis was performed by electron spectroscopy for chemical analysis (ESCA) on a Perkin Elmer 5500 multitechnique system, and by energy dispersive spectroscopy with X-rays (EDS) on a Cambridge S-200 scanning tunneling microscope fitted with a Northern Tracor Micro Z-II X-ray detector. Quantitative analysis was done by EDS on polished samples on a JEOL

JSM-840 electron microscope with KEVEX EDX system.

Magnetic measurements and tests for superconductivity were done on a Quantum Design SQUID magnetometer.

#### Calculations

Many of the calculations are performed routinely and quickly on the computer. A list of the programs used is presented in Table 2.2. A brief description of the programs follows. All the calculations were done on a VAX system, except the extended Hückel band calculations, which were carried out on the Iowa State University Project Vincent system.

The first analysis of a sample is often a powder X-ray diffraction experiment. Powder patterns are very useful in identifying the phases present in a sample. The films are scanned automatically in the Line Scanner LS-20. The positions and intensities of the lines are converted to d-spacings,  $2\theta$  values, and relative intensities by the program SCANPI. The d-spacings of the observed pattern can be compared to the values corresponding to known phases, or patterns calculated for new phases, as calculated by the program PWDR. Visual comparison of calculated powder patterns and observed powder patterns is possible by plotting the calculated patterns with the PLOT program. If the phase is positively identified, the *hkl* indices can be assigned to the appropriate lines and the LATT program will do a least squares refinement of the lattice parameters based on the observed d-spacings, or  $2\theta$  values, and the assigned *hkl* values. The lattice parameters of the powdered samples obtained from this calculation are those used in the reports of structural information.

The Rigaku AFC6R X-ray single crystal diffractometer is fully automated for data collection. While several options exist in the data collection procedure, in a successful structural determination the diffractometer will search for several diffraction peaks, and index them. The cell is reduced to

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a standard cell by the Delauney subroutine. The Laue symmetry is checked before intensity data are actually collected. Data collection often extends to 50-60° in 20. Following the data collection, the lattice parameters are refined based on the position of several high-angle reflections (although parameters from powder samples are reported). Finally, a psi scan is collected for absorption correction purposes. The data are processed and refined by full matrix least squares refinement using the accompanying TEXSAN package. The SHELXS direct methods program is used to obtain a starting model for the structure solution. The graphic generation of crystal structures is done with the ORTEP program.

Energy band calculations based on the extended Hückel method were performed on the Project Vincent workstation. The calculations performed gave total energies, Fermi energies, orbital populations and overlap populations. Results could be plotted as DOS curves and COOP curves. Starting parameters for  $H_{ii}$  values were obtained by using a charge iteration program.

Program	Calculations performed	Reference
Charge iteration	Charge iteration	49,50
Extended Hückel	Energy band calculations	51-54
LATT	Least squares refinement of lattice parameters	55
PLOT	Plot calculated powder patterns	56
PWDR	Calculate powder patterns	57
ORTEP	Graphical display of crystal structures	- 58
SCANPI	Calculate d-spacings in observed powder patterns	59-61
SHELXS	Direct methods structural solution for X-ray diffraction data	62
TEXSAN	X-ray single crystal structural least squares refinement	63

Table 2.2 Computer programs used in this research

# 3. SINGLE CRYSTAL X-RAY STUDY OF Zr<sub>3</sub>NiO

#### Introduction

A good starting place for the study of interstitially stabilized phases in the zirconium-nickel system is with the only previously reported Zr/Ni/O ternary phase, Zr<sub>3</sub>NiO. This compound crystallizes in the filled Re<sub>3</sub>B type structure. It was first identified in a study of the zirconium-rich corner of both the Zr/Co/O and Zr/Ni/O ternary systems at 950°C [39]. The structure for this phase was not known until a single crystal solution was published for Zr<sub>3</sub>Co [64]. Subsequently, the phases Zr<sub>3</sub>MO<sub>x</sub> (M = Fe, Co, Ni) were examined by powder diffraction data to determine the range and extent of oxygen occupancy, with related changes in lattice parameters [65]. The iron compound is reported to occur as a binary intermetallic, with no oxygen solubility (x = 0). The cobalt compound is found to exhibit a full range of oxygen occupancy ( $0 \le x \le 1$ ), forming as a binary and with full filling of octahedral sites by oxygen. The nickel compound exists only as an oxide, and does not occur as a binary phase ( $0.2 \le x \le 1.0$ ). The single crystal X-ray study confirms the previously reported results [66].

#### **Experimental Details**

A crystal for X-ray study was selected from a sample which had undergone a number of experimental treatments. Initially, zirconium, nickel and sulfur in the molar ratios 6:4:5 were heated in an evacuated silica tube at temperatures up to 690°C. The resulting mixture was arc melted. Additional zirconium and nickel were added to the sample to bring the final metal ratio to n(Zr):n(Ni)=3:1. The sample was repeatedly crushed, pelletized, and inductively heated to temperatures of 1050-1230°C for 12-18 hours. The sample was soaked in concentrated HCl for a week to remove a binary sulfide phase,  $Zr_3S_2$ , and subsequently heated to 1130°C for 5 days. The

crystal studied here was picked from this final sample, although the oxide phase, as identified by X-ray diffraction films of the powder, was present before the sample was placed in the acid.

Intensity data for this crystal were collected using a Rigaku AFC6R single crystal diffractometer and monochromated MoK $\alpha$  radiation, employing the  $\omega$ -2 $\theta$  scan technique up to 55°(2 $\theta$ ). From a total of 422 reflections ( $\pm h,k,l$ ), 162 independent reflections with  $F_0^2 > 3\sigma(F_0^2)$  were obtained and used for structure analysis. The observed intensities were corrected for Lorentz polarization and absorption effects with the maximum to minimum transmission factor ratio of 1 to 0.768. No significant decay was observed during the data collection. The crystal data are tabulated in Table 3.1.

#### **Results and Discussion**

The atomic coordinates and thermal parameters for  $Zr_3NiO$  are reported in Table 3.2, and Table 3.3, respectively. This phase has been shown to exist with variable oxygen content. The fractional oxygen occupancy ranges from 0.2 to 1.0, and the variation of the lattice parameters as a function of oxygen occupancy has been measured [65]. Full oxygen occupancy in this crystal was indicated by agreement in lattice parameters (a = 3.33 Å, b = 10.99 Å, c = 8.77 Å [65], cf Table 3.1) as well as the single crystal refinement.

The structure may be viewed as being built up from two polyhedral units - trigonal prisms of zirconium centered by nickel atoms, and octahedra of zirconium centered by oxygen atoms (Figure 3.1). The trigonal prisms share triangular faces, forming chains in the *a* direction. Adjacent chains are offset from each other by x=1/2. Oxygen atoms occupy the interstitial octahedral site formed by the zirconium atoms from adjacent chains. The octahedra form a zig-zag chain sharing corners in the *c* direction, and they share edges with adjacent octahedra in the *a* direction.

The interatomic distances less than 3.5 Å are listed in Table 3.4. The zirconium-zirconium

Table 3.1 Crystal data for Zr<sub>3</sub>NiO

Formula	Zr <sub>3</sub> NiO		
Space Group	Cmcm(#64)		
a (Å)	3.353(1)		
b (Å)	11.013(4)		
c (Å)	8.755(7)		
V (Å <sup>3</sup> )	323.3(3)		
Z	4		
d <sub>cale</sub> , (g/cm <sup>3</sup> )	7.153		
Crystal size, (µm <sup>3</sup> )	60x30x20		
μ(ΜοΚα), (cm <sup>-1</sup> )	147.71		
Data collection instrument	Rigaku AFC6R		
Radiation (monochromated in incident beam)	ΜοΚα (λ=0.71069 Å)		
Temperature, °C	23		
No. unique data, total with $F_o^2 > 3\sigma(F_o^2)$	162		
No. parameters refined	20		
Secondary ext. coeff. $(10^{-7})$	8(1)		
R <sup>a</sup> , R <sub>w</sub> <sup>b</sup> , GOF <sup>c</sup>	0.025, 0.033, 1.149		
Largest difference peak (Å <sup>3</sup> )	+1.50		
Largest negative diff. peak (Å <sup>3</sup> )	-1.40		

<sup>a</sup> R =  $\Sigma ||F_0| - |F_c|| / \Sigma |F_0|$ 

<sup>b</sup> 
$$R_w = [\Sigma w (|F_o| - |F_c|)^2 / \Sigma w |F_o|^2]^{1/2}; w = 1/\sigma^2 |F_o|^2$$

<sup>c</sup> GOF = (
$$\Sigma$$
( |F<sub>o</sub>| - |F<sub>c</sub>|)/ $\sigma$ <sub>i</sub>) / (N<sub>obs refl</sub> - N<sub>parameters</sub>)

•

ţ

Atom	Site	x	у	Z	B <sub>eq</sub> <sup>a</sup> (Å <sup>2</sup> )
Zr1	8 <i>f</i>	0	0.3645(1)	0.5601(1)	0.65(5)
Zr2	4 <i>c</i>	0	0.9338(2)	1/4	0.69(8)
Ni	4 <i>c</i>	0	0.2460(2)	1/4	1.2(1)
0	4 <i>a</i>	0	0	0	0.9(6)

Table 3.2 Atomic parameters for Zr<sub>3</sub>NiO

<sup>a</sup>  $B_{eq} = 8\pi^2/3 \Sigma_1^3 \Sigma_1^3 U_{ij} a_i^* a_j^* \overline{a}_i^* \overline{a}_j^*$ 

Table 3.3 Anisotropic thermal parameters for Zr<sub>3</sub>NiO

Atom	U <sub>11</sub>	U <sub>22</sub>	U <sub>33</sub>	U <sub>12</sub>	U <sub>13</sub>	U <sub>23</sub>
Zrl	0.0082(7)	0.0071(7)	0.0093(7)	0	0	-0.0016(5)
Zr2	0.005(1)	0.012(1)	0.010(1)	0	0	0
Ni	0.022(2)	0.014(1)	0.010(1)	0	0	0
0	0.010(7)	0.018(7)	0.007(6)	0	0	0.006(6)



Figure 3.1 Unit cell of  $Zr_3NiO$  showing ocahedral coordination of oxygen and trigonal prismatic coordination of nickel

Zr1	- 0	2.305(1) x 2	Zr2	- 0	2.307(2) x 2
	- Ni	2.657(2) x 2		- Ni	2.662(3) x 2
	- Ni	3.012(3) x 1		- Zri	3.242(2) x 4
	- Zr1	3.165(3) x 1		- Zr1	3.281(2) x 4
	- Zrl	3.206(2) x 2		- Zr2	3.353(1) x 2
	- Zr2	3.242(2) x 2		- Ni	3.439(4) x 1
	- Zr2	3.281(2) x 2			
	- Zrl	3.325(4) x 1	Ni	- Zr1	2.657(2) x 4
	- Zr1	3.353(1) x 2		- Zr2	2.662(3) x 2
				- Zrl	3.012(3) x 2
0	- Zr1	2.305(1) x 4		- Ni	3.353(1) x 2
	- Zr2	2.307(2) x 2		- Zr2	3.439(1) x 1

Table 3.4 Interatomic distances less than 3.5 Å in Zr<sub>3</sub>NiO

distances between the zirconium atoms in adjacent trigonal prisms are short compared to those distances within the prism, suggesting zirconium-zirconium interactions are stronger between the trigonal prisms than within the prism. All the zirconium-zirconium distances in the trigonal prism are greater than 3.3 Å. In fact, the Zr1-Zr2 distance on the triangular face of the prism is 3.682 Å. This is significantly larger than the 3.23 Å separation in elemental zirconium and the 3.165 Å separation within the octahedra here, as well as other zirconium-zirconium separations in this oxide (Table 3.4). Although the zirconium-zirconium linkages around the prism are outlined in Figure 3.1, the important interactions within the prism are between the nickel and the zirconium atoms. This is expected on the basis of the behavior of early transition metals and late transition metals, where strong Lewis acid - base interactions are involved. The zirconium-nickel separation here is 2.66 Å. This is shorter than the zirconium-nickel distances in ZrNi (d = 2.68-2.77 Å) and Zr<sub>2</sub>Ni (d = 2.76 Å) [67].

The role of oxygen in the compounds  $Zr_3MO_x$  (M = Fe, Co, Ni) is that of an electron acceptor. In terms of so-called electron compounds, where a certain electron per atom ratio is necessary for a given phase, the binary  $Zr_3Fe$  is taken to have an ideal composition. Then in moving from iron to cobalt, and then to nickel, the electron/atom ratio increases until the phase becomes unstable with respect to neighboring intermetallic phases. When the metal atoms have more electrons the oxygen acts as an electron sink to maintain the proper electron/atom ratio in the metal framework, enabling the phase to form. In terms of energy band arguments, if the Fermi level in  $Zr_3Fe$  lies at the energy at which all bonding levels are occupied, additional electrons would fill antibonding orbitals. Oxygen, octahedrally coordinated by zirconium atoms, provides low lying orbitals for the additional electrons in the cobalt and nickel compounds.

The magnetic susceptibility of a single phase sample, prepared by arc melting and annealing at 1000°C, was measured in a field of 3 Tesla, over a temperature range of 6 - 298 K.

The sample was also checked for superconductivity, but none was detected. The lattice parameters of this sample were a = 3.3238(4)Å, b = 10.974(1)Å, and c = 8.7982(9)Å. By Boller's plot [65], this corresponds to a stoichiometry of Zr<sub>3</sub>NiO<sub>0.6</sub>. Figure 3.2 shows paramagnetic behavior for this compound. The very low apparent magnetic moment may actually be caused by a very small amount of nickel in the sample. The figure is not corrected for core diamagnetism, which would increase the molar susceptibility by 0.5 x 10<sup>-4</sup> emu/mole [111]. See also Figure 4.7.



Figure 3.2 Magnetic susceptibility of Zr<sub>3</sub>NiO<sub>0.6</sub>

#### 4. NEW OXIDES OF THE FILLED Ti2Ni TYPE STRUCTURE

#### Introduction

The study of new phases of the filled Ti<sub>2</sub>Ni type structure is but one of many potentially fruitful areas of investigation in intermetallics and in interstitially stabilized intermetallics. The chemistry of intermetallics in general is not well understood. The commercial world benefits greatly from the technologically important uses of intermetallic compounds, while scientists continue to incrementally increase their knowledge and understanding of these materials. One area of increasing interest in recent years is the role of interstitials in intermetallics. Many known structures may include undetected interstitials. Discoveries in this field are being made because the interstitials are being specifically looked for. Also, the ability to detect the presence of interstitials has increased. The precision of Guinier cameras makes measurements of lattice parameters from powder data very sensitive to changes in composition, either from changes in metal composition or from the presence of light interstitial atoms. Single crystal diffractometers can provide X-ray beam intensity sufficient to detect and refine light elements present in the intermetallic. Although over 150 compounds with this structure have been reported, only now, with the discovery of new phases and the reinvestigation of reported phases, are the structural details being investigated and clarified.

The metal-atom ordering and oxygen occupancy of four compounds of the filled-Ti<sub>2</sub>Ni type structure have been determined by single crystal X-ray diffraction studies. Three additional phases have been identified and indexed from powder X-ray diffraction data. All the phases crystallize in space group Fd3m with the following compositions:  $Zr_4Ni_2O$  (a=12.1970(9) Å),  $Zr_6Ni_4Ti_2O_{0.6}$  (a=12.0299(9) Å),  $Nb_6Ni_6O$  (a=11.2117(5) Å), and  $Nb_6Ni_4Ta_2O_2$  (a=11.5813(3) Å). Phases identified using powder data are  $Nb_4Ni_2O$  (a=11.5933(3) Å),  $Zr_4Cu_2O$  (a=12.2659(7) Å), and  $Zr_6Co_4Ti_2O$  (a=11.8649(9) Å). A comparison of the structures and oxygen occupancies, as well as
tentative explanations, are presented based on extended Hückel calculations. The role of interstitial oxygen as an electron acceptor and its affect on metal-metal bonding will be considered.

The Ti<sub>2</sub>Ni, the filled Ti<sub>2</sub>Ni, and the related  $\eta$  carbide type structures have been known for some time [68]. Much of the earlier work revealed the variety of combinations of metals which adopt this framework to make it the most frequently found structure of binary intermetallics of stoichiometry  $A_2B$  [69]. The simplicity of the formula conceals the subtleties and complexities in the chemistry of these phases. Many of the binary intermetallics may incorporate light interstitial elements [69]. Many more phases form only in the presence of these interstitial atoms, commonly C [67,70-72], N [73,74], O [46,75,76], and even H [77], and these are the interstitially stabilized phases. Structural reports indicate the interstitial atoms, not considering H, occupy one of two possible octahedral sites, but not both. An additional feature is the possible deviation from an A<sub>2</sub>B stoichiometry to an AB stoichiometry. In some systems both ratios are observed, not as a wide solid solution, but as two distinct phases. A review of the literature and list of reported phases suggests there is no general explanation for the variability in compositions, nor is there any correlation to interstitial atom site occupancy and metal/metal ratio. Although much of the work was done a number of years ago, significant recent reports in the literature prompt further investigation of these phases [46,72,77,78]. Many reports are based on X-ray powder diffraction data, with the inherent difficulty in refining parameters for light interstitial elements. Some neutron diffraction work has been reported [72,77-79]. Single crystal work has not been previously reported for the oxides or carbides. Presumably this is because of the difficulty in forming single crystals suitable for diffraction experiments. The crystals examined here were all very small, and the successful refinements were possible because of the high X-ray beam intensity obtained from using a diffractometer with a rotating anode X-ray generator.

The filled Ti<sub>2</sub>Ni type structure crystallizes in space group Fd3m, and the unit cell contains

96 metal atoms. Adopting the notation by Newsam et. al.[72], the general formula for the oxides is written  $M_6^f M_4^q M_2^0 O_5^c O_1^a$ . The superscript letters are those of the Wyckoff symbol for the crystallographic site occupied by the superscripted atoms. The subscripts are based on the unit cell formula with Z=8. For a ternary compound  $M^f$  and  $M^e$  are different transition metals.  $M^d$  may either be the same as  $M^f$  or  $M^e$ , depending on the system being considered. The transition metal  $M^f$  is always to the left of the  $M^e$  metal atom on the periodic table. The  $M^f$  atoms form an octahedral network. The  $M^e$  atoms have a tetrahedral arrangement. The  $M^d$  atoms cap the faces of the tetrahedra formed by the  $M^e$  atoms. When the *f* and *d* sites are occupied by the same metal the metal:metal ratio is 8:4, or 2:1. When the *e* and *d* sites are occupied by the same metal the metal:metal ratio is 6:6, or 1:1. There is no mixing reported on the  $M^d$  site, and this explains the two ratios reported as distinct phases, and not as a single phase with a large range of homogeneity. The assumption is made that the interstitial oxygen atoms occupy only one of the two possible sites. They occupy either the 16*c* site, in which they fill distorted octahedra, or the 8*a* site, in which they fill regular octahedra. Thus for a given ternary system the four possible compositions reported are  $M_8M_4'O$ ,  $M_8M_4'O_2$ ,  $M_6M_6'O_6$ , and  $M_6M_6'O_2$ . Examples of each have been reported.

The  $Ti_2Ni$  structure contains ninety-six metal atoms in the unit cell. When interstitial atoms are present there are up to 104 or 112 atoms in the unit cell. It is hard to visualize or depict a cell this size. It is easiest to consider the building blocks in the unit cell and see how they order. Consider first a large cubic cell divided into two alternating subunits, as in Figure 4.1. Each subunit is one - eighth of the total cell, and the alternating pattern extends in all three directions in space. Figure 4.2 is a projection of one layer of the unit cell depicted in Figure 4.1, and contains four subunits. The subunits in the lower left and upper right are centered by an octahedron. The lower right and upper left subunits are centered by a tetrahedron. The octahedron - centered subunits and



Figure 4.1 A large cubic cell divided into two alternating subunits



Figure 4.2 Projection of one half the unit cell, in the direction of projection axis, of  $Zr_4Ni_2O$ .

tetrahedron - centered subunits pack in an alternating pattern in all three dimension. Each subunit is displayed individually in Figure 4.3. Figure 4.3 (a) shows the subunit centered by an octahedron in which the central octahedron is surrounded by four more octahedra arranged tetrahedrally at the corners of the subunit. It is also surrounded by four tetrahedra, arranged tetrahedrally at the other four corners of the subunit. Figure 4.3 (b) is centered by a tetrahedron, and is similarly surrounded by four octahedra and four tetrahedra. Note that these two subunits adjoin one another, so that the octahedron at the lower right of Figure 4.3 (a) is the same octahedron at the lower left of Figure 4.3 (b), and so on for the other polyhedra on the shared face.

The diagram for Figure 4.3 is made for the compound  $Zr_4Ni_2O$ , where the M<sup>d</sup> atom is the same metal as the  $M^{f}$  atom, which is zirconium in this case. The  $M^{d}$  zirconium atom is seen capping the faces of the central tetrahedron in Figure 4.3 (b). The interstitial oxygen in the 16c site is seen in Figure 4.3 (a), capping four faces of the central octahedron. This atom is actually six coordinated, in a distorted octahedral arrangement, where opposite faces of the distorted octahedron share faces with the regular octahedra outlined. Thus, rather than looking at isolated polyhedra, consider a network built up of these face - sharing octahedra. The subunit in Figure 4.3 (a) viewed as a section of such a network is drawn in Figure 4.4. The central octahedron shares four faces with four other octahedra. Each of these four octahedra, shown shaded and centered by oxygen, share just two opposite faces. The network, then, consists of face - sharing octahedra which alternately share two and four faces. The octahedra shown are alternately centered by oxygen and empty. The face - sharing octahedra form rings made up of 12 octahedra. The void spaces within and between these rings are filled by an interpenetrating network consisting of the tetrahedra and the capping atoms, forming stella quadrangulea. This network is depicted in Figure 4.5. The structure has been described in the literature by both schemes outlined here; as made up of alternating subunits, and as two interpenetrating networks. Additional comments about the structure



# Figure 4.3

View of individual subunits making up the unit cell of Zr<sub>4</sub>Ni<sub>2</sub>O (a) subunit centered by zirconium octahedron (b) subunit centered by nickel tetrahedron



Figure 4.4 Network of face-sharing zirconium octahedra in  $Zr_4Ni_2O$ . Shaded octahedra are centered by oxygen, unshaded octahedra are empty.



Figure 4.5 Network of stella quadrangulae in  $Zr_4Nl_2O$ . Nickel tetrahedra are shaded.

will be made later, at which point structural features are considered in terms of chemical interactions.

### **Experimental Details**

All chemicals were used as they were received from the supplier, except as noted in the experimental section earlier. Samples were prepared by two general techniques. The first technique consisted of arc melting the metals and the oxide of either zirconium or nickel. The samples were then annealed under vacuum in an induction furnace. This technique often resulted in a mixture of phases.  $ZrO_2$  was always present as a minor phase. Other minor phases present in various samples were  $Zr_3NiO$  and the cubic Laves phase. Apparently, the Laves phase has a low melting point (less than 1000°C) and the presence of this phase masks the refractory nature of this family of compounds. Samples free of this phase remained solid when annealed at 1250-1275°C. Samples containing niobium all had NbO as a minor phase, and some also had Nb<sub>7</sub>Ni<sub>6</sub> present. The desired phase was present upon annealing as low as 1000°C, but most samples were annealed at 1250°C.

A second method was used successfully for the preparation of a nearly single phase sample of  $Zr_4Ni_2O$ . Only the two strongest lines of  $ZrO_2$  were barely visible in the powder X-ray diffraction pattern of this phase. A sample of Zr and Ni was arc-melted, as before, then ground to small pieces. The metal and an appropriate amount of oxidizing agent, NaClO<sub>4</sub>, were sealed in an evacuated fused silica tube. Upon heating to 600°C for 4 days in a tube furnace the perchlorate decomposed, and crystals of NaCl formed at the cool end of the tube. The resulting oxide was crushed to a fine powder and pressed into a pellet before annealing as before.

Single crystal X-ray diffraction data collection was done on a Rigaku AFC6R diffractometer, with MoK $\alpha$  radiation ( $\lambda$ =0.71069 Å). All crystals were refined in space group Fd3m. Details of crystal data are listed in Table 4.1.

A Quantum Design SQUID magnetometer was used to check for superconductivity and to measure magnetic behavior at a field of 3T over the temperature range of 6 - 298 K.

A JEOL JSM-840 electron microscope was used to examine the zirconium nickel oxides.

#### Results

Interest in the Ti<sub>2</sub>Ni type structures initially arose from a study of the interstitially stabilized intermetallic phases that form in the Zr-Ni system [66,80,81]. Two curious results deserved attention. First, previous work on the Zr-Ni-O phase diagram in an intentional search for this phase indicated that it does not exist in equilibrium at 950°C [39]. It does exist, however, at 1275°C, the annealing temperature used in these experiments. This is thus an example of a high temperature solid phase which decomposes at lower temperature, in this case probably to Zr<sub>3</sub>NiO and Ni. Second, there was a noticeable shift in lattice parameters for this phase in several of the samples, as observed in the films of the powder diffraction patterns taken on a Guinier camera. A single crystal was chosen from both a sample with the larger lattice parameter, and a sample with the smaller lattice parameter. The results for the data refinement of the larger cell correspond to the data reported for  $Zr_4Ni_2O$  in Table 4.2. The preliminary solution for the smaller cell was also based on a Zr/Ni/O ternary system, and required Ni vacancies on the 16d site for a suitable refinement, giving a stoichiometry of  $Zr_6Ni_{6-x}O$ . This solution was corrected when elemental analysis revealed the presence of titanium, which could be detected in samples prepared with a zirconium starting material which unexpectedly contained significant amounts of titanium. Placing Ti in the 16d site in the structure solution improved the refinement significantly, and the final refinement showed full occupancy on all the metal sites. The results for  $Zr_6Ni_4Ti_2O_{0.6}$  are also in Table 4.2. Efforts to synthesize a compound of stoichiometry  $Zr_6Ni_6O$ , without titanium, were unsuccessful.

39

		2		
Formula	Zr <sub>4</sub> Ni <sub>2</sub> O	$\mathrm{Zr_6Ni_4Ti_2O_{0.6}}$	Nb <sub>6</sub> Ni <sub>6</sub> O	Nb <sub>6</sub> Ni <sub>4</sub> Ta <sub>2</sub> O <sub>2</sub>
a Å	12.1970(9)	12.0299(9)	11.2117(5)	11.5813(3)
VÅ <sup>3</sup>	1814.5(4)	1740.9(4)	1409.3(2)	1553.4(1)
Z	16	8	8	8
d <sub>calc</sub> , g/cm <sup>3</sup>	7.295	6.747	8.742	10.390
Crystal size, µm <sup>3</sup>	40x50x70	50x50x100	40x40x40	30x40x50
μ(MoKα), cm <sup>-1</sup>	167	169	246	494
Data collection range, 20	0-60	0-55	0-55	0-60
No. refl. measured	768	579	482	1253
No. unique data, total with $F_o^2 > 3\sigma(F_o^2)$	112	87	79	101
No. parameters refined	13	15	11	15
Trans. factors, max./min.	1.116	1.168	1.146	1.179
R <sup>a</sup>	0.020	0.029	0.017	0.022
R <sub>w</sub> <sup>b</sup>	0.024	0.031	0.023	0.029
GOF <sup>c</sup>	1.019	0.995	0.980	1.026
Largest peak, e/Å <sup>3</sup>	1.59	1.20	0.88	1.54
Largest negative peak, e/Å <sup>3</sup>	-1.17	-1.31	-1.04	-3.19

Table 4.1 Single crystal data of new filled - Ti<sub>2</sub>Ni type phases

<sup>a</sup> R =  $\Sigma ||F_0| - |F_c|| / \Sigma |F_0|$ 

<sup>b</sup> 
$$R_w = [\Sigma w (|F_o| - |F_c|)^2 / \Sigma w |F_o|^2]^{1/2}; w = 1/\sigma^2 (|F_o|)^2$$

<sup>c</sup> GOF = ( $\Sigma(|F_o|-|F_c|)/\sigma_i$ )/ (N<sub>obs refl</sub>- N<sub>parameters</sub>)

				the second s	
Atom	Site	x	у	Z	$B_{eq}(Å^2)^a$
			Zr <sub>4</sub> Ni <sub>2</sub> O		
Zr1	48 <i>f</i>	0.18517(8)	0.0	0.0	0.51(1)
Ni	32 <i>e</i>	0.8396(1)	0.8396	0.8396	1.2716(5)
Zr2	16 <i>d</i>	0.625	0.625	0.625	1.5990(5)
0	16 <i>c</i>	0.125	0.125	0.125	0.562(2)
		2	Zr <sub>6</sub> Ni <sub>4</sub> Ti <sub>2</sub> O <sub>0.6</sub>		
Zr	48f	0.1901(1)	0.0	0.0	0.73(4)
Ni	32 <i>e</i>	0.8326(2)	0.8326	0.8326	1.1795(7)
Ti	16 <i>d</i>	0.625	0.625	0.625	1.430(1)
O <sup>b</sup>	16c	0.125	0.125	0.125	1.17(3)
O <sup>b</sup>	8 <i>a</i>	0.0	0.0	0.0	0.98(3)
			Nb <sub>6</sub> Ni <sub>6</sub> O		
Nb	48f	0.1996(1)	0.0	0.0	0.47(2)
Ni1	32 <i>e</i>	0.8317(1)	0.8317	0.8317	0.3289(4)
Ni2	16d	0.625	0.625	0.625	0.4602(6)
0	8 <i>a</i>	0.0	0.0	0.0	0.497(4)
		1	Nb <sub>6</sub> Ni <sub>4</sub> Ta <sub>2</sub> O <sub>2</sub>		
Nb <sup>c</sup>	48f	0.1867(1)	0.0	0.0	0.48(4)
Ni	32 <i>e</i>	0.8311(1)	0.8311	0.8311	0.422(1)
Ta <sup>d</sup>	16d	0.625	0.625	0.625	0.3491(6)
0	16 <i>c</i>	0.125	0.125	0.125	1.154(5)
		Idealize	ed Metal Positi	ions <sup>e</sup>	
M1	48 <i>f</i>	0.1875	0.0	0.0	
M2	32 <i>e</i>	0.8250	0.8250	0.8250	

Table 4.2 Final atomic parameters from single crystal refinement

a

 $B_{eq} = 8\pi^2/3 \sum_{i}^{3} \sum_{i}^{3} U_{ij} a_{i}^{*} a_{j}^{*} \overline{a}_{i}^{*} \overline{a}_{j}^{*}$ Refinement of the oxygen occupancy gave results of the 16*c* site being 18(6)% occupied and b the 8a site 24(6)% occupied.

c Refined with mixed Nb/Ta occupancy; Nb 82(2)%, Ta 18(2)%.

d Refined with mixed Ta/Nb occupancy; Ta 61(3)%, Nb 39(3)%.

e [84] A systematic check for a solid solution between  $Zr_4Ni_2O$  and  $Ti_4Ni_2O$  was not performed but for low concentrations of titanium, the titanium preferentially substitutes on the 16*d* site. Furthermore, the oxygen partially occupies both interstitial sites in the sample containing titanium, with total oxygen occupancy given by the formula  $Zr_6Ni_4Ti_2O_{0.6}$ . The refinement was carried out considering the possible solutions:  $Zr_6Ni_4Ti_2$  (no oxygen),  $Zr_6Ni_4Ti_2O_{1.x}$  (variable oxygen occupancy on the 8*a* site only),  $Zr_6Ni_4Ti_2O_{2.x}$  (variable oxygen occupancy on the 16*c* site only), and  $Zr_6Ni_4Ti_2O_{3.x}$  (variable oxygen occupancy on both the 8*a* and the 16*c* sites). By careful comparison of each of the refinement solutions, according to Hamilton's test [82], the solution with both sites partially occupied is correct with a 95% level of confidence. This result raises the question of whether a small amount of oxygen is required for the formation of the phase with a small addition of Ti (these samples were all made with intentional inclusion of oxygen). The binary intermetallic  $Ti_2Ni$  can reportedly accommodate oxygen to completely occupy of the 16*c* site, forming  $Ti_4Ni_2O$  [79]. The corresponding zirconium compound reported here has complete occupation of the 16*c* site.

Conflicting reports exist for the  $Zr_4Co_2O$  phase. Nevitt and Downey [39] did not find this phase in determining the 950°C isothermal section of this ternary system. Hollock and Thümmler [74] include  $Zr_4Co_2O$  (a=12.18 Å) in a list of phases observed. Attempts to synthesize this phase at 1100°C were unsuccessful. However, it was observed that this phase formed in samples prepared with the titanium-contaminated zirconium. By analogy with the substitution of Ti in  $Zr_4Ni_2O$ , this is formulated as  $Zr_6Co_4Ti_2O$  (a=11.8649(9) Å), with undetermined oxygen occupancy.

The Zr/Cu/O system was also investigated. The synthesis of both  $Zr_4Cu_2O$  and  $Zr_6Cu_6O$  was attempted. With the Zr:Cu starting ratio of 2:1, the powder pattern indicated the presence of the desired phase as well as binary  $Zr_2Cu$  as a minor phase. When the starting Zr:Cu ratio was 1:1 the products were the cubic phase and the binary  $Zr_3Cu_8$ . The lattice parameters of the Ti<sub>2</sub>Ni type

phase differed only slightly in all of the samples made. For the nearly single phase sample made with a 2:1 starting metal ratio, a=12.2659(7) Å. The smallest cell edge measured for the cubic phase with the 1:1 starting ratio was a=12.2615(6) Å. This leads to the conclusion there is only the one phase,  $Zr_4Cu_2O$ , with perhaps a slightly varying oxygen content accounting for the differences in observed cell lengths. Characterization of these phases was done by film data from X-ray powder diffraction experiments. The oxygen is assumed to occupy the 16*c* site. A significant shortening in the unit cell is observed when Ti is added to form  $Zr_6Cu_4Ti_2O$  (a=12.16(2)Å).

The existence of the two distinct phases in the Nb/Ni/O system reported previously is confirmed [74]. Single crystal X-ray diffraction data for Nb<sub>6</sub>Ni<sub>6</sub>O (a=11.2117(5) Å) was used to determine oxygen occupancy in this phase, which had been reported as Nb<sub>3</sub>Ni<sub>3</sub>O (a=11.20 Å). Nb<sub>4</sub>Ni<sub>2</sub>O has lattice parameter a=11.5933(3) Å (previously reported as 11.58 Å). Comparison of oxygen occupancies in the Nb/Ni/O samples is incomplete because single crystals of Nb<sub>4</sub>Ni<sub>2</sub>O have not been found. The difference in lattice parameters clearly indicates the existence of two distinct phases. This contrasts with the Nb/Ni/C system for which only the Nb<sub>4</sub>Ni<sub>2</sub>C phase appears in the 1100°C isothermal section of the termary phase diagram [83]. Samples of the oxides have been prepared which contain both phases in an equilibrium mixture. The existence of two distinct phases shows the 16*d* site is occupied either entirely by niobium or by nickel, but not by both in a solid solution on this metal site.

 $Ta_4Ni_2O$  is reported by Holleck & Thümmler [74], but Kotyk & Stadelmaier [73] find this phase only exists with nitrogen present, as either  $Ta_4Ni_2N$  or the mixed  $Ta_4Ni_2(O,N)$ , but not as the pure oxide. Efforts to synthesize both  $Ta_4Ni_2O$  and  $Ta_6Ni_6O$ , annealing at temperatures between 1430-1550°C, resulted in mixtures of binary phases. However, noting the effect of titanium in the zirconium compounds, the synthesis of mixed Ta/Nb compounds was attempted. Both of the starting compositions  $Ta_6Ni_4Nb_2O_2$  and  $Nb_6Ni_4Ta_2O_2$  were tried. Only the latter formed the cubic phase, at 1550°C, with  $(Ta,Nb)_7Ni_6$  present as a minor phase. A single crystal was selected for study by X-ray diffraction. A psi - scan suitable for absorption correction in the refinement process was not collected. As an empirical absorption correction (DIFABS) did not improve the refinement, no correction was applied in the final refinement. The Nb and Ta occupancies were allowed to mix in the refinement, resulting in a final stoichiometry of  $(Nb_{0.82}Ta_{0.18})_6Ni_4(Ta_{0.61}Nb_{0.39})_2O_2$ , or  $Nb_{5.7}Ni_4Ta_{2.3}O_2$ .

Crystal data for all the single crystal refinements are listed in Table 4.1. Positional and thermal parameters for the four single crystal refinements are listed in Table 4.2. Table 4.3 contains anisotropic thermal parameters. Interatomic distances are shown in Table 4.4. Table 4.5 summarizes all of the phases identified in this study and corresponding lattice parameters.

 $Zr_4Ni_2O$ , Nb<sub>6</sub>Ni<sub>4</sub>Ta<sub>2</sub>O<sub>2</sub>, Nb<sub>4</sub>Ni<sub>2</sub>O, and Nb<sub>6</sub>Ni<sub>6</sub>O were checked for superconductivity down to 6 K. None was detected. Magnetic measurements of the  $Zr_4Ni_2O$  and Nb<sub>6</sub>Ni<sub>4</sub>Ta<sub>2</sub>O<sub>2</sub> phases from 6 - 297 K at a field of 3 Tesla show they are both paramagnetic (Figure 4.6). Figure 4.6 (a) shows a peculiar rise in susceptibility with temperature for  $Zr_4Ni_2O$ . Note the expanded scale on this figure. The sample contained an estimated 5% impurity phase of  $ZrO_2$ . A correction for the diamagnetism of the impurity phase and the core diamagnetism increases the molar susceptibility by  $0.7x10^{-4}$  emu/mole from that shown in the figure. The source of the glitch at 225 K in Figure 4.6 (b) for Nb<sub>6</sub>Ni<sub>4</sub>Ta<sub>2</sub>O<sub>2</sub> is unknown. When the temperature was cycled the glitch shifted to 240K, but did not disappear. This sample contained approximately 10% of an impurity phase of the Nb<sub>7</sub>Ni<sub>6</sub> type. No magnetic measurements of Nb<sub>7</sub>Ni<sub>6</sub> or Ta<sub>7</sub>Ni<sub>6</sub> have been reported, and as it is possible this phase is paramagnetic also, no correction is made to the measured values. Figure 4.7 contains the results of the magnetic measurements on all the samples measured on the same scale.

Atom	U <sub>11</sub>	U <sub>22</sub>	U <sub>12</sub>	U <sub>23</sub>
		Zr <sub>4</sub> Ni <sub>2</sub> O		
Zr1	0.0066(3)	0.0064(3)	0	0.0010(4)
Ni	0.02025(5)	0.02025	0.002(1)	0.002
Zr2	0.01611(5)	0.01611	0.009(1)	0.009
0	0.00712(3)	0.00712	0.0000(1)	0.0
		Zr <sub>6</sub> Ni <sub>4</sub> Ti <sub>2</sub> O <sub>0.6</sub>		
Zr	0.009(1)	0.0094(6)	0	0.0000(8)
Ni	0.01494(1)	0.01494	0.0003(8)	0.0003
Ti	0.01812(2)	0.01812	0.008(2)	0.008
0	0.0148(4)	0.0148	-0.01(3)	-0.01
O <sup>b</sup>	0.0125(3)			
		Nb <sub>6</sub> Ni <sub>6</sub> O		
Nb	0.0073(5)	0.0053(4)	0	0.0005(4)
Ni1	0.004167(5)	0.004167	0.0006(4)	0.0006
Ni2	0.005830(7)	0.005830	-0.0010(6)	0.0010
O <sup>b</sup>	0.00630(5)			
		Nb <sub>6</sub> Ni <sub>4</sub> Ta <sub>2</sub> O		
Nb	0.0070(8)	0.0055(6)	0	-0.0002(5)
Ni	0.00534(1)	0.00534	0.0001(6)	0.0001
Та	0.004421(7)	0.004421	-0.0007(3)	-0.0007
0	0.01461(6)	0.01461	-0.005(6)	-0.005

Table 4.3 Anisotropic thermal parameters<sup>a</sup> for new phases of filled  $Ti_2Ni$  type

<sup>a</sup> Symmetry requirements for atoms listed first are  $U_{22} = U_{33}$ , and  $U_{12} = U_{13} = 0$ . For all other atoms,  $U_{11} = U_{22} = U_{33}$ , and  $U_{12} = U_{13} = U_{23}$ .  $U_{33}$  and  $U_{13}$  values are not explicitly included on table.

<sup>b</sup> Isotropic refinement

		Zr <sub>4</sub> Ni <sub>2</sub> O	Zr <sub>6</sub> Ni <sub>4</sub> Ti <sub>2</sub> O	Nb <sub>6</sub> Ni <sub>6</sub> O	Nb <sub>6</sub> Ni <sub>4</sub> Ta <sub>2</sub> O <sub>2</sub>
M1 <sup>a</sup> -	O1 x1		2.287(2)	2.238(1)	
	O2 x2	2.2776(7)	2.266(2)		2.162(1)
	Ni x2	2.7832(9)	2.861(2)	2.691(1)	2.774(1)
	Ni x2	3.152(1)	3.075(2)	2.773(1)	2.9912(6)
	M2 x2	3.164(1)	3.078(1)	2.7920(8)	2.999(1)
	M1 x4	3.194(1)	3.175(1)	2.915(1)	3.058(1)
	M1 x4	3.248(1)	3.234(1)	3.165(1)	3.075(1)
Ni -	M2 x3	2.688(1)	2.600(1)	2.4170(6)	2.4928(6)
	Ni x3	3.0910(9)	2.811(5)	2.591(1)	2.657(1)
	M1 x3	2.7832(9)	2.861(2)	2.691(1)	2.774(1)
	M1 x3	3.152(1)	3.075(2)	2.773(1)	2.999(1)
	O1 x1		3.488(3)	3.268(2)	
	O2 x3	3.534(1)	3.590(2)		3.388(1)
M2 <sup>b</sup> -	Ni x6	2.6878(8)	2.600(1)	2.4170(6)	2.4928(6)
	M1 x6	3.164(1)	3.078(1)	2.7920(8)	2.9912(6)
O1 <sup>c</sup>	M1 x6		2.287(2)	2.238(1)	
	Ni x4		3.488(3)	3.268(2)	
O2 <sup>d</sup>	M1 x6	2.2776(7)	2.266(2)		2.162(1)
	Ni xб	3.534(1)	3.590(2)		3.388(1)

Table 4.4 Interatomic distances in new filled-Ti $_2$ Ni type phases

 $^{a}M1 = Zr \text{ or } Nb \text{ in } 48f$ 

 $^{b}M2 = Zr$ , Ti, Ni, or Ta in 16d

 $^{c}O1 = O \text{ in } 8a$ 

 $^{d}O2 = O$  in 16c

Composition	a (Å)	
Zr <sub>4</sub> Cu <sub>2</sub> O	12.2659(7)	<u></u>
Zr <sub>4</sub> Ni <sub>2</sub> O	12.1970(9)	
$\mathrm{Zr}_{6}\mathrm{Ni}_{4}\mathrm{Ti}_{2}\mathrm{O}_{0.6}$	12.0299(9)	
Zr <sub>6</sub> Co <sub>4</sub> Ti <sub>2</sub> O	11.8649(9)	
Nb <sub>4</sub> Ni <sub>2</sub> O	11.5933(3)	
Nb <sub>6</sub> Ni <sub>4</sub> Ta <sub>2</sub> O <sub>2</sub>	11.5813(3)	
Nb <sub>6</sub> Ni <sub>6</sub> O	11.2117(5)	

Table 4.5 Lattice Parameters for all new filled-Ti $_2$ Ni type phases found



Figure 4.6 (a) Magnetic susceptibility of  $Zr_4Ni_2O$ . (b) Magnetic susceptibility of  $Nb_6Ni_4Ta_2O_2$ .



$$Nb_6Ni_4Ta_2O_2$$

$$- \Box - Zr_6 Ni_6 TiSiO_{1.8}$$

$$\rightarrow$$
 Zr<sub>3</sub>NiO<sub>0.6</sub>

Figure 4.7 Summary of magnetic properties of phases studied in this research.

## **Band Calculations**

Band calculations were done in an effort to explain the role of oxygen in the  $Zr_4Ni_2O$  phase, and determine if calculations could predict a preferred ordering of oxygen. Calculations were performed also on the compound Nb<sub>6</sub>Ni<sub>6</sub>O in an attempt to correlate the oxygen ordering with the metal ratios. The calculations were of the extended Hückel type using the tight binding method. The programs were described previously in the second chapter on Experimental Techniques. Density of states (DOS) diagrams and crystal orbital overlap population (COOP) curves were obtained, in addition to Fermi energies, total energies, orbital populations, and overlap populations of specific interactions. The atomic parameters used for the calculations are listed in Table 4.5. Calculations were done on the primitive cell of the large face center cubic cell. The k-points used for the calculation were chosen automatically by the program. The number of k-points used affects the accuracy of the results, and also determines the computer time required. Ten k-points were used for these calculations.

Atom	Orbital	H <sub>ii</sub> , eV	ζı <sup>a</sup>	$\zeta_2^{a}$	c <sub>1</sub> <sup>b</sup>	c <sub>2</sub> <sup>b</sup>
Zr <sup>c</sup>	4d	-8.65	3.84	1.505	0.6213	0.5798
	5s	-7.78	1.82			
	5p	-4.96	1.78			
Ni <sup>d</sup>	3d	-12.99	5.75	2.20	0.5817	0.5800
	4s	-8.86	1.925			
	4p	-4.90	1.925			
O <sup>e</sup>	2s	-32.3	2.275			
	2p	-14.8	2.275			

 Table 4.5
 Atomic parameters used for extended Hückel calculations

<sup>a</sup> Exponent in the double  $\zeta$  function for d orbitals

<sup>b</sup> Coefficients to exponential terms

<sup>c</sup> Parameters taken from [85]

<sup>d</sup> Parameters taken from[86]

<sup>e</sup> Parameters taken from [87]

The calculations carried out did not give clear answers to the questions asked. A clear preference for ordering of oxygen was not observed in Zr<sub>4</sub>Ni<sub>2</sub>O, as would be indicated by a lowering of the total energy of the system. To explain the subtle energy differences between oxygen occupying the different crystallographic sites, the possibility that the calculations might be sensitive to the starting parameters was considered. Consequently, a charge iterative procedure was performed to obtain new H<sub>ii</sub>, ionization potential, values for zirconium and nickel. These new parameters are listed in Table 4.6 and were used to repeat several of the band calculations performed previously. However, again there was no clear preference calculated for ordering of the oxygen. The charge iteration was done only for zirconium and nickel. The oxygen parameters were kept the same. The iteration was done on the binary Zr<sub>2</sub>Ni, which has the Al<sub>2</sub>Cu type structure, with the assumption the parameters of the intermetallic would be very similar to those of the oxide. That this is a fair assumption can be inferred from the fact that the initial values were obtained from calculations on ZrCl for zirconium and on Ni(CO)<sub>4</sub> for nickel. Performing the charge iteration on  $Zr_2Ni$  saved time as well, since it has a much smaller unit cell than the oxide. Eleven cycles were necessary for the parameters to converge to the values listed in the table.

Atom	Orbital	H <sub>ii</sub> , eV	
Zr <sup>a</sup>	4d	-6.72	
	5s	-7.06	
	5p	-3.68	
Ni <sup>b</sup>	3d	-8.43	
	4s	-6.76	
	4p	-3.03	

Table 4.6 Atomic parameters obtained from charge iteration on Zr<sub>2</sub>Ni

<sup>a</sup> A, B, C parameters for  $H_{ii} = Aq^2 + Bq + C$  taken from [88] <sup>b</sup> A, B, C parameters taken from [89]

General features of the DOS plots of Zr<sub>4</sub>Ni<sub>2</sub>O can be seen in Figures 4.8 and 4.9. Figure 4.8 (a) shows the DOS plot using the initial  $H_{ii}$  values listed in Table 4.5. Figure 4.8 (b) shows the same plot using the H<sub>ii</sub> values obtained from the charge iteration, listed in Table 4.6. The most obvious result of the charge iteration procedure is the shift of all the levels to higher energies, except those for oxygen, for which parameters were not changed. The narrow band below -15 eV is principally oxygen 2p in character. Figure 4.8 (a) shows a contracted band between - 14 and -12 eV, and a broad band from -12 eV and up. These bands can be assigned as being principally the nickel d band and zirconium d band, respectively. The d bands for late transition metals are more contracted than are those for early transition metals. In Figure 4.8 (b) the nickel d band is more contracted and is centered at about -9 eV, overlapping with the zirconium d band. The zirconium d band has the same general shape both with and without the charge iteration, but it is shifted to higher energies in (b). The broad, shallow Zr s and Ni s bands are in this region also. The projection of the individual atoms on the total DOS is shown in Figure 4.9 for the results from the charge iteration. Figure 4.9 (a) shows the projection of the Zr1 atoms on the total DOS. These are the zirconium atoms which make up the network of face-sharing octahedra. The oxygen atoms center an alternating set of these octahedra, and the mixing of zirconium with the oxygen p band is seen at low energy. The broad zirconium d band is seen at higher energy. Figure 4.9 (b) similarly shows the broad d band of zirconium in the icosahedral environment. Figure 4.9 (c) shows the narrow nickel d band, with nickel character extending up through the conduction band to higher energy. These general features are the same for both DOS plots in Figure 4.8. In both, the Fermi level is in the middle of the conduction band. The shifting of ionization potentials results in a shift of the calculated Fermi Energy from -9.386 eV to -7.205 eV. Another consequence of the charge iterative procedure was a change in orbital populations calculated for each atom. These changes are shown in Table 4.7, below. This shows the result of raising the ionization potentials of the metal



Total density of states plots for  $Zr_4Ni_2O$ . Fermi energy indicated by dashed line. (a) DOS before charge iteration. (b) DOS after charge iteration. Figure 4.8



Figure 4.9 Projection of individual atomic contributions on total DOS for  $Zr_4Ni_2O$ . (a) Projection of Zr1 on total DOS (b) Projection of Zr2 on total DOS (c) Projection of Ni on total DOS

atoms to nearly the same level. There is less charge transfer between zirconium and nickel, or less ionic character, indicative of metal - metal bonding and more realistic for intermetallic compounds, as for example, nickel changes from Ni<sup>-0.7</sup> when the initial parameters are used, to Ni<sup>-0.3</sup> using the parameters obtained from the charge iteration. The Zr2 becomes negatively charged. Oxygen builds up a higher charge, as these orbitals are kept at low energy even as the metal orbitals rise as a result of the charge iteration.

Atom	Initial parameters	Charge iteration parameters
Zr1	3.1	3.3
Ni	10.7	10.3
Zr2	4.0	4.3
0	7.1	7.4

Table 4.7 Calculated orbital populations

For comparison of results a consistent set of parameters is needed. The results reported here are those obtained using the parameters from the charge iteration procedure. In all of the calculations, the Zr1 atoms were placed on the "idealized" atom position [84], making all octahedral sites equal in size to avoid biasing the results and favoring a site for oxygen occupancy dependent on size factors. The nickel position was shifted to be between the observed atom position and the "idealized" atom position. The approach taken to this problem was to determine the effect the ordering of oxygen would have in the density of states and the total energy in the  $Zr_4Ni_2O$  phase. Figure 4.10 (a) shows the total density of states for the hypothetical oxygen-free  $Zr_4Ni_2$  with the  $Ti_2Ni$  type structure. One can see in Figure 4.10 (b) the effect adding oxygen has to the DOS curve. The nickel band is unaffected by the addition of oxygen, as expected, since there are no nickel oxygen interactions. Small changes in the DOS are seen at -7 and -9 eV, as zirconium metal



(a)

(b) ·

Figure 4.10 Effect on DOS of adding oxygen to the system (a) DOS plot for hypothetical  $Zr_4Ni_2$ (b) DOS plot for  $Zr_4Ni_2O$ .



Figure 4.11 Effect on DOS of oxygen occupying different crystallographic sites. (a) DOS when oxygen occupies 16c site, as observed in  $Zr_4Ni_2O$ . (b) DOS when oxygen occupies 8a site, as in hypothetical  $Zr_4Ni_2O_{1/2}$ .

becomes involved in zirconium - oxygen bond formation. Figure 4.11 compares the effect on the DOS of adding oxygen to the sixteen - fold site, as is observed by the single crystal refinement, and adding oxygen to the other possible octahedral site, an eight - fold site. Little difference is observed between the two plots. The Fermi energies and total energies for each of these calculations are shown in Table 4.8. The bottom row of Table 4.8 is the total energy gain per oxygen atom added to the system. The formation of  $Zr_4Ni_2O$  from  $Zr_4Ni_2$  decreases the total energy of the system from -1225.62 eV to -1775.43 eV, or by -549.81 eV. There are four oxygen atoms in the primitive unit cell, so the energy change per oxygen atom is one-fourth the total change, or -137.45 eV. By comparing the change per oxygen atom, the results of adding different amounts of oxygen can be compared. The table shows the two results differ by only 0.31 eV per oxygen. The calculated preferred ordering is in favor of the observed result, but it is doubtful the difference is significant within the errors of the calculations associated with the approximations of the extended Hückel method.

	Zr <sub>4</sub> Ni <sub>2</sub>	Zr <sub>4</sub> Ni <sub>2</sub> O <sub>1/2</sub>	Zr <sub>4</sub> Ni <sub>2</sub> O	
Fermi energy, E <sub>F</sub>	-7.242	-7.212	-7.205	
Total energy, E <sub>T</sub>	-1225.62	-1499.91	-1775.43	
ΔE <sub>T</sub> /oxygen		-137.14	-137.45	

Table 4.8 Fermi energy and total energy of calculated phases (eV)

The results of the single crystal refinement of  $Nb_6Ni_6O$  show the oxygen can occupy the eightfold site in the structure. Not only is the oxygen occupancy different in this compound from  $Zr_4Ni_2O$ , but the metal/metal ratio is also different. An attempt was made to determine if there was a correlation between the differences in the oxygen and metal orderings. Calculations were done on the compound  $Nb_6Ni_6O$ , using for niobium the zirconium parameters from the charge iteration.

Figure 4.12 illustrates how changing the metal framework from the hypothetical  $Nb_8Ni_4$  to the also hypothetical Nb<sub>6</sub>Ni<sub>6</sub> effects the DOS. The nickel d band is broadened slightly, as might be expected from additional nickel atoms. Figure 4.13 is the result of the calculations for the observed  $Nb_6Ni_6O$  and the hypothetical  $Nb_6Ni_6O_2$ . Table 4.9 lists the energies associated with each of these phases. Again, there is little difference observed in the DOS plots. The changes in energy per oxygen atom are such that the observed phase is again favored, but by only 0.15 eV. In addition to the uncertainty within the calculations, another caution to the interpretation of these numbers must be added. The calculations do not allow for nonstoichiometry, or partial filling of the sites. If only half of the sixteen - fold sites are occupied by oxygen, the stoichiometry is the same as for the the observed phase, Nb<sub>6</sub>Ni<sub>6</sub>O. The program does not allow random partial occupancy of any sites. Electron counts can be varied, but the sites must be either completely filled or empty. For this calculation, then, two of the four oxygen sites were filled, and the other two were empty. The total energy for this phase was -1789.01 eV, resulting in a stabilization of -136.82 eV per oxygen atom. This is only 0.04 eV difference with the calculated energy for the observed structure. If these results show anything, it may be that the important consideration is not which site is occupied, but rather the amount of oxygen the system requires for maximum stabilization.

Crystal orbital overlap population (COOP) curves were calculated for the interactions in  $Zr_4Ni_2O$ . The calculated overlap populations are tabulated in Table 4.10. Nickel - nickel overlap population was very low, about one one-thousandth, and is not included in the table. There are twenty - four symmetry related  $Zr^2$  -  $Zr^1$  interactions in the unit call. In fact, there are twenty - four symmetry related interactions for each of the combinations listed. The sum of the overlap populations of the symmetry related bonds are plotted in the COOP curves. The program would not yield the sum of all the overlap populations in one curve, so the interactions were broken down into smaller groups. Figure 4.14 (a) contains the sum of all  $Zr^2$  -  $Zr^1$  and  $Zr^2$  - Ni overlap



Figure 4.12 Effect on DOS of changing metal/metal ratio in  $Ti_2Ni$  type structure. (a) DOS for  $Nb_8Ni_4$ (b) DOS for  $Nb_6Ni_6$ 



Figure 4.13Effect on DOS of oxygen occupying different crystallographic sites.(a) DOS when oxygen occupies the 8a site, as observed in Nb<sub>6</sub>Ni<sub>6</sub>O.(b) DOS when oxygen occupies the 16c site, as in hypothetical Nb<sub>6</sub>Ni<sub>6</sub>O<sub>2</sub>.

ince 4.9 Termi energy and total energy of calculated phases (ev)					
Nb <sub>6</sub> Ni <sub>6</sub>	Nb <sub>6</sub> Ni <sub>6</sub> O	Nb <sub>6</sub> Ni <sub>6</sub> O <sub>2</sub>			
-7.087	-7.027	-6.817			
-1515.37	-1789.10	-2062.22			
	Nb <sub>6</sub> Ni <sub>6</sub> -7.087 -1515.37	Nb <sub>6</sub> Ni <sub>6</sub> Nb <sub>6</sub> Ni <sub>6</sub> O           -7.087         -7.027           -1515.37         -1789.10	Nb <sub>6</sub> Ni <sub>6</sub> Nb <sub>6</sub> Ni <sub>6</sub> O         Nb <sub>6</sub> Ni <sub>6</sub> O <sub>2</sub> -7.087         -7.027         -6.817           -1515.37         -1789.10         -2062.22		

-136.86

-136.71

Table 4.9 Fermi energy and total energy of calculated phases (eV)

Table 4.10 Overlap populations for Zr<sub>4</sub>Ni<sub>2</sub>O

 $\Delta E_{T}$ /oxygen

Atomic interaction	Overlap population	Interatomic distance (Å)
Zr2 - Zr1	0.1646	3.12
Zr1 - Ni	0.1347	2.76
Zr1 - 0	0.1089	2.27
Zr2 - Ni	0.1014	2.67
Zr1 - Zr1	0.0980	3.21
Zr1 - Ni	0.0412	3.10

populations. Figure 4.14 (b) contains the sum of the Zr1 - Zr1 and the short Zr1 - Ni overlap populations. Each of these COOP curves show empty bonding orbitals above the Fermi level. The only indication of antibonding character at the Fermi level is in the COOP curve for Zr1 - O interactions, in Figure 4.14 (c). The calculation of empty bonding levels was the motivation for the synthesis of more electron - rich compounds than  $Zr_4Ni_2O$ , substituting niobium for zirconium, or copper for nickel.

## Discussion

The  $Ti_2Ni$  type structure has been described in terms of two interpenetrating three-dimensional networks made of idealized octahedra and tetrahedra [84]. Table 4.2 lists the idealized positions that



Figure 4.14 COOP curves for  $Zr_4Ni_2O$ . Fermi level indicated by dashed line. Bonding interactions indicated by (+), and antibonding by (-). (a) Sum of  $Zr_2 - Zr_1$  and  $Zr_2 - Ni$  overlap populations. (b) Sum of  $Zr_1 - Zr_1$  and  $Zr_1 - Ni$  overlap populations. (c) Sum of  $Zr_1 - O$  overlap populations.

would give regular polyhedra. A network of octahedra is formed by the metal atoms on the 48f site. Figure 4.4 shows this network of octahedra, with oygen occupying the 16c site. With the idealized parameters, M1 is at (x,0,0) with x = 0.1875, and all the face sharing octahedra are exactly the same size. When x deviates from this position the octahedra centered at an 8a site maintain ideal octahedral symmetry, but the other octahedra, centered at 16c site, lose their four fold symmetry, and become distorted octahedra, or more precisely, trigonal antiprisms. The direction of the deviation of x from ideality is related to the oxygen occupancy. The octahedra, regular or distorted, centered by oxygen are expanded. When oxygen occupies the 8a site, at the origin, the expansion of the regular octahedron corresponds to an increased value for x (compare Nb<sub>6</sub>Ni<sub>6</sub>O, with x = 0.1996, and ideal x = 0.1875). Occupancy of the 16c site causes expansion of the distorted octahedra, or trigonal antiprisms, and a corresponding decrease in x (compare x = 0.1852 in  $Zr_4Ni_2O$  and x = 0.1867 in  $Nb_6Ni_4Ta_2O_2$ , with ideal x = 0.1875). The expansion of the oxygen - centered octahedra can be interpreted as resulting from the filled antibonding metal - oxygen orbitals, as seen in Figure 4.14 (c) for  $Zr_4Ni_2O$ . Oxygen occupancy is not the full story, however. In the case of the binary  $Ti_2Ni$ [79], with no oxygen, x = 0.189, and is also expanded from the ideal framework. Likewise, in  $Zr_6Ni_4Ti_2O_{0.6}$ , where oxygen is in both sites, x increases. Only one reference suggests the simultaneous occupation of both 8a and 16c sites in Nb<sub>8</sub>Zn<sub>4</sub>C<sub>3</sub> [71], noting the C-C separation would be comparable to the spacing between octahedral sites in the filled - Mn<sub>5</sub>Si<sub>3</sub> type structures. The stoichiometry of this phase was determined by elemental analysis on a heterogeneous sample. The coordination number of an interstitial atom in the  $Mn_5Si_3$  structure is 6 + 2. The interstitial atoms in a  $Ti_2Ni$  structure with all octahedral sites filled would have coordination numbers of 6 + 2 and 6 + 4. Refinement results of  $Zr_6Ni_4Ti_2O_{0.6}$  are the first indication of partial occupancy of both sites. All previous reports in which interstitial atomic parameters are refined indicate occupancy of either the 8a or 16c site, but not both.

Interpenetrating the octahedral network is another network made of corner-sharing stella quadrangula. See Figure 4.5. An ideal stella quadrangula is defined as consisting "of four regular tetrahedra, each sharing one face with a central, fifth tetrahedron, which is also regular (or four regular tetrahedra each sharing three edges, one with each of its three neighbors)." [84] In these compounds the central tetrahedron is always Ni, on the 32e site, and the other atoms are the metals on the 16d site, which cap the faces of the Ni<sub>4</sub> tetrahedra. None of these tetrahedra are centered by interstitial atoms. The fractional coordinate of x for the metal atom at 32e has been converted from the value in the source to the alternate but equivalent value corresponding to the conventional positions. The atom position for Ni at 32e, (x, x, x), shifts from the ideal x = 0.8250 to the observed x = 0.8311 to x = 0.8396. The effect of increasing the x parameter is to enlarge the central nickel tetrahedron. A look at the distances in Table 4.4 shows these units are far from regular stella quadrangula. In all cases the central Ni<sub>4</sub> tetrahedron is expanded ( $d_{Ni-Ni} > d_{Ni-M2}$ ). Zr<sub>4</sub>Ni<sub>2</sub>O shows the largest departure from ideality. For the ideal structural arrangement of this compound, d<sub>Ni-Ni</sub> = 2.5873 Å. The observed distance is much larger,  $d_{Ni-Ni}$  = 3.0910 Å. The distance between the nickel atoms and the zirconium atoms in the octahedral network consequently decreases considerably from the ideal. Compare the observed  $d_{Zr1-Ni} = 2.783$  Å with the ideal  $d_{Zr1-Ni} = 3.0224$  Å in Zr<sub>4</sub>Ni<sub>2</sub>O. This bond lengthening within the Ni<sub>4</sub> tetrahedron suggests Ni-Ni interactions are weakening, relative to Zr-Ni interactions. It is tempting to suggest this is supported by the calculated overlap populations, where nickel - nickel overlap was more than an order of magnitude lower than the other interactions. The zirconium - nickel overlap populations, on the other hand, were quite significant (see Table 4.10). However, comparisons between overlap populations must be done with care. The overlap population between atoms A and B is defined as being proportional to  $c_{iA}c_{iB}S_{ii}$ , where c is the orbital coefficient, and S is the overlap integral. Overlap populations of Ni-Ni interactions can only be compared to other Ni-Ni interactions, and even then only when
distances are the same, since S is a function of distance. Then, if there is a difference in the overlap populations is it related to chemical interactions driven by symmetry rather than by distance. But if these Zr-Ni interactions are strong, as mentioned above, this suggests that the visual description of the structure in terms of two interpenetrating networks does not accurately portray the chemical interaction between the two networks. Rogl [90] perhaps recognized this, and described the structure in terms of the packing of the icosahedral units around the M2 atoms at the 16*d* sites. Figure 4.5 only shows the six nickel atoms around M2. Table 4.4 lists the coordination also to six M1 atoms, and they arrange in a distorted icosahedral coordination. The Zr1 - Zr2 and Zr1 - Ni interactions are exactly the bonding connections between the two networks. Note the highest orbital overlap populations in Table 4.10 involve interactions *between* the two interpenetrating networks, rather than within a network.

The inherent beauty of this structure has not been overlooked by others. Calculations of periodic minimum surfaces for  $W_3Fe_3C$  of this structure type divide the structure into two interpenetrating networks, and suggest the mode for wearing of this high speed steel [91]. Two flaws appear in this article. First,  $W_3Fe_3C$  is not responsible for the characteristic properties of high speed steel [70]. Second, periodic minimum surfaces cannot be generated for certain space groups,  $Fd\overline{3m}$  among them [92]. However, periodic equi-potential surfaces and periodic zero potential surfaces can be generated for this space group. The potential surfaces of appropriate Coulombic fields are very similar in shape to minimal surfaces, but can be correlated to the spatial distribution of the electrons, and hence correlated to physical properties. For the  $Ti_2Ni$  structure the potential surface resides between the two interpenetrating networks. One can assume that the weakest bound electrons are located close to the potential surface. In a metal, these are the conduction electrons. This view of potential surfaces in no way contradicts the finding here of significant interaction between the two structural networks.

It is interesting to note some structural similarities with other phases here. A two-dimensional analogue to the three-dimensional network of face-sharing zirconium octahedra is seen in the kappa phase [80] and the new  $Zr_6Ni_6TiSiO_{1.8}$  structure [81]. In each case, rings of twelve face-sharing octahedra form. In the case of all three of these structures, icosahedral units fill the void spaces and link the octahedral networks.

The results of this study can be rationalized in a system by system manner. In the Nb/Ni/O system the two phases Nb<sub>4</sub>Ni<sub>2</sub>O and Nb<sub>6</sub>Ni<sub>6</sub>O occur. This occurance was not observed in the Zr/Ni/O system. This may be explained by looking at the phase diagrams of the intermetallic Zr/Ni and Nb/Ni systems. In the Nb/Ni binary system there are only two compounds, NbNi3 and Nb7Ni6, which compete with formation of the ternary oxide. In neither case is the Nb:Ni ratio 1:1 or 2:1. The binary intermetallics in the Zr/Ni system, especially ZrNi, compete more favorably with the formation of the ternary oxide. The oxygen occupancy in the Nb<sub>4</sub>Ni<sub>2</sub>O phase has not been determined experimentally, but is based on the assumption that the oxygen occupancy in this phase is the same as for Nb<sub>6</sub>Ni<sub>4</sub>Ta<sub>2</sub>O<sub>2</sub>. The two phases Nb<sub>6</sub>Ni<sub>6</sub>O and Nb<sub>4</sub>Ni<sub>2</sub>O show different Nb/Ni ratios and different oxygen content. The band calculations on Nb<sub>6</sub>Ni<sub>6</sub>O suggest the ordering of the oxygen may not be as important as the total amount of oxygen present. Figure 4.15 (a) outlines the possibility of adding different amounts of oxygen to metal frameworks with different Nb/Ni ratios. With oxygen acting as an electron sink, the core with more free valence electrons in the conduction band will favor adding more oxygen atoms. Assuming a filled  $d^{10}$  configuration, Nb<sub>8</sub>Ni<sub>4</sub> contains 80 free valence electrons per primitive unit cell, and  $Nb_6Ni_6$  has 60 electrons. Thus  $Nb_8Ni_4$  will add two oxygen atoms per formula unit to form  $Nb_8Ni_4O_2$  and  $Nb_6Ni_6$  will add only one to form Nb<sub>6</sub>Ni<sub>6</sub>O.

The same conclusion is reached if the oxygen ordering is assumed to determine the metal ratios, rather than the metals determining oxygen ordering as described above. In this case, the two



Figure 4.15 (a) Addition of oxygen to hypothetical metal framework follows path shown by bold arrows. (b) Addition of capping metal atoms to core compounds follows path shown by bold arrows.

core compounds with different oxygen content, Nb<sub>6</sub>Ni<sub>4</sub>O and Nb<sub>6</sub>Ni<sub>4</sub>O<sub>2</sub>, can add either niobium or nickel to the 16*d* site (Figure 4.15 (b)). Nb<sub>6</sub>Ni<sub>4</sub>O has 56 free electrons in its conduction band, and Nb<sub>6</sub>Ni<sub>4</sub>O<sub>2</sub> has 52. Since Nb<sub>6</sub>Ni<sub>4</sub>O is more electron rich it will more readily add nickel, whose atomic orbitals lie lower in energy than the Fermi level and will act as electron acceptors, than gain electrons by adding niobium. Nb<sub>6</sub>Ni<sub>4</sub>O<sub>2</sub>, with fewer free electrons will favor the addition of niobium, whose orbitals lie above the Fermi energy and will act as electron donors to form Nb<sub>8</sub>Ni<sub>4</sub>O<sub>2</sub>, or Nb<sub>4</sub>Ni<sub>2</sub>O. While this explanation is internally consistent, it does not explain the formation of phases like Mo<sub>6</sub>Co<sub>6</sub>C and Mo<sub>6</sub>Co<sub>6</sub>C<sub>2</sub> where both possible orderings of interstitials are observed for a single metal ratio. A Nb<sub>6</sub>Ni<sub>6</sub>O<sub>2</sub> phase may also exist, but the corresponding shift in lattice parameters would be minimal, and would require sufficient diffraction data for structural analysis. However, the formation of this phase is unlikely. When additional oxygen was added in the synthesis NbO and Ni formed as minor phases.

The formation of only Nb<sub>6</sub>Ni<sub>4</sub>Ta<sub>2</sub>O<sub>2</sub>, and no other tantalum containing compounds, can be explained on the basis of work on mixed niobium/tantalum sulfides performed previously in this lab [19,20]. In these sulfides, the formation of certain phases depends on the relative strengths of metal -sulfur bonds and metal - metal bonds. The same interplay between metal - oxygen and metal - metal bonds exists in these oxide phases. Generally speaking, Ta-O bonds are stronger than Nb-O bonds, by electronegativity arguments. Also, Ta-M bonding among transition metals is generally stronger than Nb-M bonds in a given structure, because of greater d-orbital expansion and overlap of 5d transition metals. In the Ti<sub>2</sub>Ni type structure one must consider the balance between the M-O and the M-M bonding. It was found that Nb<sub>4</sub>Ni<sub>2</sub>O forms. In this structure, the oxygen is surrounded by niobium in the 48*f* site, forming Nb<sub>6</sub>O octahedra. The other niobium atom sees only other metal atoms, icosahedrally coordinated to six nickel and six niobium atoms. When tantalum replaces niobium in the 16*d* site, oxygen still sees only niobium, but now tantalum can increase the

metal-metal interactions in the structure. If, however, tantalum were to replace the other niobium atoms, the stronger Ta-O bonds would come *at the expense* of the Ta-M bond strength, shifting the balance of metal - oxygen versus metal - metal bond strength, and the phase becomes unstable with respect to formation of the binary phases.

One can consider the role of oxygen in stabilizing the  $Ti_2Ni$  type structure in the  $Zr_4Ni_2O$  phase. Oxygen is also necessary for the formation of the  $Hf_4Ni_2O$  phase [73], but is not necessary for  $Ti_2Ni$ . A principle difference between titanium on the one hand, and zirconium and hafnium on the other, is the orbital expansion of the d orbitals for zirconium and hafnium and the corresponding increase in metal - metal bond strength. The binary intermetallic phases that form are the arrangements of atoms that maximize the bonding energy between them, and thus minimize the Gibbs free energy. The phases in the Zr/Ni system are different than those in the Ti/Ni system because the bonding energies of zirconium and titanium are different. When oxygen is added to the Zr/Ni system and zirconium - oxygen bonds form, the zirconium - metal bonding decreases. This decrease in metal - metal bonding makes it more like the Ti/Ni system, and the filled  $Ti_2Ni$  phase is stabilized with respect to the binary phases. In the mixed Zr/Ti phase,  $Zr_6Ni_4Ti_2O_{0.6}$ , even less oxygen is required, as would be expected.

#### 5. NEW ZIRCONIUM KAPPA PHASES

### Introduction

The kappa phases are an interesting set of compounds. The kappa phase is of the general form  $M_0M'_4X$ , where M and M' are transition metals, M being the more electropositive of the two. They exist for a wide variety of interstitial atoms, and for a wide combination of transition metals. Recently, superconductivity has been discovered in a kappa phase [21]. Interest has also been expressed in studying the catalytic properties of these compounds in processes where Chevrel phases have been studied. If a technological interest arises for these kappa phases, many of which have been known for quite some time, they may come under intense physical and chemical study. The work reported here demonstrates that through the use of modern techniques these compounds may each be found to be significantly more complicated than the formula suggests. Both the transition metal framework and the interstitial atoms demonstrate significant deviation from ideality. Specifically, the mixing of M and M' on the metal atom sites can change the stoichiometry substantially from the  $M_0M_4X$  formula. Secondly, the formula, as written, does not reveal the presence of a second interstitial site, the occupation of which may have been undetected in the earlier work. The possibility exists for two different interstitial sites to be occupied by the same element, or by different elements, or for one site to be preferentially occupied in one compound and the other site to be occupied in another compound. The interstitial sites may also undergo substitution and/or exhibit partial occupancy or nonstoichiometry. Each of these are considered later in more detail, but this serves to illustrate that the findings of this study will be important in any future work on these kappa phases. Specifically, the presence of light interstitial elements must be considered, i.e. by performing the synthesis with both the intentional and unintentional presence of oxygen, for example, and noting changes in lattice parameters. In some cases, the formation of the

phase may be affected by the presence of the interstitial atoms. Chemical analysis, i.e. by EDS, is important for determining ranges of substitution in metal atoms, and in the interstitial atoms. Finally, the importance of the precision of single crystal diffraction studies cannot be overstated.

Many examples of the hexagonal kappa phase in ternary systems have been reported since their original discovery [93,94]. Table 5.1 shows the surprising variability and adaptability in the elements which fill the X position in the kappa phase. X can be one of several p-group elements or an iron group 3d transition metal.

M-M'-X	X	M-M'-X	X
Zr-Os-X	0	Ti-Fe-X	0
Zr-Re-X	В,О	Ti-Mn-X	0
Zr-Mo-X	B,O,Fe,Co,Ni <sup>b</sup> ,S <sup>b</sup>	Mo-Cu-X	AI/C
Zr-W-X	B,O,S <sup>b</sup> ,S/Ni <sup>b</sup>	Mo-Ni-X	AI/C
Zr-Nb-X	S <sup>c</sup>	Mo-Co-X	AI/C
Zr-Ta-X	S <sup>c</sup>	Mo-Fe-X	AI/C
Hf-Os-X	B,O,Si,P,S,Ge,As, Se,Fe,Co,Ni	Mo-Mn-X	AI/C
Hf-Re-X	B,O,Si,P,S,Ge,As, Se,Fe,Co,Ni	W-Ni-X	С
Hf-Mo-X	B,O,Si,P,S,Ge,As, Se,Fe,Co,Ni	W-Co-X	С
Hf-W-X	B,O,P,S,Ge,As,Sc, Fe,Co,Ni	W-Fe-X	C, AI/C
Hf-Nb-X	S <sup>c</sup>	W-Mn-X	C, AI/C
Hf-Ta-X	S <sup>c</sup> ,Se <sup>d</sup> ,S/Se <sup>d</sup>	W-Cr-X	С

Table 5.1 Known kappa phases  $(M_0M_4X)^a$ 

<sup>a</sup> Table adapted from [94]

° [21] d [95]

<sup>&</sup>lt;sup>b</sup> [80]

The above formulation is somewhat simplified in that it does not reveal the fact that the interstitial elements can occupy different interstitial sites. To take this into account the formula can be rewritten  $M_9M_4X_1X_3$ , where X is an interstitial atom on the 2c position, a trigonal prismatic site, and X' is an interstitial atom on the 6g position, an octahedral site. It has been convenient up until now to consider just one interstitial site because all previous reports, with three exceptions, have indicated occupancy of only one site or the other, but not both. These exceptions are the carbides W-Fe-C and W-Co-C, where both sites are simultaneously occupied, but with 50% of the 2c site vacant [96,97]. Hf-Mo-S has also been reported with complete filling of the 2c site, but only partial filling (6-9%) of the 6g site by S [98]. The ternary Hf-Mo-Ge kappa phase is found to be a quaternary, Hf-Mo-Ge-O, with germanium on the 2c site, and oxygen on the 6g site, and vacancies on both sites [99]. Besides these three exceptions, the kappa phases are reported to have only one interstitial site occupied. The oxides are thought to contain oxygen in the octahedral site, and all other interstitial atoms, X, occupy the larger trigonal prismatic site. The results of this study demonstrate that simultaneous occupation of both sites is at least a common, and sometimes necessary, condition. The new zirconium-containing kappa phases,  $Zr_9W_4SO_x$ ,  $Zr_9Mo_4SO_x$ , and  $Zr_9W_4(S/Ni)O_3$ , have been synthesized. The  $Zr_9W_4Ni$  phase has been determined to be oxygen stabilized. The lattice parameters of the new phases are reported, as well as the single crystal refinement of the nickel substituted sulfide. This last compound is an example of nickel substitution for sulfur in metal rich chalcogenides, a previously reported effect [27]. In addition, this compound shows the ability of the structure to fully occupy the octahedral interstitial sites with oxygen.

Before proceeding further with the chemistry of the kappa phase it is useful to look more closely at the structure of this phase. The unit cell is hexagonal (P6<sub>3</sub>/mmc) with a c/a ratio nearly equal to one. Figure 5.1 shows in projection a layer network of face sharing octahedra. In terms of the M<sub>9</sub>M<sub>4</sub>X<sub>1</sub>X<sub>3</sub> formula, this figure contains only the M<sub>9</sub>X<sub>3</sub> portion. The hexagonal unit cell is



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Figure 5.1 Projection of  $M_9X_3$  portion of  $M_9M_4XX_3$  kappa phase, showing network of face sharing octahedra. Central octahedron is outlined for clarity. Alternating octahedra are centered by interstitial atom X'.

outlined. The octahedron in the center of the unit cell is also outlined for clarity, and is centered by an X' atom. This octahedron shares two opposite faces with octahedra which are seen in projection along their three fold axis. The face sharing octahedra form rings containing twelve octahedra. The octahedra are alternately centered and empty. In terms of a zirconium network of face sharing octahedra there is a surprising relation between the kappa phase and the  $Ti_2Ni$ -type structure. In the kappa phase a two-dimensional hexagonal layer forms from these octahedra, which are alternately filled and empty. In the cubic  $Ti_2Ni$ -type structure, these rings of face sharing octahedra form a three-dimensional network. In these cases, similar building blocks arrange to form strikingly different structures. Oxygen is essential to the formation of this network of octahedra in these kappa phases as well as in the  $Ti_2Ni$ -type phases containing zirconium.

The interstitial sites are more clearly seen viewing along the [110] direction. In Figure 5.2 trigonal prismatic sites and two crystallographically distinct octahedral sites are shown. The trigonal prisms are tricapped, although only one face is shown capped in the figure. The octahedra above and below the trigonal prism have their center at the 4f site and are vacant in all known cases. The octahedra which are occupied by interstitial atoms are those shown between the trigonal prisms. These form a zig-zag chain of corner-sharing octahedra along the *c*-axis. This network shown consists only of the metal M atoms.

Figure 5.3 is a projection of the complete structure. Icosahedral units fill the voids in the octahedral network. These icosahedra share faces to form a chain along the c-axis. The icosahedra are all centered by metal M<sup> $\prime$ </sup> atoms (Figure 5.4).

Such is the structure of the kappa phase. The variability in X and X'suggests the formation of this phase depends largely on the strength of the metal-metal interactions within the framework of this structure. In fact, the kappa phase may be considered a filled variant of the intermetallic compounds  $Mn_3Al_{10}$  and  $Co_4Al_{10}$ .



Figure 5.2 Portion of the kappa phase structure, showing only the metal atoms M, projected along a plane almost perpendicular to the (110) plane. Octahedral and trigonal prismatic interstitial sites clearly seen. Distances shown for  $Zr_9W_4(S/Ni)O_3$ .





Figure 5.4 View of icosahedral chain along c axis. Distance shown for  $Zr_9W_4(S,Ni)O_3$ .

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### **Experimental Details**

The single crystal used for the refinement was picked from a multi-phase sample of zirconium, nickel, and sulfur which melted and reacted with the tungsten crucible at 1400°C. The stoichiometry of the sample was initially taken to be " $Zr_3NiS$ ". The product contained the kappa phase as a major phase, with  $Zr_3S_2$  and another (unknown) phase present as minor phases. The crystal was small but regular shaped. Intensity data for this crystal were collected using a Rigaku AFC6R single crystal diffractometer and monochromated MoK $\alpha$  radiation, employing the  $\omega$ -2 $\theta$  scan technique up to 55° in 2 $\theta$ . The observed intensities were corrected for Lorentz polarization and absorption effect. Table 5.2 contains the crystal data.

The bulk synthesis of all samples was carried out by initially combining elemental zirconium and sulfur powders in the mole ratio n(Zr)/n(S) of 9/1 and heating in an evacuated silica tube at 450°C until no visible traces of elemental sulfur remained. The temperature was raised to 800°C and held there for several days. The resulting zirconium sulfide was mixed with powders of the other metals and pressed into pellets. The pellets were arc-melted on a water cooled copper hearth in an argon atmosphere with a tungsten electrode. Each arc-melted sample was annealed in a tungsten crucible in an induction furnace at about 1200°C for 6-18 hours.

X-ray powder patterns were obtained with a vacuum Guinier camera FR552 (Enraf-Ninius, Delft, The Netherlands) and CuK $\alpha$ 1 radiation, with silicon as an internal standard. The powder patterns were indexed by comparison to the kappa phases, and the lattice parameters were calculated by least-squares refinement.

### **Results and Discussion**

The initial refinement of the single-crystal data led to the nominal formula  $Zr_9W_4S$ . Three corrections were necessary for the final refinement. Initially, the thermal parameters for the sulfur

Formula	$Zr_{9.22}W_{3.78}S_{0.67}Ni_{0.33}O_{3.00}$
Space group	P6 <sub>3</sub> /mmc (#194)
a (Å)	8.688(7)
c (Å)	8.558(5)
V (Å <sup>3</sup> )	559.4(7)
Z	2
d <sub>calc</sub> (g/cm <sup>3</sup> )	9.627
Crystal size (mm <sup>3</sup> )	0.04x0.02x0.02
μ (MoKα) (cm <sup>-1</sup> )	480.79
Data collection instrument	Rigaku AFC6R
Radiation (monochromated in incident beam)	ΜοΚα (λ=0.71069)
Octants measured	±h,k,±l
No. reflections measured	1904
No. unique data, total with $F_o^2 > 3\sigma(F_o^2)$	162
No. parameters refined	24
Trans. factors, max/min	1.000/0.560
Secondary ext. coeff. (10 <sup>-7</sup> )	2.496
$R^{a}, R_{w}^{b}, GOF^{c}$	0.026, 0.026, 0.975
Largest difference peak (e/Å <sup>3</sup> )	+3.78
Largest negative peak (e/Å <sup>3</sup> )	-2.17

Table 5.2 Crystal data for  $Zr_9W_4(S/Ni)O_3$ 

<sup>a</sup> R =  $\Sigma ||F_0| - |F_c|| / \Sigma |F_0|$ 

<sup>b</sup>  $R_w = [\Sigma w (|F_o| - |F_c|)^2 / \Sigma w |F_o|^2]^{1/2}; w = 1/\sigma^2 (|F_o|)$ 

<sup>c</sup> GOF =  $(\Sigma(|F_o|-|F_c|)/\sigma_i)/(N_{obs refl}-N_{parameters})$ 

were unreasonably small. Placing nickel on that position gave equally unreasonable results. Placing mixed sulfur/nickel occupancy on the 2*c* site improved the results considerably. Kappa phases are known which contain either sulfur or nickel, as well as many other elements, but this is the first example of mixed occupancy of this site. EDS measurements also detect the presence of both sulfur and nickel in this phase. The atoms in this site are tricapped trigonal-prismatically coordinated to zirconium atoms. Nickel substitution of sulfur has been observed in the metal rich sulphides  $Nb_6Ni_xS_{3-x^*}$  and  $Nb_9Ni_{2-x}S_{3+x}$  [27], in which nickel substitutes for sulfur in highly coordinated capped trigonal-prismatic sites. Substitution of sulfur by nickel is consistent with the ability of sulfur to be involved in delocalized, metallic bonding.

An additional change was necessary, since the Fourier difference map calculated during refinement indicated the presence of an atom at the 6g position. As noted previously, other reports have indicated partial occupancy of the octahedral position by oxygen (up to 48% [99,100]). The result of the refinement in this work yielded total oxygen occupancy of this site. This is the first example of both the 2c and the 6g sites being fully occupied. The experimental steps for sample preparation offered several opportunities for inclusion of oxygen. As discussed in the introduction, techniques for solid state synthesis of early transition-metal sulfides are susceptible to oxygen inclusion. The determination of partial or complete oxygen occupancy in the known kappa phases is incomplete, and the results obtained here suggest that such occupation is in all cases a real possibility.

The final step in the refinement was to allow partial zirconium substitution of the tungsten on the 6h and 2a sites [98-103], as substantial M-M' mixing has been observed in other phases. The variability in M-M' mixing has been correlated with the variability observed in lattice parameters of these phases. Full details of the refinement results are in the following tables. Table 5.3 lists the atomic parameters, including percent mixing on those sites refined with mixed occupancy. Anisotropic thermal parameters are in Table 5.4. Interatomic distances less that 3.7 Å are listed on Table 5.5.

A few of the interatomic distances are labelled in Figure 5.2 and Figure 5.4. The zirconiumzirconium distances within the trigonal prism range from 3.350 to 3.473 Å (Figure 5.2). This range is similar to the distances in the trigonal prism in  $Zr_3NiO$ , where  $d_{Zr-Zr} = 3.325 - 3.682$  Å. In both structures, these distances are much larger than the distance between the zirconium and the central atom, which is 2.612 Å in the kappa phase with mixed S/Ni occupancy, and 2.657 Å in  $Zr_3NiO$ , where just nickel occupies the central position. The octahedral arrangement of zirconium atoms is significantly distorted. Along one edge  $d_{Zr1-Zr1} = 3.151$  Å, while along the edge shared with the trigonal prism it is 3.473 Å. Consequently, the zirconium-oxygen distances are different, with  $d_{Zr1-O}$ = 2.345 Å and  $d_{Zr2-O} = 2.240$  Å.

The possibility of filling the 4*f* site by placing oxygen in this octahedral site at (1/3, 2/3, 0.598) can be considered. The zirconium-oxygen distances would be between 2.26 and 2.39 Å. The short oxygen-oxygen distance would be only 2.60 Å, and with the oxygen in the 6*g* position the separation would be 2.64 Å. For the same reason as discussed in the  $Ti_2Ni$  type structures, full occupancy of both sites simultaneously is not expected.

A bulk sample of the  $Zr_9W_4(S_{0.7}Ni_{0.3})O_3$  phase was prepared, and had the same lattice parameters as the minor phase from which the crystal was picked. Very little work on zirconiumcontaining kappa phases has been done. Only two previous reports for Zr-W-X kappa phases exist, so an attempt was made to synthesize both the Zr-W-S and Zr-W-Ni phases. In the synthesis of these phases, if the kappa phase was present after the arc melting step, as determined by X-ray powder diffraction films, the sample was then annealed. If the phase was not present after arc melting, it generally did not appear upon annealing. In preparing these new phases oxygen was not added in the starting material as a metal oxide, but oxygen was undoubtedly present as surface or

Atom	Site	x	у	Z	Occupancy(%)	B <sub>eq</sub> (Å) <sup>a</sup>
Zr1	12k	0.2001(2)	0.4002	0.0543(2)	100	0.4(1)
Zr2	6 <i>h</i>	0.5442(2)	0.0883	1/4	100	0.5(2)
W1 Zr	6 <i>h</i>	0.8928(1)	0.7857	1/4	94(2) 6	0.35(7)
W2 Zr	2 <i>a</i>	0	0	0	95(2) 5	0.26(6)
S Ni	2 <i>c</i>	1/3	2/3	1/4	67(6) 33	0.9(3)
0	6 <i>g</i>	1/2	0	1/2	100	0.7(4)

Table 5.3 Atomic parameters for  $Zr_9W_4(S,Ni)O_3$ 

<sup>a</sup>  $B_{eq} = 8\pi^2/3 \Sigma_i^3 \Sigma_i^3 U_{ij} a_i^* a_j^* \overline{a}_i^* \overline{a}_j^*$ 

Table 5.4 Anisotropic thermal parameters for Zr<sub>9</sub>W<sub>4</sub>(S,Ni)O<sub>3</sub>

Atom	U <sub>11</sub>	U <sub>22</sub>	U <sub>33</sub>	U <sub>12</sub>	U <sub>13</sub>	U <sub>23</sub>
Zr1	0.005(1)	0.008(1)	0.004(1)	0.004	0.002(2)	0.001
Zr2	0.005(1)	0.009(2)	0.006(1)	0.004	0	0
W1	0.0050(6)	0.0038(7)	0.0041(7)	0.0019	0	0
W2	0.004(1)	0.004	0.002(1)	0.002	0	0
S/Ni	0.012(5)	0.012	0.008(6)	0.006	0	0
O <sup>a</sup>	0.008(5)					

<sup>a</sup> Isotropic thermal parameter refined for oxygen

		· · · · · · · · · · · · · · · · · · ·	3		
Zr1	- 0	2.345(2) x 2	W1	- W2	2.679(2) x 2
	- S/Ni	2.612(2) x 1		- W1	2.793(4) x 2
	- W1	2.956(2) x 1		- Zr2	2.951(3) x 2
	- W2	3.047(3) x 1		- Zr1	2.956(2) x 2
	- W1	3.101(3) x 2		- Zr1	3.101(3) x 4
	- Zr1	3.151(3) x 2			
	- Zr2	3.241(3) x 2			
	- Zr2	3.245(2) x 2	<b>W</b> 2	- W1	2.679(2) x 6
	- Zrl	3.350(4) x 1		- Zr1	3.047(3) x 6
	- Zr1	3.473(5) x 2			
			S/Ni	- Zr1	2.612(2) x 6
Zr2	- 0	2.240(2) x 2		- Zr2	3.172(4) x 3
	- W1	2.951(3) x 2		- 0	3.300(2) x 6
	- S/Ni	3.172(4) x 1			
	- Zr2	3.193(6) x 2	0	- Zr2	2.240(2) x 2
	- Zrl	3.241(3) x 4		- Zr1	2.345(2) x 4
	- Zr1	3.245(2) x 4		- S/Ni	3.300(2) x 2

Table 5.5 Interatomic Distances for  $Zr_9W_4(S/Ni)O_3$ . Values listed for distances less than 3.7 Å.

low level bulk oxide in the zirconium. The zirconium used was in a powder form, and was stored on a shelf rather than in a dry box. Thus, while the presence of oxygen is certain, the amount of oxygen is undetermined. By this method  $Zr_9W_4SO_x$  was prepared.  $Zr_9W_4Ni$  did not form, even when oxygen was intentionally added, as  $ZrO_2$  or NiO, in the starting material. Thus, there is not a continuous range of solid solubility between the two endmembers  $Zr_9W_4SO_x$  and  $Zr_9W_4NiO_x$ , since the nickel endmember does not form. A few more experiments were done to investigate the extent of nickel substitution for sulfur. The four molar ratios n(S)/n(Ni) 3/1, 2/1, 1/1, and 1/3 were used in the starting materials. The kappa phase formed when the n(S)/n(Ni) ratio was 3/1 and 2/1, but did not form when it was 1/1 or 1/3. The maximum extent of nickel substitution may be that found in the sample from which the crystal was picked. In all of these experiments there was a small (1-3%) mass loss in the arc melting step due to vaporization of sulfur and/or nickel. Consequently, in all these samples, minor phases present were elemental zirconium, tungsten, or  $W_2Zr$ .

The kappa phase  $Zr_9Mo_4Ni$  has been previously reported [97]. The preparation of this compound from the elements, by the arc melting method, was not successful. When the synthesis was tried again using NiO in the starting materials, the kappa phase was observed by X-ray powder diffraction. Thus it appears that complete oxygen occupancy of the 6g site may be necessary for the formation of the kappa phase. The importance of oxygen for the formation of the phase is dependent on the elements making up the metal framework, as well as the interstitial element X. Indeed, the role of the metal framework and the difference between tungsten and molybdenum is evident in the fact that the kappa phase forms for Zr/Mo/Ni/O, but not for Zr/W/Ni/O. The  $Zr_9Mo_4SO_x$  phase was also synthesized, and since  $Zr_9Mo_4NiO_x$  is also known, and sulfur/nickel substitution has been observed on the tungsten analogue, it might expected that a solid solution forms between these two. The lattice parameters for these new kappa phases are listed below in Table 5.6.

By looking at the list of known kappa phases, many other possibilities of mixed interstitial sites can be considered. Examples, like  $Zr_9W_4(S,Ni)O_3$ , where another element only partially substitutes for the interstitial atom, or examples of complete solubility ranges might be found. In the former case, new understanding may be gained concerning the role of metal-metal bonding in this phase (i.e. W vs Mo in Zr-M-Ni). In the latter case, in which the identity of the interstitial atoms is of little consequence, the effect of orbital interactions and electron counts may be such that the Fermi level crosses a region of nonbonding bands. The properties to be found for mixed interstitial phases are not known and present a fertile area for future study. Exceptions to this are the recently discovered superconductivities in Hf-Nb-S, Zr-Nb-S, and Hf-Ta-Se [21,95]. In general, it can be stated that the single crystal and powder diffraction results obtained here strongly suggest that the known kappa phases (Table 5.1) could contain currently undetected interstitials and could exhibit currently undetermined variations in stoichiometry.

Table 5.6 Lattice parameters for new kappa phases

	a (Å)	c (Å)	V (Å <sup>3</sup> )
Zr <sub>9</sub> Mo <sub>4</sub> SO <sub>x</sub>	8.685(2)	8.571(2)	559.8(2)
Zr <sub>9</sub> W <sub>4</sub> SO <sub>x</sub>	8.671(2)	8.607(3)	560.4(3)
$Zr_{9.2}W_{3.8}S_{0.67}Ni_{0.33}O_3$	8.688(4)	8.558(7)	559.4(7)

# 6. Zr<sub>6</sub>Ni<sub>6</sub>TiSiO<sub>x</sub>: A NEW STRUCTURE TYPE WITH A MIXED EARLY-LATE TRANSITION METAL FRAMEWORK

## Introduction

An interstitially stabilized intermetallic in a mixed early-late transition metal system has been found to crystallize in a new structure type. The new compound,  $Zr_6Ni_6TiSiO_x$  (x=1.8), was synthesized by melting Zr, Ni, Si, and  $Ti_2O_3$  in an arc furnace, followed by annealing in vacuum at 900 - 1150°C. The crystal structure was determined by refinement of single crystal x-ray diffraction data. The structure was refined in the centrosymmetric space group  $P\overline{3}m1$ , Z=2, with lattice parameters a = b = 8.2778(9) Å, and c = 7.444(1) Å (R=0.030, R<sub>w</sub>=0.033). Oxygen atoms center zirconium trigonal antiprisms, which share faces to form a three dimensional network. The titanium and silicon atoms are coordinated by icosahedra of nickel, or zirconium and nickel atoms. A structural comparison with the kappa-phase will be discussed.

A substantial diversity of structures of binary compounds in mixed early-late transition metal systems, particularly in the Zr-Ni system, is described in the literature [47,104]. Typically, when an interstitial element reacts with a binary early-late transition metal compound to form a ternary compound, the compound crystallizes in a common structure type. In fact, only a limited number of structure types are known for phases of mixed early and late transition metals which are interstitially stabilized [46]. This work has described the importance of the presence of small amounts of oxygen in stabilizing phases in the Zr-Ni system which do not appear as true binary intermetallic compounds.

The ternary metal system, Zr-Ti-Ni, contains phases which do not occur in either of the binary systems Zr-Ni or Ti-Ni (i.e. the hexagonal Laves phase ZrTiNi [105,106], and the BaPb<sub>3</sub> type

structure  $ZrTi_2Ni_9$  [107,108]). It is natural to expect that interstitials in this ternary system may stabilize new compounds, with respect to the ternary intermetallics and interstitially stabilized binary compounds. There are some examples of ternary, and quaternary, phases which form with the addition of an interstitial atom, such as oxygen in the case of a few kappa-phases (eg.,  $Zr_9W_4(S,Ni)O_{3}$  [80,94,99]. In this section the structure of a new interstitially stabilized compound with the composition  $Zr_6Ni_6TiSiO_{1,8}$  is reported.

## **Experimental Details**

Samples were prepared from materials and by procedures described previously. All samples were arc melted three times on a water cooled copper plate with a thoriated nonconsumable tungsten electrode in an argon atmosphere. The arc melted buttons were subsequently crushed and pressed into pellets and annealed in evacuated silica tubes at 900 - 1150°C for 2-3 days. All samples contained  $ZrO_2$  as a minor phase.

The single crystal used for the structural investigation was picked from a sample of a Zr-Ti-Ni alloy which reacted with the silica tube in the annealing process. Subsequent reactions included silicon and oxygen in the starting materials. All handling of materials was done in air. Details of crystal data are listed in Table 6.1.

Semiquantitative analysis by energy dispersive x-ray analysis (EDS) was carried out on a Cambridge S-200 scanning electron microscope with a Northern Tracor Micro Z-II x-ray detector. Surface analysis by x-ray photoelecron spectroscopy was performed on a Perkin Elmer 5500 multitechnique system.

A Quantum Design SQUID magnetometer was used to check for superconductivity and to measure magnetic behavior at a field of 3T over the temperature range 6 - 298 K.

Formula	Zr <sub>5.39</sub> Ni <sub>6.00</sub> Ti <sub>1.71</sub> Si <sub>0.90</sub> O <sub>1.80</sub>
Space group	P3m1(164)
a Å	8.2778(9)
c Å	7.444(1)
v Å <sup>3</sup>	441.7(1)
Z	2
d <sub>cale</sub> , g/cm <sup>3</sup>	7.366
Crystal size, mm <sup>3</sup>	0.08x0.04x0.04
μ(MoKa), cm <sup>-1</sup>	200.84
Data collection instrument	Rigaku AFC6R
Radiation (monochromated in	
incident beam)	$MoK_{\alpha} (\lambda = 0.71069 \text{ Å})$
Temperature, °C	23±1
Scan method	2θ-ω
Octants measured	±h±kl
Data collection range, 20, deg	0-60
No. refl. measured	2897
No. unique data, total	
with $F_0^2 > 3\sigma(F_0^2)$	272
No. parameters refined	37
Trans. factors, max./min.	1.500
Secondary extinction coefficient	2.0(8) x 10 <sup>-7</sup>
R <sup>a</sup> , R <sub>w</sub> <sup>b</sup> , GOF <sup>c</sup>	0.030, 0.033, 1.006
Largest peak, e/Å <sup>3</sup>	+1.44
Largest negative peak, e/Å <sup>3</sup>	-1.89

Table 6.1 Crystal data for  $Zr_6Ni_6TiSiO_x$ 

 $\overline{\mathbf{A}_{\mathbf{R}}^{a} \mathbf{R} = \Sigma ||F_{o}| - |F_{c}|| / \Sigma |F_{o}|}$   $\overline{\mathbf{A}_{\mathbf{W}}^{b} \mathbf{R}_{\mathbf{W}}^{b}} = [\Sigma w (|F_{o}| - |F_{c}|)^{2} / \Sigma w |F_{o}|^{2}]^{1/2}; \ w = 1 / \sigma^{2} (|F_{o}|)$   $\overline{\mathbf{C}_{\mathbf{G}}^{c} \mathbf{G}} = (\Sigma (|F_{o}| - |F_{c}|) / \sigma_{i}) / (N_{obs \ refl}^{-} N_{parameters})$ 

### Results

The crystal was found to exhibit Laue symmetry 3m1, and the single crystal refinement was carried out in the centrosymmetric space group P3m1. The refinement converged with the placement of the Zr, Ni, Ti, Si, and O(1) atoms at the proper sites. The refinement improved significantly when titanium was allowed to partially occupy the Zr(2) position, and also to partially occupy the Si position. At this point, a peak in the Fourier difference map suggested the presence of another oxygen atom, O(2). This atom was added to the refinement, and the multiplicities of both oxygen atoms were allowed to vary. The final positional parameters, equivalent B values, and occupancies of all sites are listed in Table 6.2. The refinement reported here was calculated using a  $F_o^2 > 3\sigma(F_o^2)$  cutoff. An additional refinement using a 1 $\sigma$  cutoff resulted in R = 0.054 and R<sub>w</sub> = 0.043 and no significant change in the thermal or positional parameters. The anisotropic thermal parameters of all non-oxygen atoms are in Table 6.3. Structure factor amplitudes, including unobserved reflections, are in the appendix.

A projection of the whole structure is shown in Figure 6.1. The structure can be described by viewing two connected, alternating layers, the projections of which are shown in Figures 6.2 and 6.3. The layers are labeled A and B, as shown in Figure 6.4. Figure 6.2 shows layer A, centered at z=1/2 and containing only the atoms within the range  $z=1/2 \pm 1/3$ . This layer consists of a network of face-sharing zirconium trigonal antiprisms which form buckled rings. This structural unit matches the description of the kappa phase (compare Figure 5.3). The bold lines mark the Zr-Zr connections that outline the rings. Titanium atoms in an icosahedral environment are in the center of the rings. A common feature in oxygen-stabilized intermetallics of zirconium is the presence of oxygen in the center of the zirconium trigonal antiprisms. The antiprisms in the buckled ring are centered by oxygen in two distinct crystallographic sites, one of which (O(2)) is only approximately one third occupied (this is the antiprism with the three-fold axis along the c-axis, as viewed in the

Atom	Site	x	У	Z	B <sub>eq</sub> <sup>a</sup> (Å <sup>2</sup> )	% occup
Ni(1)	6i	0.1129(2)	-0.1129	0.2553(3)	0.54(2)	100
Ni(2)	6i	0.1726(2)	-0.1726	0.9326(3)	0.54(2)	100
Zr(1)	6i	0.4598(1)	-0.4598	0.1953(2)	0.63(2)	100
Zr(2) Ti	6i	0.2073(1)	-0.2073	0.5688(2)	0.49(3)	79(2) 21(2)
Ti(1)	1 <i>a</i>	0	0	0	0.4(2)	100
Ti(2)	1 <i>b</i>	0	0	1/2	0.7(2)	100
Si Ti	2 <i>d</i>	1/3	2/3	0.874(1)	0.4(2)	90(4) 10(4)
O(1)	3f	1/2	0	1/2	0.7(3)	96(4)
O(2)	2 <i>d</i>	1/3	2/3	0.367(9)	0.4(8)	36(6)

Table 6.2 Positional parameters for  $Zr_6Ni_6TiSiO_x$ 

<sup>a</sup>  $B_{eq} = 8\pi^2/3 \Sigma_1^3 \Sigma_1^3 U_{ij} a_i^* a_j^* \overline{a}_i^* \overline{a}_j^*$ 

Atom	U <sub>11</sub>	U <sub>22</sub>	U <sub>33</sub>	U <sub>12</sub>	U <sub>13</sub>	U <sub>23</sub>
Ni(1)	0.0081(8)	0.0081	0.006(1)	0.0052(9)	-0.0004(4)	0.0004
Ni(2)	0.0077(7)	0.0077	0.006(1)	0.0044(8)	0.0001(4)	-0.0001
Zr(1)	0.0087(6)	0.0087	0.008(1)	0.0054(7)	-0.0004(3)	0.0004
Zr(2)	0.0051(7)	0.0051	0.007(1)	0.0015(7)	-0.0005(4)	0.0005
Ti(1)	0.005(2)	0.005	0.003(4)	0.003	0	0
Ti(2)	0.007(2)	0.007	0.013(4)	0.003	0	0
Si	0.003(2)	0.003	0.007(4)	0.002	0	0
O(1)	0.009(3) <sup>a</sup>					
O(2)	0.01(1) <sup>a</sup>					

Table 6.3 Anisotropic thermal parameters for  $Zr_6Ni_6TiSiO_x$ 

<sup>a</sup>Isotropic thermal parameter refined for oxygen atoms



Figure 6.1 Projection along the c axis of the  $Zr_6Ni_6TiSiO_x$  structure



Figure 6.2 Projection of Layer A, showing atoms at positions with  $z=1/2 \pm .33$  (Ni(2), Ti(1), and Si not in this layer). Zr trigonal antiprism outlined at cell center.

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Figure 6.3 Projection of Layer B, showing atoms at positions with -1/2 < z < 1/2 (O(1), O(2), and Ti(2) at z=1/2 not in this layer).



Figure 6.4 View along the c-axis. Icosahedral coordination of Ti atoms shown. Side view of regions included in Layers A and B, which are shown in projection in Figures 6.2 and 6.3, respectively.

projection in Figure 6.1). The antiprisms in the ring, then, form an alternating pattern of filled, and partially filled antiprisms. The Zr-O distances (2.22-2.35 Å) are typical of oxygen-centered zirconium antiprisms in intermetallic compounds ( $d_{Zr-O}=2.305-2.307$  Å in Zr<sub>3</sub>NiO [66] and 2.27 Å in Zr<sub>4</sub>Ni<sub>2</sub>O). The short O(1)-O(2) distance (2.59 Å) suggests that full occupancy of both sites would be energetically unfavorable, similar to the situation of filling adjacent octahedral sites in the Ti<sub>2</sub>Ni type structures [72]. The icosahedron around the titanium atom consists of 6 zirconium and 6 nickel atoms. Distances in the Ni<sub>6</sub>Zr<sub>6</sub> icosahedron are indicated in Figure 6.4. Figure 6.5 shows the distances within the zirconium network. All interatomic distances less than 3.6 Å are listed in Table 6.4.

Figure 6.3 shows the projection along c of layer B, centered at z=0 and including all atoms except those at z=±1/2. The bold outlines show the Ni<sub>12</sub> icosahedra, centered by titanium at the unit cell origin. Figure 6.4 illustrates how this Ni<sub>12</sub> icosahedron shares faces and stacks with the Ni<sub>6</sub>Zr<sub>6</sub> icosahedron centered at z=1/2. The Ni<sub>12</sub> unit is a fairly regular icosahedron, with a slight expansion at the top and bottom  $(d_{Ni1-Ni1}=2.80 \text{ Å}, \text{ compared to } d_{Ni1-Ni2}=2.55 \text{ Å} \text{ or } d_{Ni2-Ni2}=2.67 \text{ Å})$ . This expansion is necessary to allow face-sharing chains to form with the larger and more irregular Ni<sub>6</sub>Zr<sub>6</sub> icosahedron. The central titanium atom has very short titanium-nickel distances in all of these icosahedra (2.44-2.52 Å). They are shorter, in fact, than any of the nickel-nickel distances (2.55-2.80 Å). A calculation of Pauling bond orders [4] was carried out on this compound, and the short distances and high coordination give the titanium atoms an unusually high bond order in comparison to the other transition metal atoms. This short titanium-nickel distance, however, was also observed in Ti<sub>2</sub>Ni and the filled-Ti<sub>2</sub>Ni, Ti<sub>4</sub>Ni<sub>2</sub>O, structures (d<sub>Ti-Ni</sub>=2.48 Å and 2.46 Å, respectively), in which Ti atoms also center icosahedra [79]. This may be surprising if one considers that the atomic radius of titanium is larger than that of nickel. It is not so surprising when the Lewis acid - base interaction is considered because strong titanium - nickel acid - base interactions



Figure 6.5 (a) Zr-Zr distances within and between layers of face-sharing trigonal antiprisms. (b) two edge-sharing silicon-centered icosahedra, which lie between the zirconium layers in (a).

Zr(1) -	O(2)	2.22(4) x 1	<b>Zr(2)</b> -	O(1)	2.2179(6) x 2
	O(1)	2.340(1) x 1		O(2)	2.35(4) x
	Ni(1)	2.784(2) x 2		Ni(1)	2.698(2) x 1
	Ni(2)	2.860(1) x 2		Ni(2)	2.754(2) x 1
	Ni(2)	2.871(2) x 2		Ni(1)	2.891(2) x 2
	Si	3.001(6) x 1		Si	2.903(6) x 1
	Si	3.011(2) x 1		Ti(2)	3.017(2) x 1
	Zr(1)	3.128(3) x 1		Zr(1)	3.128(2) x 2
	Zr(2)	3.128(2) x 2		Zr(2)	3.129(3) x 2
	Zr(1)	3.140(3) x 2		Zr(2)	3.144(2) x 2
	Zr(2)	3.317(2) x 2		Zr(1)	3.317(2) x 2
Ni(1) -	Ti(2)	2.436(2) x 1	Ni(2) -	Si	2.345(2) x 1
	Ti(1)	2.496(2) x 1		<b>Ti(1)</b>	2.525(2) x l
	Ni(2)	2.551(3) x 1		Ni(1)	2.551(3) x 1
	Ni(2)	2.588(2) x 2		Ni(1)	2.588(2) x 2
	Zr(2)	2.698(2) x 1		Ni(2)	2.671(2) x 2
	Zr(1)	2.784(2) x 2		Zr(2)	2.754(2) x 1
	Ni(1)	2.803(3) x 2		Zr(1)	2.860(1) x 2
	Zr(2)	2.891(2) x 2		<b>Zr(1)</b>	2.871(2) x 2
	O(2)	3.27(4) x 1			
	O(1)	3.386(1) x 2			
Гi(1) -	Ni(1)	2.496(2) x 6	Ti(2) -	Ni(1)	2.436(2) x 6
	Ni(2)	2.525(2) x 6		Zr(2)	3.017(2) x 6
Si -	Ni(2)	2.345(2) x 3	O(1) -	Zr(2)	2.2179(6) x 4
	Zr(2)	2.903(6) x 3		Zr(1)	2.340(1) x 2
	Zr(1)	3.001(6) x 3		O(2)	2.52(2) x 2
	Zr(1)	3.011(2) x 3		Ni(1)	3.386(1) x 4
			O(2) -	Zr(1)	2.22(4) x 3
				Zr(2)	2.35(4) x 3
				O(1)	2.52(2) x 3
				Ni(1)	3.27(4) x 3

Table 6.4 Interatomic distances in  $Zr_6Ni_6TiSiO_x$  (Å) (distances less than 3.6 Å listed)

are expected rather than strong nickel - nickel interactions, which were minimal in the results of the extended Hückel calculations of overlap populations for  $Zr_4Ni_2O$ . The titanium - nickel interactions in this case are certainly more important than the nickel - nickel interactions.

The projection in Figure 6.3 shows a  $Ni_{12}$  icosahedron sharing six vertices with six very distorted silicon-centered icosahedra. The distortion is seen in the very short Si-Ni distances (2.34 Å), compared with the Si-Zr distances (2.90-3.01 Å). These silicon-centered icosahedra form a network of edge-sharing icosahedra. Figure 6.5 (b) shows how two of these icosahedra share edges. Figure 6.5 (a) shows the location of the silicon between the layers of zirconium antiprisms. The trigonal antiprisms and icosahedra share faces. Thus, the structure consists of a metal framework of zirconium trigonal antiprisms and nickel icosahedra which arrange in this three-dimensional network. Titanium and silicon fill the icosahedral sites, and oxygen occupies trigonal antiprismatic sites.

The crystal structure refinement yields the atomic ratios Ni/Zr/Ti/Si of 6/5.4/1.7/0.9, to be compared with the idealized atomic ratios of 6/6/1/1. A small piece of the sample from which the crystal was extracted was studied by both EDS and XPS techniques. Surface analysis on a sample which was ion-beam etched in an argon atmosphere gave ratios of 6/5.8/1.6/0.5. Semiquantitative elemental analysis by EDS on a rough surface also resulted in a Ni/Zr ratio greater than one, with excess titanium, supporting the conclusion that titanium substitutes on the zirconium sites. The EDS experiment did not, however, indicate a deficiency in silicon. A bulk sample prepared with starting stoichiometry  $Zr_6Ni_6TiSiO_2$ , and containing  $ZrO_2$  as a minor phase, had lattice parameters a = b =8.334(2) Å and c = 7.483(2) Å. This lattice expansion from that reported for the sample from which the single crystal was selected is expected if less titanium substitutes for zirconium on the Zr(2) site, and suggests that there is a homogeneity range for this phase. The structure was not observed when nickel was substituted by iron or cobalt. The sample was checked for superconductivity, but none was detected down to 6 K. Magnetic measurements from 6-297 K show the sample is paramagnetic. A correction was applied for the diamagnetism of the core electrons, and an approximately 5% impurity phase of  $ZrO_2$  [111] (Figure 6.6). See also Figure 4.7.

# Discussion

This new structure may usefully be compared to the kappa phases [94]. Kappa phases crystallize in the hexagonal space group P6<sub>3</sub>/mmc. This new phase crystallizes in the trigonal space group  $P\overline{3}m1$ . Figure 6.7 compares the metal framework in the structures of these two phases, viewed perpendicular to the [ $\overline{1}10$ ] direction. The oxygen atoms are omitted in this figure. Figure 6.7 (a) is similar to Figure 6.5, showing the icosahedral coordination of silicon (B) between the two layers of zirconium trigonal antiprisms (A). Figure 6.7 (b) is a view of the kappa phase which also contains parallel layers of trigonal antiprisms made up of metal atom M at the top and bottom of the figure (A). A horizontal mirror plane contains the interstitial atom, X, and one face of the trigonal antiprism. It can be noticed that the parallel layers are connected by a middle "antiparallel" layer (A'). The interstitial atom has a tricapped trigonal-prismatic coordination. The new structure can be pictured as a modified kappa phase, where the distortion consists of expanding one trigonal face of the trigonal prism, as indicated by the arrows in Figure 6.7 (b), and moving the atoms to a position corresponding to the Ni atoms in Figure 6.7 (a). The interstitial atom then moves into this expanded region. A compression along the c-axis completes the distortion (a value of c/a=0.97-0.99 is typical for the kappa phases, compared to c/a=0.90 for the new structure).

The kappa phases are an intriguing class of compounds, in which the metal framework provides a host to many different interstitial elements. The general formula for the kappa-phase is  $M_9M'_4X$ , where X = B, C, Si, Ge, P, As, S, Se, Fe, Co, or Ni. Apparently, the strength of the


Figure 6.6 Magnetic susceptibility of  $Zr_6Ni_6TiSiO_{1.8}$ . The bump below 50 K is attributed to atmospheric oxygen.



metal-metal interactions in the framework allows for the variability in X. A similar argument suggests that this new phase might also form with a variety of interstitial elements. The kappa phase and the new phase both have a metal/non-metal ratio of 13/1, neglecting the oxygen. The difference between the two phases is the metal framework. The kappa phase contains two transition metals, while this new phase has a ternary framework with two early transition metals and a late transition metal.

It is very likely that this new phase will also accomodate a variety of interstitial atoms in the icosahedral site occupied by silicon. A tabulation of preferred coordination number for main group, and iron group transition metal elements, based on the results of the structural determination of compounds in 324 structure types, indicates gallium and aluminum prefer a twelve coordinated site over a coordination number of nine [109]. Many of the elements which are found in the tricapped trigonal prismatic interstitial site of the kappa phase, including B, Ge, As, Si, and P prefer a coordination number of nine. While this does not preclude the possibility of these elements forming in this new structure type (as in the case of silicon), it certainly gives an indication of what might be expected in attempts to synthesize new compounds of this structure type.

#### 7. IDEAS FOR FUTURE WORK

#### Cubic Laves Phase: Zr/Ni/O

Reference has been made throughout of the existence of an interstitially stabilized cubic Laves phase in the zirconium - nickel system. Very little is actually reported for this phase, and as these phases appeared in the course of this research, a few comments are appropriate. The Laves phase is not known in the binary system. It was initially reported as a cubic ZrNi<sub>2</sub> [48], but was subsequently shown to form only when stabilized by an interstitial atom. Bsenko suggested it was stabilized by silicon [112]. Blažina and Ban report cubic ZrNi<sub>5</sub> can substitute oxygen for nickel, forming  $ZrNi_{5-x}O_x$ , for x = 0 to 1 [113]. ZrNi<sub>5</sub> crystallizes in the AuBe<sub>5</sub> type structure, which is related to the  $MgCu_2$  structure by a group/subgroup relationship. The atoms in  $MgCu_2$  both occupy special positions, 8a and 16d in Fd3m. In the AuBe<sub>5</sub> structure the eight fold site is split into two four fold sites, with a lowering in symmetry to  $F\overline{43}m$ . In the Laves phase  $AB_2$ , the larger A atoms are sixteen coordinated. The smaller B atoms are coordinated to twelve atoms. Because of the change in symmetry, the AuBe<sub>5</sub> type structure splits the A atoms position of the Laves phase, and the large sixteen coordinated sites are occupied by both A and B atoms. The solution of Blažina and Ban places zirconium and oxygen on these large four fold sites. This is a very large site for an oxygen atom. Their work was based on powder diffraction data, without full profile refinement, and should be checked. A solution to this may also help to understand the structure of the Laves phase. The lattice parameter for  $ZrNi_4O$  is a = 6.680(5) Å. The lattice parameter of a cubic phase observed in the course of this work is a = 6.9158(4) Å.

The cubic phase was present in a sample also containing  $Ni_{10}Zr_7$ . This sample was examined by EDS, and identified as  $Zr_{26}Ni_{70}O_4$ . This corresponds to a formula  $ZrNi_{3-x}O_x$ , with x = 0.3. This is written assuming oxygen substitutes for nickel, not for zirconium. Clearly, the

difference in lattice parameters between those reported by Blažina and Ban and those reported here indicate more than just a range of oxygen substitution. This Zr/Ni ratio falls between the 1/2 ratio for a Laves phase and the 1/4 or 1/5 ratio for the AuBe<sub>5</sub> type. The Laves phases are tetrahedral close packed structures. The interstitial tetrahedral sites are too small for oxygen atoms, so substitution of oxygen on metal sites is assumed. No silicon was detected, so although it may also stabilize this cubic phase, it is not necessary. A single phase sample was prepared, and the magnetic measurements were taken (see Figure 4.7). A single crystal suitable for diffraction study was not found.

#### Hexagonal Laves Phase: Zr/Ti/Ni

The reports for the  $MgZn_2$  type structure in the ternary Zr/Ti/Ni system are also incomplete. There are no Laves phases known in any of the binary systems, Zr/Ti, Zr/Ni, or Ti/Ni. It would be interesting to find this phase in a ternary system. There is indication that the hexagonal phase exists over a large region of homogeneity. One report gives the range of zirconium present as 21 to 30 atomic percent [106]. A 700°C isotherm of the Zr/Ti/Ni system shows the MgZn<sub>2</sub> phase extending from 14-34 atomic % Zr, 27-38 atomic % Ni, and 33-59 atomic % Ti [114].

This phase appeared in a sample which melted at 950°C, and contained a mixture of the MgZn<sub>2</sub> type phase and the filled  $Ti_2Ni$  type phase. EDS measurements gave the stoichiometry of this hexagonal phase as  $Zr_{26}Ti_{32}Ni_{34}O_8$ . A single crystal was picked from this mixture. The results are given below. Structure factor amplitudes, including unobserved reflections, are included in the appendix. The stoichiometry from the refinement is much different from that given by EDS, and those given from previous studies.

It is interesting to observe titanium substituting for nickel, in light of the results given for new filled  $Ti_2Ni$  phases, and  $Zr_6Ni_6TiSiO_{1.8}$ , where titanium substituted for zirconium atoms. The

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Formula	ZrNi <sub>1.45</sub> Ti <sub>0.55</sub>
Space group	P6 <sub>3</sub> /mmc (#194)
a (Å)	5.154(2)
c (Å)	8.376(3)
V (Å <sup>3</sup> )	192.7(1)
Z	4
d <sub>calc</sub> (g/cm <sup>3</sup> )	7.06
μ (ΜοΚα) (cm <sup>-1</sup> )	214.06
Data collection instrument	Rigaku AFC6R
Radiation (monochromated in incident beam)	ΜοΚα (λ=0.71069)
Octants measured	±h,±k,l
No. reflections measured	1240
No. unique data, total with $F_o^2 > 3\sigma(F_o^2)$	142
No. parameters refined	12
Trans. factors, max/min	1.00/0.88
R <sup>a</sup> , R <sub>w</sub> <sup>b</sup> , GOF <sup>c</sup>	0.028, 0.034, 1.03
Largest difference peak (e/Å <sup>3</sup> )	1.17
Largest negative peak (e/Å <sup>3</sup> )	-1.44

Table 7.1 Crystal data for hexagonal Laves phase

<sup>a</sup>  $\mathbf{R} = \Sigma ||F_0| - |F_c|| / \Sigma |F_0|$ 

<sup>b</sup>  $R_w = [\Sigma w (|F_o| - |F_c|)^2 / \Sigma w |F_o|^2]^{1/2}; w = 1/\sigma^2 (|F_o|)$ 

<sup>c</sup> GOF = ( $\Sigma(|F_o|-|F_c|)/\sigma_i$ )/ (N<sub>obs refl</sub>- N<sub>parameters</sub>)

Atom	x	у	Z	$B_{eq}(A^2)^a$	% Occupancy
Zr	0.3333	0.6667	0.0670(2)	0.99(5)	100
Ni1 Ti1	0	0	0	1.0(1)	55(5) 45
Ni2 Ti2	0.8288(3)	0.6575	1/4	0.9(1)	80(5) 20

Table 7.2 Atomic parameters for hexagonal Laves phase

<sup>a</sup>  $B_{eq} = 8\pi^2/3 \Sigma_1^3 \Sigma_1^3 U_{ij} a_i^* a_j^* \overline{a}_i^* \overline{a}_j^*$ 

,

Table 7.3 Anisotropic thermal parameters for hexagonal Laves phase

Atom	U <sub>11</sub>	U <sub>22</sub>	U <sub>33</sub>	U <sub>12</sub>	U <sub>13</sub>	U <sub>23</sub>
Zr	0.0134(7)	0.0134	0.011(1)	0.007	0	0
Nil Til	0.012(1)	0.012	0.014(2)	0.006	0	0
Ni2 Ti2	0.0112(9)	0.013(1)	0.012(1)	0.007	0	0

Table 7.4 Interatomic distances less than 3.6Å

Zr -	Ni2	2.9987(9)	хб	Ni2 -	Ni2	2.506(1) x 2
		3.0240(9)	x 3		Nil	2.5926(7) x 2
	Ni1	3.028(1)	x 3		Ni2	2.648(1) x 2
	Zr	3.065(1)	x 1		Zr	2.9987(9) x 4
		3.181(1)	x 3			3.0240(9) x 2
Ni1 -	Ni2	2.5926(7)	хб			
	Zr	3.028(1)	хб			

two factors most frequently used in explaining the Laves phases are the relative sizes of the atoms, and the electron concentration. By size considerations, the titanium might be too small for the large sixteen coordinated site occupied by zirconium. The short titanium - nickel distances seen in this refinement are seen also in the filled  $Ti_2Ni$  type phases and  $Zr_6Ni_6TiSiO_{1.8}$ . Size considerations favor titanium substitution of nickel. By electron concentration considerations for transition metals which form the MgZn<sub>2</sub> phase,  $ZrNi_{2-x}Ti_x$  would be favored for x ranging from 0.67 to 1.56 [115], assuming there is no substitution on zirconium. Clearly, many details remain unknown.

### New Phase in Zr/W/Ni/O System

In trying to prepare a kappa phase of stoichiometry  $Zr_9W_4NiO$ , a sample was arc-melted and annealed at 1160°C for 10 hours. The powder pattern of the annealed sample contained lines identified as unreacted tungsten, and  $W_2Zr$ , and several more lines for another phase which has not been identified. The powder data is given below. The phase has a distinctive set of low angle lines not observed in any of the phases described previously. EDS measurements indicate titanium is present also.

### New Phase in Zr/Ni/S System

Little work was actually performed in the sulfide system. Very likely, new and novel phases will be found in this ternary system. The results of this research show that even very small amounts of oxygen will favor formation of the new oxide phases. Therefore, work in the sulfide system will require great care in excluding all sources of oxygen throughout the synthetic process. As noted previously, the samples studied in this research were routinely handled in air. Thus, it may be necessary to eliminate steps like the arc-melting procedure, where the sample is momentarily exposed to air before and after melting, in favor of melting the samples in sealed metal tubes.

20	d	I/I <sub>o</sub>	20	d	I/I <sub>o</sub>
8.770	10.075	26.6	41.574	2.170	1.6
8.950	9.872	15.4	42.224	2.139	6.2
12.235	7.228	2.5	42.824	2.110	5.9
12.655	6.990	11.2	43.980	2.057	1.3
15.196	5.826	2.6	45.189	2.005	4.2
15.526	5.703	2.7	45.489	1.992	1.1
17.712	5.004	2.2	45.824	1.979	7.1
19.496	4.550	2.4	47.742 <sup>a</sup>	1.904	18.1
20.188 <sup>a</sup>	4.395	25.6	48.220	1.886	3.6
21.033	4.220	1.6	48.569	1.873	1.0
23.774	3.740	3.4	50.240	1.814	0.7
25.519	3.48	1.2	50.461	1.807	1.1
29.905	2.986	0.8	<b>52.390<sup>a</sup></b>	1.745	12.6
32.728	2.734	7.4	54.183	1.691	1.4
32.936	2.717	3.0	54.869	1.672	2.2
33.268 <sup>a</sup>	2.691	11.1	56.578	1.625	1.8
34.194	2.620	2.6	57.031	1.614	1.8
35.195	2.548	17.3	58.239 <sup>b</sup>	1.583	22.1
35.390	2.534	1.0	58.497	1.576	2.6
35.771	2.508	2.7	59.417 <sup>a</sup>	1.554	3.6
36.162	2.482	61.8	60.739	1.524	6.8
36.724	2.445	58.0	60.964	1.518	1.9
37.001	2.428	34.4	62.877	1.477	5.4
37.205	2.415	20.1	63.441 <sup>a</sup>	1.465	44.5
37.282	2.410	13.0	64.623	1.441	9.5
37.447	2.400	11.0	66.037	1.414	48.2
37.787	2.379	15.2	66.918	1.397	3.7
38.674	2.326	36.0	67.343	1.389	11.2
38.909	2.313	39.6	67.583	1.385	3.6
39.223 <sup>a</sup>	2.295	72.7	68.845	1.363	1.3
39.671	2.270	81.7	69.807 <sup>a</sup>	1.346	32.5
40.275 <sup>b</sup>	2.238	100.0			
41.042 <sup>a</sup>	2.197	41.5			

Table 7.5 Powder data for Zr/W/Ni/O sample

<sup>a</sup> W<sub>2</sub>Zr <sup>b</sup> W

## Vaporization Study of Nb<sub>4</sub>Ni<sub>2</sub>O

A sample of Nb<sub>4</sub>Ni<sub>2</sub>O was annealed at 1350°C for 8 hours, then 1100°C for 1 hour, and quenched. The sample showed the two phases Nb<sub>4</sub>Ni<sub>2</sub>O (a = 11.5917(5) Å) and Nb<sub>6</sub>Ni<sub>6</sub>O (a = 11.2344(7) Å), as well as NbO, which was also present as a minor phase in the initial sample. The quartz jacket had black vapor deposited film, probably nickel. It would be worthwhile to study the thermodynamics of the decomposition of Nb<sub>4</sub>Ni<sub>2</sub>O at high temperatures. The relation between these two phases may reveal much more about the filled Ti<sub>2</sub>Ni structures in general.

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# OBSERVED AND CALCULATED STRUCTURE FACTOR AMPLITUDES

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# Observed and calculated structure factor amplitudes (x10) for $Zr_3NiO$

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13	1	1837	1828	38	~~~~	~~~	n =	8			~~~	1.	14 000	~~~~
					•	10	050	0.07	20			n =	14	
~~~^	^ ^ ^	h =	4 ^ ^ ^	~~~~	0	14	958	1022	29	2	2	1071	1070	17
					4	8	3933	2766	66	2	2 /	1566	1580	37
0	- 4	5558	5520	85	8	10	2210	2307	50	2 A	4	500	550	55
2	4	1593	1575	32	8	12	2284	2305	52	4	- 4 - 7	1060	10/1	20
4	4	3172	3165	56		~~~	1.	0	~~~~	0	4	2212	7777	11
4	10	629	670	67	,		n =	9		0	4	6346	2212	-1-1
6	2	762	757	21	1	r	1627	1500	22					
6	10	2491	2456	42	r	5	102/	1287	22					

# Observed and calculated structure factor amplitudes (X5) for $\rm Zr_4Ni_2O$

k	1	Fo	FC	sig	7 k	1	Fo	FC	sig	r k	1	Fo	FC	sigF
^^^^	~~~	h =	0 ^^^	~~~~	^^^^	~~~	h =	5 ^^^	~~~~					:
0 4 8 10 16 16 16	12 4 0 6 0 4 8	1933 2603 868 1313 1345 933 650	1921 2590 780 1320 1448 901 688	82 42 27 29 40 33 80	5 5 7 9 11 11	3 5 15 7 9 5 13	708 2933 654 689 683 1125 558	694 2972 659 747 667 1107 553	66 57 53 36 42 70 88	2 2 4 10 14	0 2 10 4 0 0	$1252 \\ 1143 \\ 897 \\ 554 \\ 1723 \\ 676 \\ h = 1$	1213 1164 843 540 1780 645 11 ^^^	30 33 85 38 46 72
~~~~	~~~	h =	1	~~~	~~~~	~~~	h =	6 ^^^	~~~	1	1	653	659	39
1 5 11 15	7 1 5 7 5	827 2976 883 966 670	861 2979 892 949 683	45 47 41 29 72	6 6 10 10 12 16	0 2 2 4 6 6	3627 501 373 1297 1275 752	3693 496 320 1308 1285 727	58 38 58 29 59 86	5 5 11 11	1 3 1 5	$ \begin{array}{r} 1485 \\ 401 \\ 534 \\ 545 \\ 1307 \\ h =  \end{array} $	1471 400 542 435 1311	34 60 45 56 39
~~~~	~~~	h =	2 ^^^/	~~~~		~~~	h =	7 ~~~		0	12	1015	990	67
2 2 4 4	8 14 2 6	2509 725 2010 395	2556 697 2059 397	43 53 35 54	3 3 3	3 5 7	1410 684 1034	1375 712 1055	34 28 30	2 4	20	$911 \\ 445 \\ h = 1$	905 483 13 ^^^	33 48
4 6 10 12	16 2 8 6	450 685 717 572	390 675 681 563	65 26 55 37	3 5 7 9	13 5 1 7	1079 1380 1059 801	1086 1354 1048 755	27 37 32 66	5 9	1 3	450 673	413 673	51 55
16	6	546	508	52	13 13	5 7	558 852	519 833	46 78	~~~	~~~~	h =	14 ^^^	~~~~
^^^^	^^^	h =	3 ^^^	~~~~		•••	h =	8 000		2	4 8	775 1215	748 1191	31 29
1 3 3 3 3 3	7 13 1 3 9 13 15	690 971 1020 3636 2259 901 962	724 932 989 3489 2260 871 991	21 26 32 60 42 36 99	4 6 8 12	8 2 8 12 0	1860 547 1600 1014 759	1831 585 1651 1082 728	42 43 70 39 31	_				
^^^^	^^^	h =	4 ^^^	~~~~	1			613	55					
0 2 4 6 8 10 12	0 4 6 2 4 12	1038 1169 554 557 783 714 567	1029 1197 576 557 818 697 553	28 43 50 53 23 35 61	5 7 7 9 9	5 1 3 13 9	502 549 387 582 1060 773 h =	509 516 381 538 1078 849	48 31 46 45 32 76					

Observed and calculated structure factor amplitudes (X3) for  $Zr_6Ni_4Ti_2O_{0.6}$ 

.

Observed and calculated structure factor amplitudes (X5) for  $Nb_6Ni_6O$ 

k	1	Fo	Fc	sigF	r k	1	Fo	FC	sigB	r k	1	Fo	Fc	sigF
	^^	h =	0		2 6	2 0	1612 5443	1593 5401	37 84	8 8	2 6	879 936	903 947	34 35
4 8	0 0	2268 2050	2361 2043	39 43	6	26	1233	1201	36 61 28	10	0	3553	3573	64
~~~~~	^^	h =	1	~~~~	8	6	1214	1217	36	7	1	n =	11	21
1 5	1 1	678 5359	580 5341 811	33 82 43	10	6	758	825	53	3 5 5 0	1 3 5	503 1881 817	533 1955	63 52 89
TT	~~ T	0. 1.	2 0011	4J	1	1		7 7 6 4		~~~~	••••	1	12 002	~~~~
		Ω =	4		5	1	404	352	57			11 =	12	
2 4	2 2	513 3175	490 3216	60 51	5 7	5 1	1974 2774	1984 2752	45 70	0 2	0 2	2642 2531	2622	53 52
6	Õ	458	366	35	7	3	2221	2254	47	4	4	620	546	96
10	2	2480	2440	41	7	5 7	1491	1477	45 62	0	4	2120	2131	44
14 14	0 2	1036 1525	$1061 \\ 1561$	34 56	9 11	7	1562 1185	1547 1191	41 44	~~~~	~~~	h =	13 ^^^	~~~~
	~~	1.	2 000	~~~~	$\overline{11}$	3	1600	1642	35	3	3	1162	1117	41
		n =	3		^^^^	~~~	h =	8 ^^^	~~~~					
3	1	1621	1708	34	-	-								
3	3	5230	5240	83	2	2	4402	4378	70					
57	1	1203	480	43	4 Ω	2 0	1024	1400 933	33 45					
7	1	2668	2697	48	о 8	2	1113	1127	37					
á	ĩ	3456	3464	59	ă	4	2733	2772	53					
13	1	1675	1656	46	ă	8	2256	2241	78					
10	~	2010	2000		10	4	1066	1072	32					
~~~~~	^ ^	h =	4 ^^^	~~~~	12	0	2028	2073	45					
4	0	5833	5926	92	~~~~	~~~	h =	9	~~~~					
4	2	2168	2119	52	-									
12	0	790	773	36	3	1	1200	1192	29 38					
~~~~~	^^	h =	5 ^^^	~~~^	Š	3	832	815	35					
					7	1	1059	1005	29					
3	3	1145	1123	61	7	5	715	711	98					
5	1	1565	1556	39	9	· 1	979	987	42					
5	3	1652	1666	61	9	3	895	2267	54					
5	5	35/0	1636	92	9	þ	2213	2201	23					
ó	5	1/5/	1458	41	~~~~	~~~	h =	10 000	~~~~					
11	1	2095	2037	41				_ •						
13	ī	858	948	70	4	2	594	542	71					
~~	-				4	4	1321	1349	49					
~~~~~	^^	h =	6 ^^^	~~~~	6	2	827	786	33					
					6	4	2403	2415	44					

$\begin{array}{cccccccccccccccccccccccccccccccccccc$	k	1	1	Fo		Fc	sigF	r k	1	Fo		FC	sigF	r k	1		Fo	FC	sigF
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	^^^^	••••	h :	=	0	100	1.2	-4 4	04	1415 822	-	809	50 60	-9 -9	-9 -7		615 316 412	578 328	23 17
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	6	10	i	653		657	15	4	14	187		166	29	-9 -9 -7	-1 -5		216	195 217	22
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	~~~~	~~~	h :	=	1	~~~~	~~~	~~~~	~~~~	h =	5	~~~/	~~~~	-7	-5 5 3		360	364	8 10
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	-15 -11	-5 -3		431 226		429 231	9 13	-7 -7	-13 -3	349 462		350 460	9 9	9	5		327	335	14
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	-7 -5	-1 -3		173 301		165 297	12 9	~5 -5	-11 -7	724 375		712 376	21 14	~~~/	~~~~	h	= 10	~~~/	~~~~
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	-3 -3	-13 -3	1	530 686		542 694	10 26	-5 -1	-3 -5	454 232		439 246	13 20	-10 -10	-6 -4		422 304	414 335	15 15
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	-1	-11		506		526 150	14 9	1 5	7	358 1365	1	360 1336	12 95	-8 -4	-6 -6		176 487	182 483	27 9
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3	9 15	4	244	,	225	17 14	5 11	13	476		251 470	10	-4	-4 -10		278 670 228	201 675 207	15 21
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	9	1	1	206	1	213	18	~~~	~~~	h =	6	~~~	~~~	6	10		476	465	20
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	^^^^	~~~	h :	=	2	~~~~	~~~	-6 -2	-6 -14	544 374		559 380	35 10	~~~~	~~~	h	= 11	~~~	~~~
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	-10 -8	0 -10		417 349		435 353	14 10	2 6	10 0	487 1512		479 1529	9 60	-11 -9	-3 -3		253 159	250 145	14 24
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	-8 -6	-2 -6	1	100 637	1	.086	30 22	~~~	~~~~	h =	7	~~~/	~~~	-3 -1	-3 -7		181 573	172 587	18 11
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	-4 -2	-8 -14		309 587		299 587	18	-7	-7	265		241	18	5	••••	հ	332 - 12	330	8
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	-2 -2 -2	-4 -2	1	871 439		866	20 32 25	-7 -5	-1 -7	539		533 512	16 12	-8	-4		239	232	11
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0 2	-2 12		134 333		34 327	17 10	-1 3	-9 3	402 798		405 796	9 26	0 0	-8 0		568 509	572 534	11 22
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4 10	4 2	4	441 857		434 847	21 22	9 11	73	445 311		451 326	11 8	6	6		683	689	15
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	^^^^	~~~	h :	-	3	~~~~	~~~	13	3	595	•	598	12	~~~~		h	= 13	402	10
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	-5	-3	1	237	,	223	12	0	л	n =	8	1202	<b>7</b> 1	-1 -1	-9 -7		493 211 283	403 200 278	15 12
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3	9	1	188	1	.173	36	-8 -2	-2	206	-	221	16	~~~/	~~~~	h	= 14	~~~~	~~~~
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	^^^^	~~~	h :	=	4	~~~	~~~~	0 0	-8 0	319 763		332 795	16 49	-2	-8	- •	625	622	12
-8 -10  205  212  19	-14 -12	-2 0		441 636		433 645	11 13	4 8	0 8	474 475		495 468	12 29	~~~~	~~~~	h	= 15	~~~~	~~~~
-0 $-0$ $203$ $200$ IU = 9 $037$ $037$ $134$	-8 -6	-10		205		212	19 10	~~~	~~~~	h =	9	~~~	~~~^	3	3		637	634	14
-6 -2 128 130 17 -4 -12 388 385 12 -11 -1 327 322 9 ^^^^^ h = 16 ^^^^^	-6 -4	-2 -12		388		385	12	-11	-1	327		322	9	^^^/	••••	h	= 16	1011	10

Observed and calculated structure factor amplitudes (X1) for  $Nb_6Ni_4Ta_2O_2$ 

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Observed and calculated structure factor amplitudes (x10) for  $Zr_9W_4(S/Ni)O_3$ 

k	1	Fo	FC	sigr	k	1	Fo	Fc	sigF	k	1	Fo	Fe	sigF
~ ^ ^ ^	• • •	h =	0	****	-4	2	2250	2232	93	Q	5	1912	1934	64
0	2	1571	1460	0	-2	~7	2479	2461	53	1	-3	944	901	64
ŏ	Ã	7364	- 7305	ŏ	ŏ	-10	1325	1274	43	2	-4	2048	2092	43
0	6	4407	4346	80 '	Ŏ	-4	1522	1521	34	-	•			
0	8	2632	2653	79	0	~1	1225	1220	37	~ ~ ~ ^	~ ~ ~ ~	h =	5 ^ ^ ^	~ ~ ~ ~
ĭ	-5	771	652	67	1	~2	4259	4222	49	-10	-2	1629	1617	53
2	3	3842	3839	61	ĩ	ō	1066	1094	40	-ĨŎ	õ	2794	2599	õ
2	9	1032	1066	65	1	6	1641	1632	36	-10	4	1174	1190	0
1	-9	2054	2578	59	2 3	-4	1306	1842	46	-9	2	1697	1672	40
3	-1	4000	5130	õ	3	8	1957	1987	42	-7	1	767	689	58
3	4	1263	1232	33	5	-8	1298	1350	58	-6	- 3	2213	2302	47
4	-2	2272	2343	48	57	6 	989	941	64 03	-6	-1	1210	1186	38
6	-7	1762	1829	59	'	-5	1133	1104	33	-6	9	960	978	52
6	-6	2188	2186	60		• • • •	h =	3 ^ ^ ^	~ ~ ~ ^	-5	Ō	1035	1851	6Õ
6	-5	3503	3507	64	1.0	1	1464	1476	4.7	-5	8	2004	2028	46
9	-4	1915	1844	64	-10	0	977	960	43	1	-0	741	. 1155	48 61
•	-			•••	-9	5	2035	2088	5 Ž	2	-7	749	705	99
~ ^ ^ ^	~ ~ ^	h =	1	~ ~ ~ ~	-8	-3	2194	2220	46	2	- 5	1480	1472	39
~ 0	_ 1	746	570	n G	-8	~1	683	627 1214	75	2	4	743	708	75
~9	0	956	1016	Ő	-8	7	1644	1623	42	~ ~ ~ ~ /	• • • •	h =	6 ^ ^ ^	~ ~ ~ ~
~8	4	1060	1039	93	-7	Ó	3443	3441	65					
~7	2	1432	1449	40	-7	4	2218	2287	47	-10	1	1463	1394	42
~7		820	805	73	-7	8	984	4720	05	-10	_1	2367	2330	45
~5	6	662	736	82	-6	8	2659	2643	72	-9	3	2242	2207	49
-4	3	1775	1794	38	-5	5	770	664	49	-9	- 4	653	504	85
-4	6	1401	1399	35	-5	0	596	557	86	-7	-1	1029	979	62
~ 3	0	905	684	45 '		2	1836	1902	49 :30	-1	- 3	2020	2072	51
-2	ă	1084	1108	41	-4	2	952	951	33	6	-2	2406	2430	55
-2	6	909	936	55	-4	7	1382	1369	50	-6	1	3356	3394	62
-2	8	1315	1307	51	-4	8	854	778	60	1	-6	1631	1660	40
-1	0	2451	2468	64	-3	ō	2595	2656	50	3	-0	1390	1404	44
-1	8	1907	1895	44	- 3	10	2534	2536	55	•	-	2320		••
Û	-7	1190	1162	45	0	-7	1985	1944	50	~ ~ ~ ~ ~	• • • •	h =	7 ^ ^ ^	~ ~ ~ ^
0	- 5	2028	1909	41 78	0	-3	2186	2193	64	-9	-1	1332	1332	46
ĭ	-10	875	881	Ő	ĩ	-5	1594	1576	34	-9	3	1349	1306	46
2	-10	774	775	61	2	-9	616	604	0	-9	6	786	632	83
3	-10	1247	1218	55	2	-1	2066	1/53	40	-7	~2	1033	1001	76
- 4	-8	822	884	0	3	ŏ	6488	6394	Ő	-7	ĭ	1850	1750	45
5	-7	1698	1694	. 5 2	, 3	2	2051	2077	67	-7	6	1601	1720	45
5	8	890	877	66	6	2	1610	1625	50	0	5	2409	2365	64
7		1997	1930	73		• • • •	h =	4 ~~~	~ ~ ~ ~	1	- 2	1323	1471	04
	-				_	-				~ ~ ^ ^	~ ~ ^ ^	h =	0 ^^^	~ ~ ~ ~
		h =	2	~ ~ ~ ~	9	3	1168	1178	79	10	-	0.2.2	0.00	0
-9	-2	1775	1820	42	-8	4	1027	1071	76	-10 -A	ر ۲_	2014	2034	49
-9	õ	1227	1201	62	-7	6	911	898	52	1	-4	1174	1214	60
-8	0	869	748	78	-6	8	2044	2053	53					
-8 _n	2	2875	2914	73	- 5	-10	998	978	41	~ ~ ~ ~		h =	9 ~ ~ ^	
-6	Ő	2026	1906	82	-4	-9	657	782	ŏ	-10	0	1759	1664	60
-5	3	2639	2629	48	-4	-6	2015	2001	46	-9	Ő	2977	3018	0
-4	0	3678	3548	95	-4	-1	1449	1474	31	0	-4	2776	2858	0

Observed and calculated structure factor and	mplitudes (x5) for	Zr <sub>6</sub> Ni <sub>6</sub> TiSiO <sub>1.8</sub>
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$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	k	1	Fo	FC	sigE	r k	1	Fo		FC	sigl	Fk	1	Fo	FC	sigF
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	^^^^	~~~	h =	0 ^^^	~~~~	7	-6	91		31	77*	0	-1	117	89	36
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$						7	-5	255		265	39	Ő	õ	161	166	7
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0	1	183	167	16	7	-4	294		291	23	0	4	531	522	18
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0	2	168	148	35	8	-6	574		581	19	0	5	0	2	67*
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0	3	786	789	22	8	-5	322		301	75	0	8	438	433	26
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0	4	616	638	27	9	-3	263		303	34	1	-8	352	324	33
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0	5	534	509	24	9	1	234		24	56	1	-3	0	37	47*
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0	5	804	817	31	10	-1	273		244	53	1	2	0	27	44
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0	0	190	104	94"	~~~~	~~~	1	1	~~~	~~~~	2	9	241	260	10*
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0 n	o o	000	31	20 0*			11 =	т			2	-4	241	300	C0*
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	ň	10	0	73	ŏ*	- 9	- 1	273		273	1 Ω	2	-0	153	155	46
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	ĭ	-6	513	506	21	- q	, ,	394		377	15	2	-2	179	103	19
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	ĩ	-3	1159	1164	20	-9	4	309		302	23	4	-6	240	260	28
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	ī	-2	177	196	28	-8	i	253		215	31	4	-5	207	204	25
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1	-1	81	3	34	-8	4	183		173	42	5	-7	461	460	12
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1	5	583	590	16	-8	5	271		280	37	5	-6	330	321	28
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1	6	117	29	70*	-8	6	0		47	60*	5	-5	232	224	29
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1	10	334	316	56	-7	3	222		258	32	5	-4	394	389	12
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2	-7	0	25	0*	-7	4	133		115	38	5	0	263	261	17
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2	-6	945	920	35	-7	5	186		174	31	5	1	64	50	57*
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2	-4	503	641	10	-7		128		540	50	57	3	151	203	22
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2	10	111	452	22	-6	2	204		281	17	<b>'</b>	Å	120	03	55
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Ĩ.	-10		62	83*	-6	จึ	530		529	12	ต่	-5	120	47	67*
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3	-9	261	276	34	- Ğ	8	164		204	38	ğ	-3	ŏ	50	62*
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Ĵ	-8	382	372	23	-5	-7	0		22	72*					
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3	-6	319	337	28	-5	-1	433		444	10	^^^^	~~~	h =	2 ^^^	~~~~
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3	-3	446	439	13	-5	1	297		285	14					
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3	0	1025	1018	17	-5	4	289		266	14	-10	-3	32	71	68*
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4	-9	0	173	0 *	-4	-4	453		457	11	-10	-2	248	267	38
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4	-8	20	67	77*	-4	4	256		247	14	-10	-1	0	71	65*
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4	-7	229	202	27	-4	9	236		252	30	-10	2	236	224	25
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4	-6	345	362	19	-3	8	410		393	33	-10	4	406	411	17
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4	-3	665	672	23	- 3	10	209		188	55	-9	0	207	105	23
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4	-2	0	1/2	59*	-3	10	206		20	11.	-9	2	210	206	39
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4	0	510	516	20"	_2	1	200		233	0 /0*	-9		012	200	61*
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	с г	_Ω	163	147	51	-2	1	94		23	40*	_9 _9		443	10	15
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	5	-0	179	147	18	-2	ч б	265		235	22	-0	-4	208	306	21
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	5	-3	150	81	45	-2	10	205		55	69*	-7	-1	444	436	19
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	6	-6	10	87	74*	-1	-10	ŏ		46	84*	-7	$\overline{2}$	Ő	26	<u>59</u> *
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Ğ	-5	ŏ	76	71*	-ĩ	-9	100		156	83*	-7	3	ŏ	61	59*
6       -2       557       544       19       -1       3       393       395       12       -6       8       308       299       25         6       0       76       91       58*       -1       .8       217       270       44       -5       3       1185       1179       20         6       1       385       348       16       0       -9       59       65       80*       -5       6       475       486       12         6       3       337       374       18       0       -7       160       128       50       -5       9       173       111       43         6       4       318       328       20       0       -4       332       340       18       -4       1       400       392       17         6       5       856       835       21       0       -2       167       188       65       -4       2       489       492       15	Ġ	-4	693	696	27	-1	-7	0		8	91*	~6	6	431	431	13
6       0       76       91       58*       -1       · 8       217       270       44       -5       3       1185       1179       20         6       1       385       348       16       0       -9       59       65       80*       -5       6       475       486       12         6       3       337       374       18       0       -7       160       128       50       -5       9       173       111       43         6       4       318       328       20       0       -4       332       340       18       -4       1       400       392       17         6       5       856       835       21       0       -2       167       188       65       -4       2       489       492       15	6	-2	557	544	19	-1	3	393		395	12	-6	8	308	299	25
6       1       385       348       16       0       -9       59       65       80*       -5       6       475       486       12         6       3       337       374       18       0       -7       160       128       50       -5       9       173       111       43         6       4       318       328       20       0       -4       332       340       18       -4       1       400       392       17         6       5       856       835       21       0       -2       167       188       65       -4       2       489       492       15	6	0	76	91	58*	-1	· 8	217		270	44	-5	3	1185	1179	20
6  3  337  374  18  0  -7  160  1.28  50  -5  9  173  111  43 6  4  318  328  20  0  -4  332  340  18  -4  1  400  392  17 6  5  856  835  21  0  -2  167  188  65  -4  2  489  492  15	G	1	385	348	16	0	-9	59		65	80*	-5	6	475	486	12
6 = 5 = 956 = 835 - 21 = 0 = -2 = -4 = -4 = -4 = -4 = -4 = -4 = -4	6	3	337	374	1.8	0	-7	160		179	50	-5	9	1/3	302	45
	о Б	4	856	320	21	0	-2	167		188	65	-4	2	489	492	ĩ5

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k	1	Fo	FC	sigF	k	1	Fo	FC	sigF	r k	1	Fo	Fc	sigF	
-4 -4 -3 -3 -3	5 7 -6 -2 -1 2	0 278 99 141 1391 73 353	11 265 105 128 1395 92 368	55* 32 64* 38 22 43* 9	-8 -8 -8 -7 -7 -6	3 4 5 4 6 0 3	75 296 321 0 292 1413 505	134 286 326 89 294 1411 486	59* 16 26 59* 17 23 12	3 4 4 5 7	2 -8 -7 -3 -7 1	524 0 216 329 206 305	515 21 194 316 212 329	12 67* 60 15 35 36	
-3 -2	6 -10	417 451	423	12 22	-5 -5	0 2	130 212	142	22 20	~~~^	~~~	h =	4 ^^^	~~~~	
	-8521569758743210971748742737	$\begin{array}{c} 141\\ 848\\ 530\\ 24\\ 0\\ 601\\ 466\\ 161\\ 138\\ 661\\ 138\\ 661\\ 138\\ 661\\ 2557\\ 460\\ 109\\ 104\\ 5109\\ 104\\ 601\\ 191\\ 5723\\ 200\\ 141\\ 64\end{array}$		7125613344312252261169626215 * * * *	-44443333333332222111111000000	$     \begin{array}{r}       -7 \\       -3 \\       1 \\       3 \\       7 \\       -54 \\       -12 \\       3 \\       5 \\       -53 \\       00 \\       -85 \\       -10 \\       -87 \\       -64 \\       -4 \\      -4 \\       -4 \\       -4 \\      -4 \\      -4 \\      -4 \\  $	$\begin{array}{c} 101\\ 93\\ 555\\ 170\\ 500\\ 124\\ 1016\\ 559\\ 324\\ 292\\ 423\\ 102\\ 330\\ 215\\ 449\\ 286\\ 807\\ 232\\ 429\\ 286\\ 807\\ 232\\ 425\\ 588\\ 1036\\ \end{array}$	62 561 153 484 48 1014 5753 1345 1345 1345 180 323 415 180 323 221 414 120 245 89 148 240 426 910 880 1038	55612162172171512244 * * * * * * * * * * * * * * * * * * *	$\begin{array}{c} -11\\ -11\\ -10\\ -99\\ -99\\ -98\\ -88\\ -77\\ -66\\ -55\\ -44\\ -4\\ -4\\ -3\end{array}$	-3011420571352344125720540451	$\begin{array}{c} 144\\ 86\\ 0\\ 156\\ 213\\ 179\\ 559\\ 269\\ 136\\ 389\\ 0\\ 332\\ 697\\ 471\\ 611\\ 267\\ 239\\ 112\\ 90\\ 377\\ 324\\ 453\\ 889\\ 41\end{array}$	$\begin{array}{c} 50\\ 20\\ 90\\ 140\\ 381\\ 145\\ 229\\ 390\\ 384\\ 273\\ 333\\ 7072\\ 634\\ 279\\ 370\\ 3250\\ 4574\\ 370\\ 3250\\ 4574\\ 32\\ 370\\ 3250\\ 4574\\ 32\\ 3250\\ 4574\\ 32\\ 3250\\ 4574\\ 32\\ 3250\\ 4574\\ 32\\ 3250\\ 4574\\ 32\\ 3250\\ 4574\\ 32\\ 3250\\ 4574\\ 32\\ 32\\ 3250\\ 4574\\ 32\\ 32\\ 3250\\ 4574\\ 32\\ 32\\ 32\\ 32\\ 32\\ 32\\ 32\\ 32\\ 32\\ 32$	54 52* 35 612 24 62 40 143 14 60* 15 25 77 8 16 17 58 15 12 25 77 8 16 7 55 *	
8	-3	190	219	34	1	-9	121	122	24 59 50 *	-2 -2	-8 -6	376	371	15	
~~~~	~~~	h =	3 ^^^	~~~~	1	-5 -2	335	318	13	-2 -2	-3	211	217	14 23	
-10 -10 -10 -9 -9 -9 -9 -8	-2 2 3 4 -6 3 5 0	271 199 132 205 250 289 356 202	280 181 173 245 230 317 365 211	19 28 81* 37 36 20 30 20	1222233333333	-2 -8 -7 1 -9 -8 -7 -5 -4	325 138 0 231 176 264 504 429	315 160 66 193 65 271 504 432	16 58 50* 37 48 38 12 11	-1 -1 0 0 0 0 0 0 0 0	-6 -9 -8 -7 -6 -3 -2	186 322 0 218 386 99 120	187 333 85 23 37 398 177 136	29 14 83* 78* 39 30 55* 54	

k	1	Fo		FC	sigF	r k	1		Fo		FC	sigF	7	k	1	F	ю		FC	sigF	
0 1 1 2 3 3 4	1 -6 -5 -3 -8 -7 -8 -7 -6 -6 -6	646 111 136 157 150 497 103 0 356 108	5	639 67 133 187 177 509 26 72 18 351 58	16 56* 41 32 40 14 58* 67* 66* 14 64*	-2 -2 -2 -1 -1 0 0 0 0 0 0 1 1 1	-4 -3 -4 -9 -8 -7 -5 -3 -7 -5 -7 -7 -7 -7 -4 -75 -4		201 510 286 315 211 454 672 249 268 743 98 199 152		187 514 300 330 42 213 447 232 252 722 135 169 207	21 12 15 13 54* 40 20 36 39 64 23 59* 43 32	a.	-3	-61-36-28-62-5-10721	r 2 3 1 4 6 5 5 3	0 657 961 50 807 837 337 337 47		FC 272 320 23 163 411 165 59 541 559 338 66	S1GF 23 2553* 3253* 32 17 84* 65* 17 56* 13 45* 13 58*	
-11	0	110		68	42	2	-6		332		328	15	•		-		-	-			
-11	23	208		238 556	33 16	4	0 -6		79 59		14	67*				n =		7			
-10 -10	-5 0	413 700		420 701	21 14	~~~~		h	=	6	~~~	~~~~	-	11 10	2 -1		0 79		61 76	62* 60*	
-10 -10	1 2	200 84		185 52	33 56*	-10	-4		239		252	27		-9 -9	5 6	1	02		75 43	61* 65*	
-10	4	55		40	58*	-10	0		268		244	19		-7	-7	2	87		290	53	
-9	3	226		263	24	-10	3		1/8		85	43 65*		-7 -7	-3 -2	4	26		413 54	70*	
-8	-2	636		649	16	-10	4		38		88	58*		-7	-1	2	30		195	56	
-8	3	650		665	15	-9	-2		263		261	21		-/ -7	2	1	41		49	54 67	
-8	4	525		519	14	-9	ō		358		365	11		-7	6	4	05		409	24	
-8	7	528		553	17	-9	2		104		52	59*		-6	6	2	45		244	37	
-7	-8	396		381	15	-9	3		151		191	42		-5	-4	3	19		335	17	
-7	-5	417		409	18	-9	4		442		450	14		-5	0	3	60		350	10	
-7	-1	399		398	12	-8	-4		560		547	13		-5	5	-	20		34	50"	
-6	8	128		148	55	-8	- 2		490		496	13		-5	8	3	20		338	20	
~5	-6	051		004	10	-8	-1		222		102	72		-4		2	21		220	25	
-5	~ 5	230		211	40	-0 _0	3		1/0		103	17		-4 -1	-2	J	70		223	50*	
-0-	-4	461		AU0 A77	14	-0	יי ק		445		401	13		_4 _/	-1	/	21		122	10	
-5	- 2	327		305	12	-8	7		143		158	48		-1	ĭ	2	27		230	19	
-5	ĩ	113		108	62*	-7	-6		115		91	56*		-3	-5	1	85		113	33	
-5	2	1371	1	400	24	-6	-8		ŏ		20	74*		-2	-7	2	243		241	29	
-5	4	531	-	544	21	-6	-7		305		321	51		-2	-4	3	32		337	14	
-5	6	80		16	72*	-6	-3		0		20	69*		-2	-3	2	285		303	15	
-4	-9	90		111	65*	-6	-1		1285		1253	23		-1	-7	1	.34		63	58	
-4	2	120		62	44	-6	7		202		259	37		-1	-4	1	.45		102	40	
-4	8	233		211	30	-4	-5		142		148	53		-1	- 3	I	184		192	49 12	
-4	9	288		283	57	-4	-74		110		134	50		-1	-2	4	07		400	58*	
		674		697	14	- 4			- 93		34	37		-1	ō		61		37	52*	
-2	-9	163		166	47	-4	4		109		80	62*		-1	ĩ		48		34	54*	
-2	-6	356		338	14	-4	6		237		256	21		-1	2		0		42	58*	

k	1		Fo		FC	sigF	' k	1		Fo	FC	sigF	k	1	Fo	FC	sigF
0 0 0 0 2	-7 -5 -4 -3 0 6		157 480 0 224 312 0		159 459 148 167 307 59	50 23 73* 31 14 67*	-9 -9 -8 -8 -8	-1 0 2 -1 2 3		239 578 257 71 100 72	266 548 192 82 10 144	74 16 33 59* 58* 60*	-7 -7 -5 -5 -4	-2 1 -3 -2 3	0 113 272 185 174 97	89 152 249 162 233 123	71* 68* 19 44 45 70*
~~~~	~~~	h	=	8	~~~~	~~~~	-7	-1		111	152	63*	- 5	-2	001	003	10
-11 -9 -9 -9 -8 -8 -8 -8 -8 -8 -8 -8 -8 -8 -8 -8 -8	0 -2 0 4 5 4 -3 -2 0 1 2 3 4 5		118 227 173 141 116 498 146 460 278 340 728 477 109 237		57 207 151 156 199 497 117 429 272 337 733 490 92 158	69* 41 257 66* 176* 17 41 20 21 17 61* 47	- 7 - 6 - 6 - 5 - 4 - 4 - 4 - 4 - 4 - 2 2 2 0	-1 -3 -35 -1 26632 -1 -1		72 399 481 123 396 133 182 96 438 0 315 359 316 236	499 403 483 142 406 19 200 141 438 102 313 99 370 316 252	55 14 62 50 58 59 53 61 72 55 65					
-8	6 - 7		434		436	46	0	-3 4		58 272	28 259	84* 33					
-7	-2		0		16	57*	ĭ	-3		91	33	68*				•	
-7 -6 -6	0 -6 -3		499 154 180		487	10 38 34	~~~~	^^^	h	= 10	~~~~	~~~					
-65 -55 -55 -44 -1 -11 -11 -12 -12 -12 -12 -12 -12 -12	-3 -6 -12 54 -20 -6 -5 -3 -11 -4		180 114 301 257 46 174 345 192 501 307 306 80 279 384		164 47 281 219 104 232 34 387 189 497 44 301 319 66 205 415	34 * 59 * 160 * 36 * 15 24 13 * 23 32 * 32 * 18	-10 -9 -9 -6 -6 -5 -4 -4 -3 -3 -2 -2 0	0 -2 -5 -3 -5 -1 -4 -3 0 0 1 -1		48 257 211 113 0 184 365 0 72 127 114 203 117 644 478	177 263 196 69 179 372 23 108 148 100 134 114 622 515	65* 22 71* 68* 34 76* 63* 55 60* 285 15 20					
~~~~	~~~	h	=	9	~~~	~~~~	~~~~		h	= 11	~~~	~~~~					
-10 -10 -9	-1 1 -2		91 0 344		74 39 321	62* 67* 43	-8 -8 -8	-2 -1 1		126 501 196	127 495 167	61 15 60					

\* indicates unobserved reflection

Observed and calculated structure factor amplitudes (x10) for  $ZrNi_{1.5}Ti_{0.5}$ 

k	1	Fo	FC	sigF	' k	1	Fo	Fc	sigF	k	1	Fo	Fc	sigF	
~~~~	~~~	h =	0 ^^^	~~~~	-1 -1	2	116 1269	160 1254	29* 24	-2 -1	8 - 8	83 555	153 557	71* 14	
0	2	186	136	20	-1	4	541	525	13	-1	-6	24	101	62*	
ö	ã	1375	1361	23	-1	6	475	446	14	-1	-2	1490	1422	62	
0	6	1246	1240	24	-1	10	204	180	34*	-1	6	111	101	51*	
0	8	138	223	81*	0	-9	442	431	29	- 1	8	556	557	32	
0	10	533	544	24	0	-7	343	329	16	0	-9	201	160	81*	
1	-9	414	431	14	0	-5	355	347	16	0	-4	153	131	34*	
1	-6	435	. 446	16	0	3	1284	1254	20	0	.7	434	445	13	
Ţ	-5	349	347	11	0	10	100	548	24	1	-9	334	339	22	
1	- T	100	12	00° 05*	1	-2	1426	1/22	21	1	-0	237	207	35	
1	Ω	532	5/8	15	2	_0	1420	1422	18	1	-6	296	296	15	
2	Q	179	160		2	-7	235	235	21	1	-5	341	320	31	
ž	-6	868	856	21	2	-6	287	296	30	ĩ	-4	470	476	20	
2	õ	704	739	12	2	-5	325	320	14	2	-8	169	143	42*	
3	-7	66	61	59*	2	-4	468	476	13	2	-6	827	806	20	
3	-6	157	81	33*	3	-8	363	386	17	2	-4	800	790	34	
3	-5	94	77	52*	3	- 3	749	723	32	2	6	807	806	20	
3	-3	99	92	68*	4	-5	97	51	75*	3	-4	199	213	32	
3	-2	1062	1072	21	4	-4	0	61	89*	3	-2	0	27	56*	
4	-7	293	303	24	4	-2	719	691	38	د	2	20	21	22.	
4	-6	552	5/9	10	4	-1	0	63	62"	~~~~	~~~	۰. ۱۰	2 ^^^	~~~~	
5	- 1	anz	// ///						<b>n</b>						
Ē	1	226	211	17	-1	4	U	01	05				5		
5	4	336	314	17	**	4	h =	2 000	~~~~	- 6	0	455	461	19	
5	4	336 h =	314	17	••	4 ^^^	h =	2	~~~~	-6 -5	0 -6	455	461 295	19 36	
5	4 ~~~	336 h =	314 1 ^^^	17	-6	-1	h = 549	2 ^^^ 540	16	-6 -5 -5	0 -6 -5	455 282 141	461 295 166	19 36 48*	
-5	4 ~~~ -4	336 h = 103	314 1 ^^^ 61	17 17 64*	-6 -6	-1 1	h = 549 525	2 ^ ^ ^ · · · · · · · · · · · · · · · ·	16 40	-6 -5 -5 -5	0 -6 -5 -3	455 282 141 642	461 295 166 645	19 36 48* 42	
-5 -5	4 -4 -3	336 h = 103 103	314 1 ^^^ 61 58	17 64* 58*	-6 -6 -5	-1 -1 0	h = 549 525 82	2 ^ ^ ^ · · · · · · · · · · · · · · · ·	16 40 45*	-6 -5 -5 -5	0 -6 -5 -3 -1	455 282 141 642 0	461 295 166 645 31	19 36 48* 42 66*	
-5 -5 -5 -5	4 -4 -3 -2	336 h = 103 103 683	314 1 ^^^ 61 58 691	17 64* 58* 18	-6 -6 -5 -5	-1 -1 0 5	h = 549 525 82 207	2 ^ ^ ^ 2 540 540 68 166	16 40 45* 71*	- 6 - 5 - 5 - 5 - 5	0 -6 -5 -3 -1 1	455 282 141 642 0 70	461 295 166 645 31 31	19 36 48* 42 66* 52*	
-5 -5 -5 -5 -5	4 -4 -3 -2 2	102 336 h = 103 103 683 645	314 1 ^^^ 61 58 691 691	23 17 64* 58* 18 17	-6 -6 -5 -5 -4	-1 -1 0 5 8	h = 549 525 82 207 212	2 000 540 540 68 166 143	16 40 45* 71* 33	- 6 - 5 - 5 - 5 - 5 - 5 - 5	0 -6 -5 -3 -1 1 3	455 282 141 642 70 649	461 295 166 645 31 31 645	19 36 48* 42 66* 52*	
-5 -5 -5 -5 -5	4 -4 -3 -2 2 3	336 h = 103 103 683 645 251	314 1 ^^^ 61 58 691 691 58	23 17 64* 58* 18 17 51*	-6 -6 -5 -5 -4 -3	-1 -1 0 5 8 -8	h = 549 525 82 207 212 504	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	16 40 45* 71* 33	- 5 - 5 - 5 - 5 - 5 - 5 - 5 - 5 - 5	0 -6 -5 -3 -1 1 3 5	455 282 141 642 70 649 283	461 295 166 645 31 645 166	19 36 48* 42 66* 25 67*	
-5 -5 -55 -55 -55 -55	-4 -3 -2 23 5	336 h = 103 103 683 645 251 185	314 1 ^^^ 61 58 691 691 58 51	23 17 64* 58* 18 17 51* 39*	-6 -6 -5 -5 -4 -3 -3	-1 -1 0 5 8 -8 -3	h = 549 525 82 207 212 504 898	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	16 40 45* 71* 33 15 24		0 -6 -5 -1 1 3 5 6	455 282 141 642 70 649 283 312	461 295 166 645 31 645 166 295	19 36 48* 42 66* 25 67* 18	
-5-55-55-74	-4 -3 -2 2 3 5 3	103 h = 103 103 683 645 251 185 720	314 1 ^^^ 61 58 691 691 58 51 723	23 17 64* 58* 18 17 51* 39*	-6 -6 -5 -5 -4 -3 -3 -3	-1 -1 0 5 8 -8 -3 -1	h = $549$ 525 82 207 212 504 898 60	2 ^ ^ ^ 540 540 68 166 143 507 875 64	16 40 45* 71* 33 15 24 51*	655555554	0 -6 -5 -1 1 3 5 6 -7	455 282 141 642 70 649 283 312 216	461 295 166 645 31 645 166 295 215	19 36 42 66* 25 67* 18 32	
-5 -5 -5 -5 -5 -5 -5 -5 -5 -4	4 -4 -3 -2 3 5 3 8	103 h = 103 103 683 645 251 185 720 401	1 ^^^ 61 58 691 691 58 51 723 386	17 64* 58* 18 17 51* 39* 33 16	-6 -6 -5 -5 -3 -3 -3 -3	-1 -1 0 5 8 -8 -3 -1 0	h = 549 525 82 207 212 504 898 0 69	2 ^ ^ ^ 540 540 68 166 143 507 875 64 96	16 40 45* 71* 33 15 24 51* 36*		0 -6 -5 -1 1 5 -7 -6	455 282 141 642 0 70 649 283 312 216 314	461 295 166 645 31 645 295 215 205	19 36 48 52 52 52 52 7 18 32 18	
-5 -55 -55 -55 -55 -44 -3	4 -4 -3 -2 3 5 3 8 -2	103 h = 103 103 683 645 251 185 720 401 214 242	1 ^^^ 61 58 691 691 58 51 723 386 209	64* 58* 18 17 51* 39* 33 16 33	-6 -6 -5 -5 -4 -3 -3 -3 -3 -3	-1 -1 0 5 8 -3 -1 0 1 7	h = 549 525 82 207 212 504 898 0 69 111 238	2 ^ ^ ^ 540 540 68 166 143 507 875 64 96 64 235	16 40 45* 71* 33 15 24 * 36* 29*		0 -5 -3 -1 -5 -7 -7 -5 -7 -5	455 282 141 642 0 70 649 283 312 216 314 261 321	461 295 166 645 31 645 295 215 305 215 305 310	19 36 48* 42 66* 52* 25 67* 18 32 16 18	
-5 -55 -55 -55 -55 -4 -33 	4 -4 -3 -2 3 5 3 8 -2 2 4	103 h = 103 103 683 645 251 185 720 401 214 242 485	1 ^^^ 61 58 691 691 58 51 723 386 209 475	17 64* 58* 18 17 51* 39* 33 16 33 13	-6 -6 -5 -5 -4 -3 -3 -3 -3 -3 -3 -3 -3	-1 -1 0 5 8 -3 -1 0 1 7 -8	h = 549 525 82 207 212 504 898 0 69 111 238 132	2 ^ ^ ^ 540 540 68 166 143 507 875 64 96 64 235 153	16 40 45* 71* 33 15 24 51* 36* 36* 36*		0 -5 -1 -5 -1 -5 -6 	455 282 141 642 0 70 649 283 312 216 314 261 321 68	461 295 166 645 31 645 295 215 305 244 310 645 295 244 305 244	19 36 48* 42 66* 52* 67* 18 32 16 18 14 58*	
-5 -55 -55 -55 -54 -333 	4 -4 -22 35 -22 -22 -22 -22 -22 -22 -22 -22 -22 -2	$h = 103 \\ 103 \\ 683 \\ 645 \\ 251 \\ 185 \\ 720 \\ 401 \\ 214 \\ 242 \\ 485 \\ 303 \\ 303 \\ $	1 ^^^ 61 58 691 691 58 51 723 386 209 209 209 209 209	17 64* 58* 18 17 51* 39* 33 16 33 13 13 28	-6 -6 -5 -5 -4 -3 -3 -3 -3 -3 -3 -3 -3 -3 -3 -3 -3 -3	-1 -1 0 5 8 -3 -1 0 1 7 -8 -5	h = 549 525 82 207 212 504 898 0 69 111 238 132 1278	2 ^ ^ ^ 540 540 68 166 143 507 875 64 96 64 235 153 1271	16 40 45 71 33 15 24 51 54 51 54 51 54 51 54 51 54 51 54 51 54 51 54 51 54 51 54 51 54 51 54 55 54 55 54 55 55 55 55 55 55 55 55		0 -6 -5 -1 3 5 6 7 -6 -5 -7 -5 -5 -2 -2 -1	455 282 141 642 0 70 649 283 312 216 314 261 321 68 73	461 295 166 645 31 645 295 215 305 244 310 25 244 310	19 36 42 52 52 67 18 32 16 18 14 58 48	
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-1	-8	479	507	14	-3	-1	76	25	57*	-4	-2	
-1	-6	293	296	15	-3	· 0	67	19	42*	-4	0	
-1	-5	329	320	13	-3	1	0	25	63*	-4	2	
-1	-4	484	476	12	-3	2	111	88	62*	-4	3	
-1	-3	916	875	29	-3	3	746	723	38	-2	-3	
-1	-2	209	209	46*	-3	7	235	215	22	-2	-1	
-1	2	206	209	40*	-2	-4	827	790	38			
0	-8	495	477	26	-2	-2	0	63	57*			
0	-7	95	61	58*	-2	0	1648	1743	25			
0	-5	0	77	60*	-2	2	136	63	39*			
0	-4	110	107	57*	-1	-8	379	386	19			
0	-3	128	92	63*	-1	-5	256	244	24			
0	-2	1060	1072	29	-1	-4	334	310	27			

$\begin{array}{c} -2\\ -2\\ -2\\ -2\\ -2\\ -2\\ -1\\ -1\\ -1\\ -1\\ -1\\ -1\\ -1\\ -1\\ 0\\ 0\\ 0\\ 0\end{array}$	-63 -10 39 -65 -54 -28 -75 -75 -4	292 926 0 114 871 348 479 293 329 484 916 209 206 495 95 0 110	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4 5 7 -6 -5 -4 -1 1 2 3 7 -2 0 2 8	122 849 315 212 320 219 324 76 67 0 111 746 235 827 0 1648 136 379	75 835 303 215 244 310 25 88 723 215 790 63 1743 386	40* 39 18316* 418* 572** 62* 38228* 225* 39	-1 0 -5 -4 -4 -4 -4 -4 -2 -2	3 1 -3 -2 0 2 3 -3 -1	$ \begin{array}{r} 0 \\ 0 \\ 111 \\ 213 \\ 261 \\ 233 \\ 68 \\ 0 \\ 548 \\ \end{array} $	6	58 57 23 32 219 301 219 32 32 540	698 68 61 58 41 23 681 15
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\* indicates unobserved reflection

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